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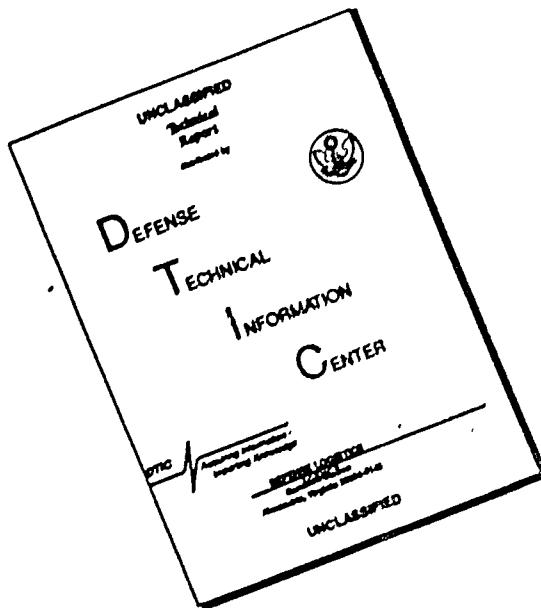
AD 340 380

Final Report
DATA PROCESSING SYSTEMS INC.
DATA PROCESSING SYSTEMS INC.

100-100-Extract-Section-10

UNION CARBIDE CORPORATION

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UNION CARBIDE CORPORATION
DEFENSE AND SPACE SYSTEMS DEPARTMENT

UCC/DSSD - 299

Final Report

LOW ENERGY PHOTOELECTRIC CROSS
SECTION CALCULATIONS

Vol. II: Program Description

A. Glick and H. Brysk

July 31, 1967

OCT 8 1968

Work Performed under Contract No. DA-49-146-XZ-511

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FOREWORD

This report was prepared by the Union Carbide Corporation, Defense and Space Systems Department, White Plains, New York, under Contract DA-49-146-XZ-511, Project 5710, funded by the Defense Atomic Support Agency (DASA). Inclusive dates of research were 1 June 1966 to 30 June 1967. The report was submitted 31 August 1967 by the AFWL Technical Monitor, Captain Guy Spitale (WLRP).

The report has been divided into two volumes for convenience. Volume I presents the theoretical analysis and the discussion of results. Volume II is a detailed description of the program.

The project was initiated and formulated by Dr. C. D. Zerby. The theoretical derivation was completed by Dr. H. Brysk, who also planned and analyzed the calculations. Programming support was supplied by Mr. A. Glick in writing the program and by Mr. E. C. Imperatore in resolving the systems problems of transcribing the tapes containing the Los Alamos Scientific Laboratory (LASL) self-consistent-field data to the UCC and the AFWL operating systems. The program is written in FORTRAN IV and is operational on the CDC 6600 computer at AFWL. We thank Dr. J. T. Waber (of LASL) who supplied us the output of his self-consistent-field program on tape.

This report has been reviewed and is approved.

ABSTRACT

A computer program was developed for the calculation of photoelectric cross sections, including angular distributions, using as input the results of a relativistic Dirac-Slater self-consistent-field program. The program was used to calculate the aluminum cross sections over the range from 1 to 150 kev and uranium cross sections at four energies within that range, and the results were correlated with pre-existent experimental and theoretical data.

Volume I presents the theoretical analysis and the discussion of results. Volume II is a detailed description of the program.

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I. INTRODUCTION

This volume is a self-contained description of a program (PELEC) for the computation of photoelectric cross sections. The companion volume (VCC/DSSD - 299, Volume I) develops the theory used and discusses the results obtained with the program.

Chapter II contains the operating instructions. It describes the input cards and self-consistent-field data tape required. The utilization of a test option to ascertain the optimum input parameters in a series of runs is indicated.

Chapter III presents sample output.

Chapter IV exhibits the program itself. For each routine, its purpose and the method of achieving it are stated. The routines it calls and those it is called by are given, as well as the Common blocks it uses and the calling sequence (if any). The variables are defined. A schematic flow chart is provided. Finally, the routine is listed.

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II. OPERATING INSTRUCTIONS

This chapter gives all the operational details needed in order to run the photoelectric program. The input variables and format are listed, along with the program diagnostics. Tape unit assignments are given and the test option is described.

Input Variables

A complete set of data consists of a single data card. The variables described below are read in on a format (9I5, 2E15.8):

5	10	15	20	25	30	35	40	45	60	75
JM	KMAX	LM	NTAPE	NEDGE	IA	IB	IZ	L _{00P}	QV	SAVE

Upon completion of a problem, the program recycles, reading in the next data card. Termination of the program is obtained by setting the flag value NEDGE = -1.

Name	Dimensions	Mode	Meaning
JM		I	Maximum order of Legendre coefficient
KMAX		I	Maximum κ for electron
LM		I	Maximum l for photon
NTAPE		I	The logical tape unit assigned for tape containing the self-consistent-field data
NEDGE		I	= -1: terminates Program = 0: normal run > 0: sets photon energy to NEDGE th binding energy
IA		I	= 0: normal case > 0: calculation commences after IA shells
IB		I	= 0: calculation to include outermost shell > 0: calculation cuts off after IB shells
IZ		I	Atomic number
L _{00P}		I	= 0: normal case = 1: photon angular momentum reduction
QV		R	Photon energy in keV
SAVE		R	Total cross section accumulation from previous run; = 0 ordinarily.

Input Testing

The program sifts the input data to insure that certain criteria are not violated. If any difficulty is observed, a violation signal is printed and the run terminated. Listed below in abbreviated form are the criteria that must be satisfied and that the program tests for:

$\text{MIN} (\text{JM}, \text{KMAX}, \text{LM}, \text{IA}, \text{IB}) \geq 0$

$2 < \text{IZ} < 102$

$\text{QV} > 0$

$\text{LopP} = 0 \text{ or } 1$

$\text{NEDGE} \leq \text{JX}$

$\text{IA} < \text{JX}$

$\text{IB} \leq \text{JX}$

$\text{NK}, \text{NKP} \leq 200$

In addition to the above the program examines the following variables and alters them if necessary:

$\text{JM} > 2^4$, program sets $\text{JM} = 2^4$, prints this fact and proceeds.

$\text{KMAX} > 12$, program sets $\text{KMAX} = 12$, prints this fact and proceeds.

$\text{LM} > 12$, program sets $\text{LM} = 12$, prints this fact and proceeds.

This is to insure that the dimension size of the variable of the program as written for the IBM 7094 is not exceeded.

Program Options

The program has two option procedures controlled by LopP and by the combination of values of IA , IB , and SAVE .

By setting $\text{LopP} = 1$, we can reduce the original angular momentum quantity LM (max 1 for photon) in unit increments (until a minimum of one is reached). The selection rules may then reduce the range limits KM and JM . The summing process is repeated to recalculate the differential and total cross sections.

By altering the input values IA and IB we can segment a run. The program proceeds through IB electron shells rather than the totality of shells (JX). The total cross section up to that point can be fed back in as part of the input (SAVE) when the user desires to continue the run. With IA greater than zero, the program starts after the first IA electron shells. This process is useful when long computer running time is not available.

System Information

The program as run at the New York Regional Computer Center utilizes the following tapes:

Logical tape unit 5	Read
Logical tape unit 6	Write
Logical tape unit 1	Self-consistent-field data

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III. SAMPLE OUTPUT

The output from an actual run is given. The complete output contains the differential cross section for each subshell in succession. Only one subshell is reproduced here, for economy.

INPUT DATA FOR PHOTOELECTRIC CALCULATION

INPUT CARD READS

JM	KMAX	LM	NIAPE	NEUGE	IA	IB	IZ	LCOP	0V	SAVE
11	0	4	1	0	0	0	13	0	0.1000000E 02	C.

INPUT DATA FOR PHOTOELECTRIC CALCULATION

13 = NUCLEAR CHARGE
10.000 = PHOTON ENERGY
0 = MAX KAPPA FOR ELECTRON
4 = MAX L FOR PHOTON
11 = MAX J (LEGENDRE COEFF.)

TAPE POSITIONED PROPERLY.

AL = ELEMENT
13 = ATOMIC NUMBER
6 = NUMBER OF ELECTRON SHELLS
0.1944370E 00 = SCREENING FACTOR OF OUTERMOST LOUD ELECTRON
257 = RADIAL GRID UP TO X = 1.0
1281 = RADIAL GRID UP TO X = 65.0
1436 = TOTAL RADIAL GRID
0.82222162E 04 = OUTERMOST RADIAL VALUE

IS1/2 = SHELL
0.27269274E 03 = INTEGRATION CUT-OFF
1327 = NUMBER OF WAVE FUNCTION GRID POINTS
5 = MAX KAPPA FOR THIS SHELL
25 = NUMBER OF MATRIX ELEMENTS FOR THIS SHELL

LENGTH UNITS ARE HBAR / MC (1 BOHR RADIUS = 137)

INTEGRATION STEP SIZE IS 0.007E125 UP TO 1.000

INTEGRATION STEP SIZE IS 0.125E000 UP TO 65.000

INTEGRATION STEP SIZE IS 1.000E000 UP TO 272.693

11 = MAX J (LEGENDRE COEFF.)

5 = MAX KAPPA FOR ELECTRON

4 = MAX L FOR PHOTON

LEGENDRE COEFFICIENTS OF CROSS SECTION

J	U(J)
0	0.84832748E 02
1	0.34841149E 02
2	-0.76300052E 02
3	-0.33218458E 02
4	-0.829068764E 01
5	-0.15982244E 01
6	-0.22848516E 00
7	-0.24035064E -01
8	-0.20669956E -02
9	-0.11737233E -03

ELEMENT	ATOMIC NUMBER	SHELL
AL	13	1S1/2
BINDING ENERGY	PHOTON ENERGY	ELECTRON KINETIC ENERGY
1.5499309 KEV	10.0000000 KEV	8.4500691 KEV

UNPOLARIZED CROSS SECTION (BARNES/STERADIAN)

THETA	COS THETA	CROSS SECTION	ANG. DIST.
0	1.0000000	0.104827e5E-01	0.0000778
2	0.9993906	0.31837447E 00	0.0023632
4	0.9975640	0.12387132E 01	0.0091947
6	0.9945219	0.27615944E 01	0.0204986
8	0.9902661	0.48706563E 01	0.0361540
10	0.9848078	0.75433565E 01	0.0559929
12	0.9781476	0.10751303E 02	0.0798049
14	0.9702957	0.14460679E 02	0.1073389
16	0.9612617	0.18632747E 02	0.1383074
18	0.9510565	0.23224424E 02	0.1723906
20	0.9395926	0.28188594E 02	0.2092409
22	0.9271839	0.33476281E 02	0.2484882
24	0.9135455	0.39034332E 02	0.2897446
26	0.8987940	0.44809127E 02	0.3326098
28	0.8829476	0.50745737E 02	0.3766766
30	0.8660254	0.56789170E 02	0.4215355
32	0.8480481	0.62834551E 02	0.4667804
34	0.8290376	0.68978249E 02	0.5120127
36	0.8090170	0.75018242E 02	0.5568465
38	0.7880108	0.80954596E 02	0.6009117
40	0.7660444	0.86740401E 02	0.6438584
42	0.7431448	0.92331445E 02	0.6853596
44	0.7193398	0.97687210E 02	0.7251140
46	0.6946584	0.10277077E 03	0.7628484
48	0.6691306	0.10754931E 03	0.7983186
50	0.6427876	0.11199406E 03	0.8313111
52	0.6156615	0.11608047E 03	0.8616438
54	0.5877853	0.11978819E 03	0.8891655
56	0.5591929	0.12310107E 03	0.9137564
58	0.5299193	0.12600702E 03	0.9353268
60	0.5000000	0.12849794E 03	0.9538164
62	0.4694716	0.13056947E 03	0.9691930
64	0.4383712	0.13222024E 03	0.9814509
66	0.4067366	0.13345459E 03	0.9906087
68	0.3746066	0.13427632E 03	0.9967063
70	0.3420202	0.13460443E 03	0.9998118
72	0.3090170	0.13471478E 03	1.0000000
74	0.2756374	0.13436550E 03	0.9973702
76	0.2419219	0.13364660E 03	0.9920340
78	0.2079117	0.13257975E 03	0.9841149
80	0.1736482	0.13118296E 03	0.9737468
82	0.1391731	0.12947556E 03	0.9610716
84	0.1045285	0.12747693E 03	0.9462376

56	0.0697565	0.12520828E 03	0.9293979
58	0.0348995	0.12269040E 03	0.9107082
60	0.0000000	0.11994453E 03	0.8903260
62	-0.0348995	0.11699190E 03	0.8684091
64	-0.0697564	0.11385362E 03	0.8451144
66	-0.1045284	0.11055058E 03	0.8205965
68	-0.1391731	0.10710323E 03	0.7950075
70	-0.1736482	0.10353156E 03	0.7684956
72	-0.2079117	0.99854979E 02	0.7412050
74	-0.2419219	0.96092227E 02	0.7132748
76	-0.2756373	0.92261351E 02	0.6848389
78	-0.3090170	0.88379639E 02	0.6560257
80	-0.3420201	0.84463592E 02	0.6269576
82	-0.3746066	0.80528891E 02	0.5977510
84	-0.4067366	0.76590403E 02	0.5685164
86	-0.4383711	0.72662151E 02	0.5393577
88	-0.4694715	0.68757333E 02	0.5103729
90	-0.5000000	0.64888321E 02	0.4816540
92	-0.5299192	0.61066679E 02	0.4532866
94	-0.5591929	0.57303176E 02	0.4253509
96	-0.5877852	0.53607805E 02	0.3979208
98	-0.6156615	0.49989820E 02	0.3710652
100	-0.6427876	0.46457748E 02	0.3448472
102	-0.6691306	0.43019425E 02	0.3193252
104	-0.6946593	0.39682028E 02	0.2945523
106	-0.7193398	0.36452100E 02	0.2705772
108	-0.7431448	0.33335594E 02	0.2474439
110	-0.7660444	0.30337900E 02	0.2251926
112	-0.7880107	0.27463871E 02	0.2038592
114	-0.8090170	0.24717871E 02	0.1834762
116	-0.8290376	0.22103803E 02	0.1640724
118	-0.8480481	0.19625136E 02	0.1456737
120	-0.8660254	0.17284947E 02	0.1283030
122	-0.8829476	0.15085945E 02	0.1119602
124	-0.8987940	0.13030508E 02	0.0967230
126	-0.9135454	0.11120710F 02	0.0825470
128	-0.9271638	0.93583400E 01	0.0694652
130	-0.9396926	0.77449520F 01	0.0574893
132	-0.9510565	0.62818086E 01	0.0466291
134	-0.9612617	0.49702084E 01	0.0368929
136	-0.9702957	0.38109178E 01	0.0282977
138	-0.9781476	0.28047778E 01	0.0208161
140	-0.9848078	0.19524343F 01	0.0144926
142	-0.9902681	0.12544079E 01	0.0093112
144	-0.9945219	0.71109624E 00	0.0052783
146	-0.9975640	0.32280832E 00	0.0023961
148	-0.9993908	0.89753443E-01	0.0006662
150	-1.0000000	0.12053592E-01	0.0000995

INTEGRATED CROSS SECTION = 0.10660397E 04 MBARS

ELEMENT	ATOMIC NUMBER
AL	13

PHOTON ENERGY = 10.0000000 KEV

TOTAL CROSS SECTION = 0.11461591E 04 BARNs

IV. THE PROGRAM

The program is written in FORTRAN IV. The versions used on the IBM 7094 and the CDC 6600 are identical except for control cards. The data tapes contain the same information in binary form, but are not compatible between the two machines.

All the Common blocks appear in the main routine (PELEC). The definition of the Common variables is given first. In the subroutines, Common blocks used are quoted. The unlabelled Common is the same wherever it appears.

Definition of Variables in COMMON

Unlabelled Common: Length 107₈

Name	Dimensions	Mode	Meaning
PI		R	π
HALFPI		R	$\pi/2$
FOURPI		R	4π
RAD		R	$\pi/180$
SQ2		R	$2^{-1/2}$
Q		R	Photon energy (in mc^2 units)
ZA		R	Atomic number
ZAZA		R	$ZA * ZA$
EFN		R	Free electron energy -1 (in mc^2 units)
EGN		R	Free electron energy +1 (in mc^2 units)
V		R	Potential; screening factor/radius
CG	30	R	$-\kappa - \gamma$ if radius < 1; $-\kappa$ if radius > 1
GAM	30	R	$\sqrt{\kappa^2 - ZAZA}$

/BESSEL/ Common: Length 420₈

Name	Dimensions	Mode	Meaning
FL	15	R	Numerical factors used in the construction of the spherical Bessel function.
PC	15	R	
φF	15 x 15	R	
M1		I	Largest order of Bessel function needed
M2		I	M1 + 1
B	15	R	Spherical Bessel function

/DFUNC/ Common: Length 1047₈

Name	Dimensions	Mode	Meaning
F	30	R	"Small" component of free-electron wavefunction
G	30	R	"Large" component of free-electron wavefunction
DF	30	R	Derivative of F
DG	30	R	Derivative of G
DFK	200	R	Integrand for matrix elements $K_{\ell}(\mu\mu')$
DFKP	200	R	Integrand for matrix elements $K_{\ell}(\mu'\mu)$
CF	30	R	$\mu - \gamma$ if radius < 1; μ if radius > 1
H		R	Integration step size

/FAC/Common: Length 324₈

Name	Dimensions	Mode	Meaning
FACT	67	R	Numerical factors used in the calculation of the Clebsch-Gordan coefficients.
RTFACT	95	R	
ROOT	50	R	

/FID\$/ Common: Length 746₈

Name	Dimensions	Mode	Meaning
FI	30 x 15	R	$\phi(\mu, \lambda)$
D	30	R	Legendre coefficient of cross section
JMP		I	Max. order of Legendre coefficient + 1
NAME		ALFA	Element
SHELL		ALFA	Electron shell
QV		R	Photon energy (in keV units)
EB		R	Binding energy of shell (in keV units)
IZ		I	Atomic number

/KUT/ Common: Length 24₈

Name	Dimensions	Mode	Meaning
RK1	4	R	Numerical coefficients used for the Runge-Kutta integration (Gill Form)
RK2	4	R	
RK3	4	R	
RK4	4	R	
K4	4	I	

/LIMIT/ Common: Length 13₈

Name	Dimensions	Mode	Meaning
JM		I	Max order of Legendre coefficient
LM		I	Max ℓ for photon
KM		I	Max κ for free electron
K2M		I	2 * KM; number of free electron states
IEND		I	Flag for zero electron kinetic energy state
NEW		I	Flag to save repetition of calculation when radius is not advanced
NK		I	Number of matrix elements $K_{\ell}(\kappa\kappa')$
NKP		I	Number of matrix elements $K_{\ell}(\kappa'\kappa)$
JKB		I	Twice j_{κ} ,
LMKB		I	$\ell_{-\kappa'}$
NTAB		I	Radial index in bound state tabulation

/MAT/ Common: Length 1535₈

Name	Dimensions	Mode	Meaning
SF	30	R	Integration storage variable for "small" component of free electron wavefunction
SG	30	R	Integration storage variable for "large" component of free electron wavefunction
FK	200	R	Matrix elements $K_{\ell}(\kappa\kappa')$
FKP	200	R	Matrix elements $K_{\ell}(\kappa'\kappa)$

Name	Dimensions	Mode	Meaning
SPK	200	R	Integration storage variable for matrix elements $K_{\mu\mu'}$
SF1..P	200	R	Integration storage variable for matrix elements $K_{\mu\mu'}$
RCUT		R	Cut-off radius for integration

/QUANT/ Common: Length 322₈

Name	Dimensions	Mode	Meaning
LK	30	I	l_n
LMK	30	I	l_{-n}
JK	30	I	Twice j_n
FKAP	30	R	κ
SN	30	R	Sign of κ
SI	30	R	Sine of phase shift
CR	30	R	Cosine of phase shift

/ONWARD/ Common: Length 48

Name	Dimensions	Mode	Meaning
RX		R	Radial variable beyond radial cutoff on uniform grid tabulation
SCX		R	Interpolated value of screening factors
GBX		R	Interpolated value of "large" component of wavefunction
FBX		R	Interpolated value of "small" component of wavefunction

/TAPES/ Common: Length 13562₈

Name	Dimension	Mode	Meaning
X	1500	R	Radial value
SCF	1500	R	Screening factor
FB	1500	R	"Small" component of bound state wavefunction

Name	Dimensions	Mode	Meaning
GB	1500	R	"Large" component of bound state wavefunction
GAMB		R	$\sqrt{x^2 - ZAZA}$ for bound state
SCREEN		R	Normalization factor for least bound electron

/TRANS/ Common: Length 1700₈

Name	Dimensions	Mode	Meaning
HF	30 x 15	R	H (μ, μ') for $\mu' > 0$
HFM	30 x 15	R	H (μ, μ') for $\mu' < 0$
JNG	30	I	(μ') max + 1/2
JPS	30	I	(μ') max + 1/2 provided $\mu' > 0$ permitted; -1 otherwise

/VECT/ Common: Length 1441₈

Name	Dimensions	Mode	Meaning
KF	200	I	Index for μ values for $K_{\ell}(\mu' \mu)$
KG	200	I	Index for μ values for $K_{\ell}(\mu \mu')$
LBES	200	I	Photon angular momentum + 1 for $K_{\ell}(\mu' \mu)$
LBS	200	I	Photon angular momentum + 1 for $K_{\ell}(\mu \mu')$
LKB		I	$\ell_{\mu'}$

ROUTINE PELEC

Purpose: This is the main program. It serves as the control section, reading the input cards and the tape containing the self-consistent-field data and setting up the calculations. Nearly all the actual computation is done in subroutines.

Method: Numerical constants are computed and stored, the input read and checked (and diagnostics printed, if needed), then printed with interpretation; the tape is scanned for the element required and the data read from it and interpreted. For each subshell, SINDEX is called to set up the matrix elements and their quantum numbers, RADINT to perform the radial integrations. LEGEND is called to perform the angular momentum sums, ANGLE to produce the differential cross section (headings are supplied for the tables printed in the subroutines); if the matrix reduction option is called for, the cutoff values of the quantum numbers are reduced and the program loops back through the angular sums. The total cross section is accumulated in PELEC and printed out. The program recycles to read the next input card and perform the next case, until a flag on the input card signals termination.

Subroutines called: SINDEX, RADINT, LEGEND, ANGLE, HUM

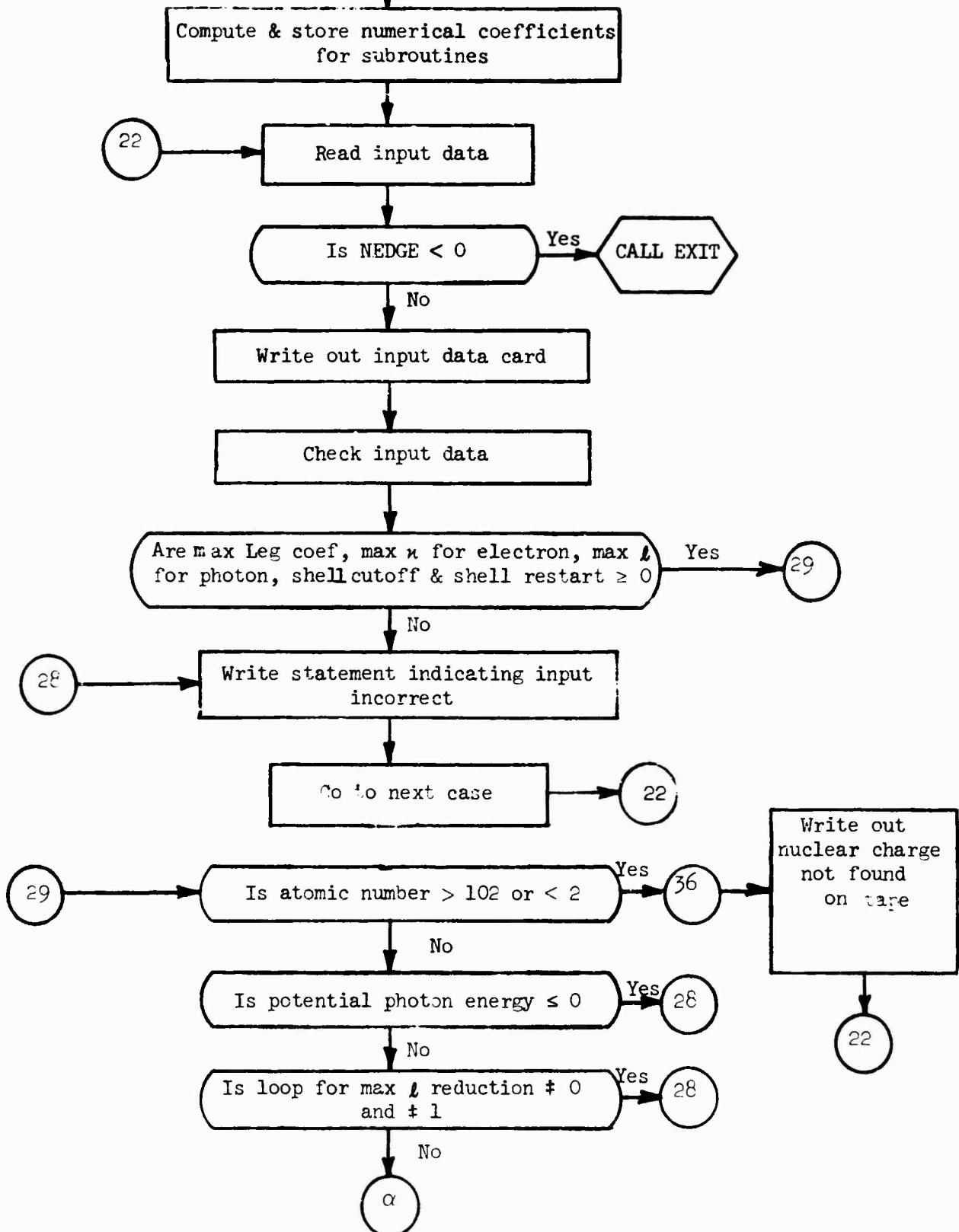
Variables in unlabelled Common: PI, HALFPI, FOURPI, RAD, SQ2, Q, ZA, ZAZA, EFN, EGN, V, CG, GAM

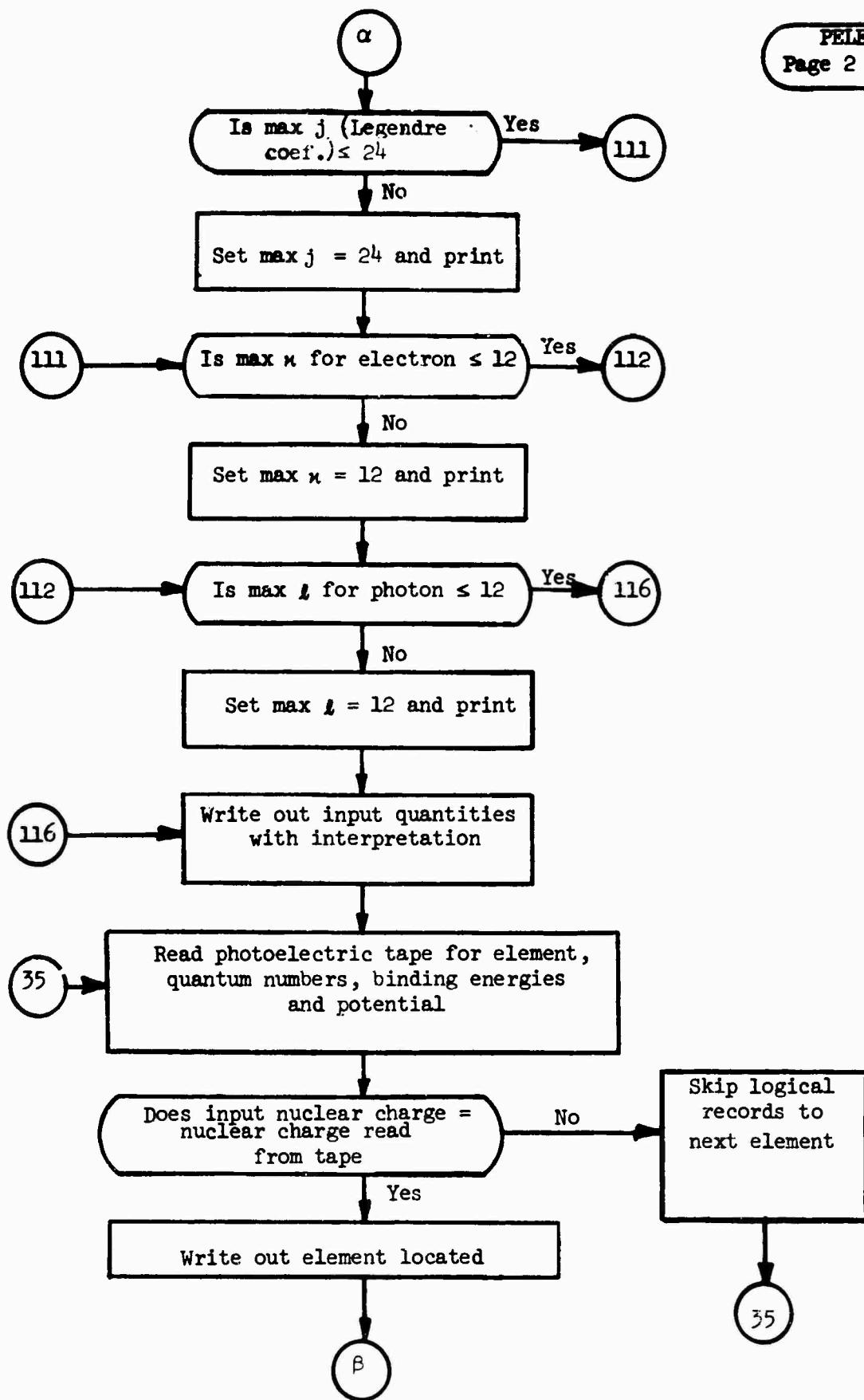
Labelled Common: BESSEL, DFUNC, FAC, FID, KUT, LIMIT, MAT, QUANT, INWARD, TAPES, TRANS, VECT

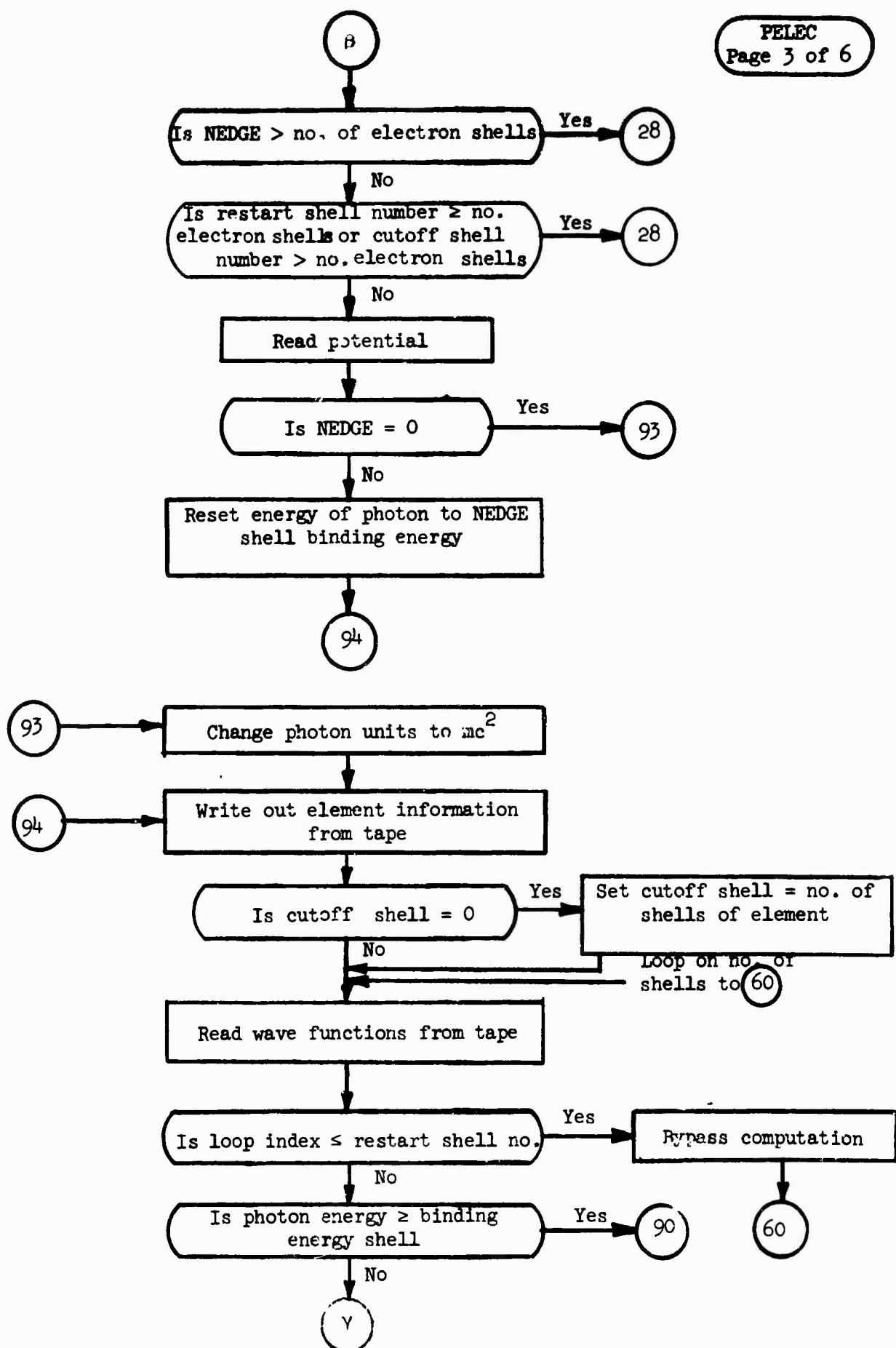
Local Variables:

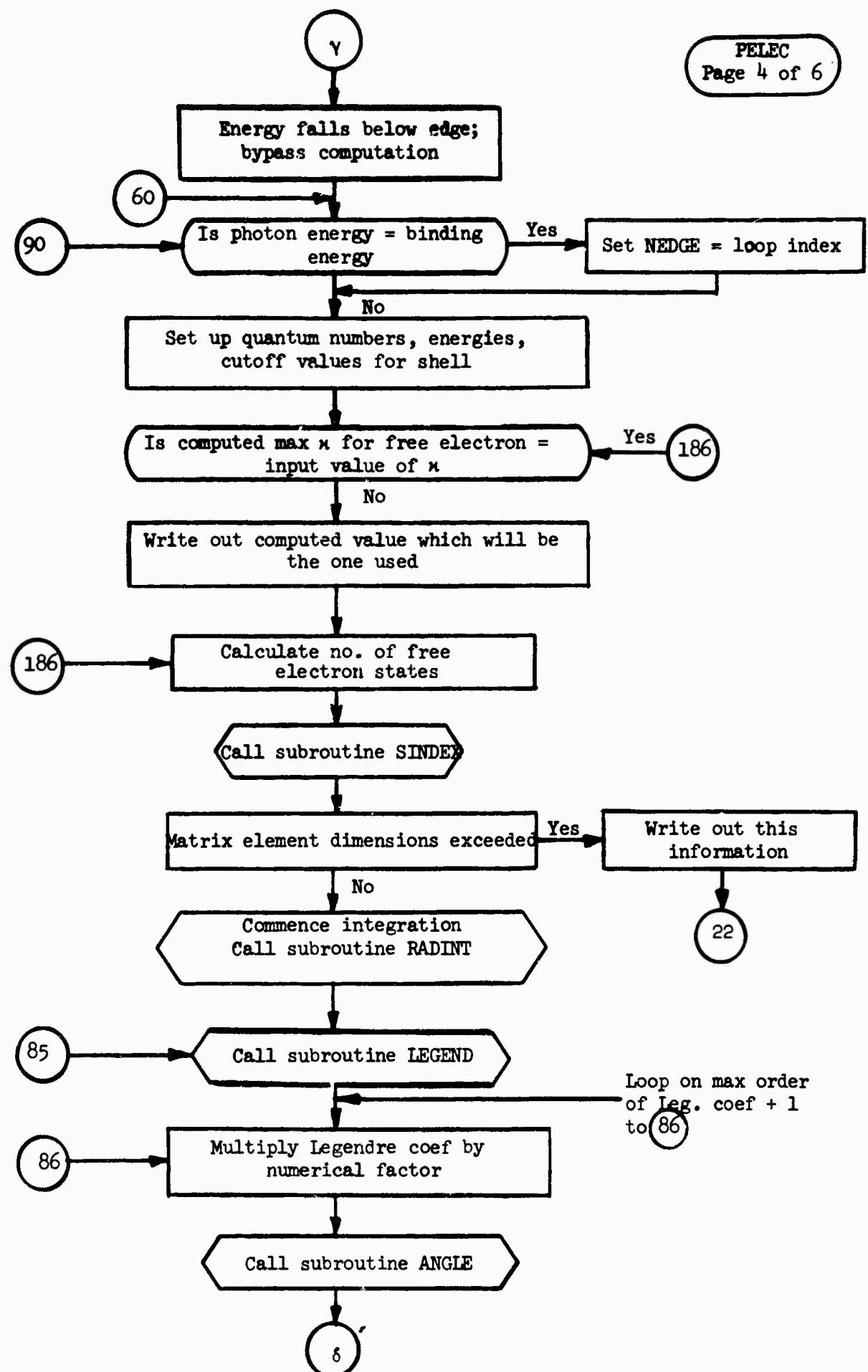
Name	Dimension	Mode	Meaning
KMAX		I	Input max n for free electron
NTAPE		I	The logical tape unit assigned for tape containing the self-consistent-field data
NEDGE		I	= -1 terminates program = 0 normal run = integer sets photon energy to NEDGEth binding energy
IA		I	= 0 normal case > 0 calculation commences after IA shells
IB		I	= 0 calculation includes outermost shell > 0 cuts off calculation after IB shells
LDP		I	= 0 normal case = 1 for photon angular momentum reduction
QV		R	Input photon energy in keV
SAVE		R	Input total cross section; accumulation from previous run; = 0 otherwise
IZ		I	Input atomic number
NGRID		I	Number of grid points in table
RSIXFI		I	Number of grid points for radial value of 65 (1/2 Bohr unit)
RDNE		I	Number of grid points for radial value of one
RSIXFI		R	Radial value of 65, read from tape
RDNE		R	Radial value of one, read from tape
ZTRY		R	Atomic number read from tape
JX		I	Number of electron shells
XN	36	ALFA	Shell identification
XL	36	R	l_n
XJ	36	R	j_n
XZ	36	R	Shell occupancy

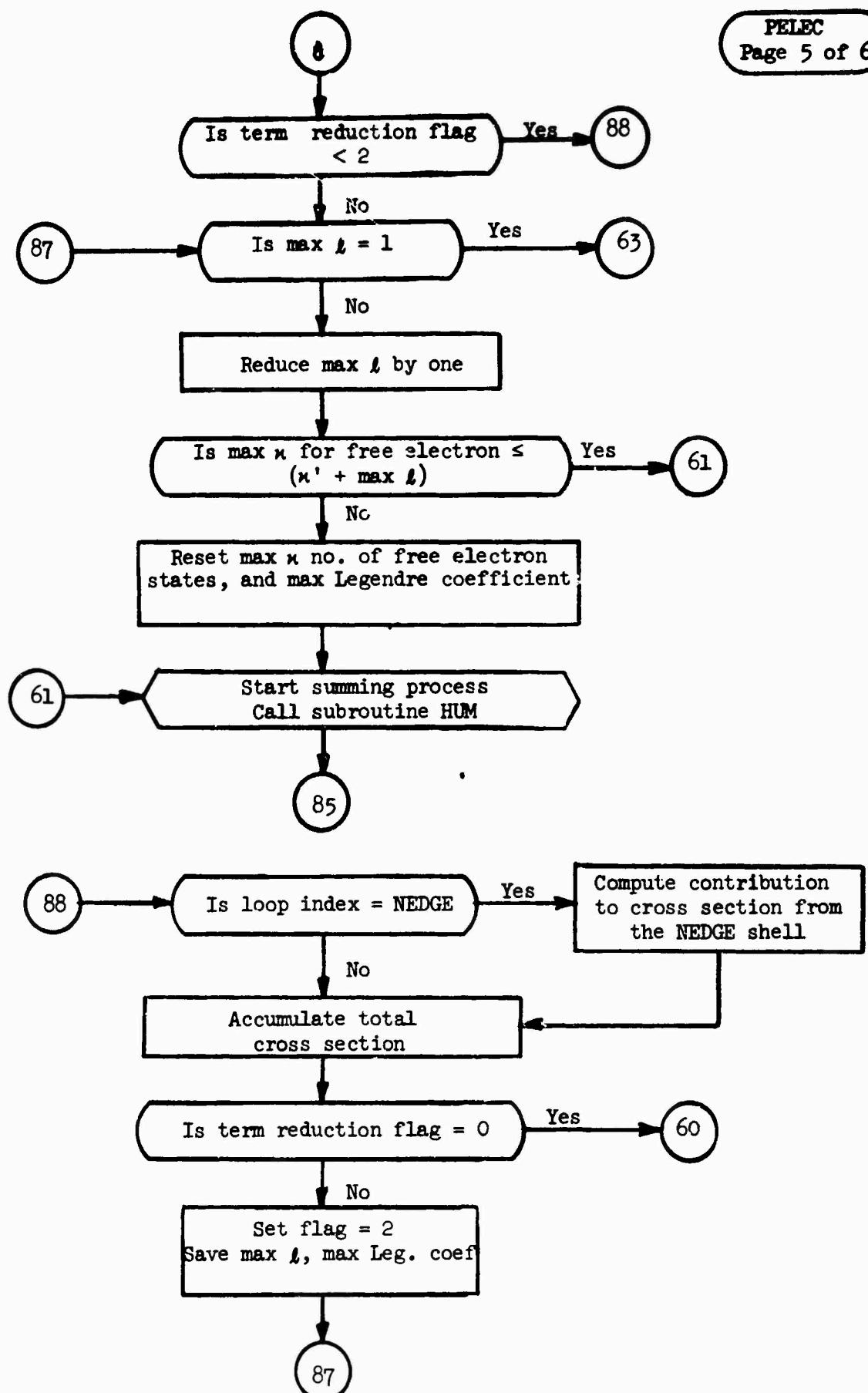
Name	Dimension	Mode	Meaning
ERG	36	R	Binding energy
KJI		I	Number of wavefunction grid points
SECT		R	Total cross section
NTOT		I	Number of matrix elements for shell
SEDGE		R	Cross section jump at edge
LMS		I	Initial max ℓ (in loop reduction)
JMS		I	Initial max order of Legendre coefficient (in loop reduction)
JPS		I	Initial max order of Legendre coefficient + 1 (in loop reduction)
CCM		R	Conversion factor (keV/mc ²)
ALFA		R	Fine structure constant: 1/137.0367
REL		R	Classical electron radius (in cm) $\times 10^{12}$
KB		I	j_{μ}
FKB		R	j_{μ}

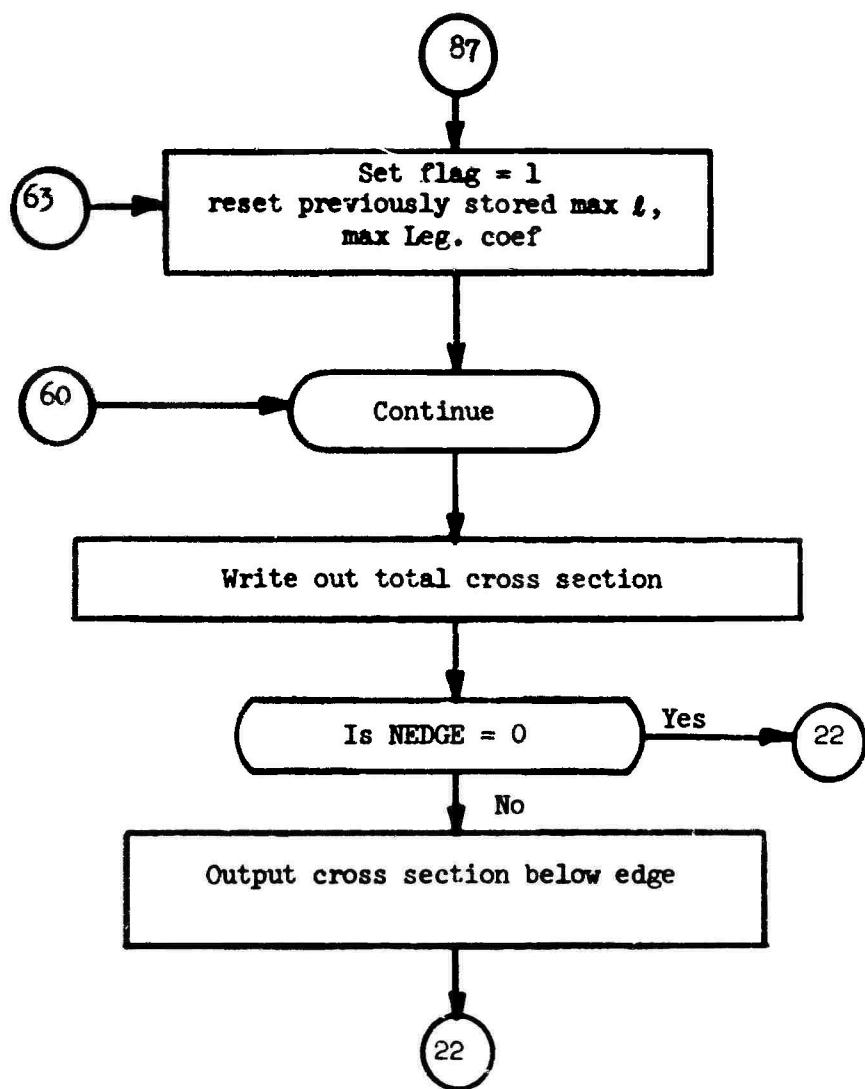












SIBYL PELEC

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C      FOR LUC 66UU OPERATION, ADD CARD READING
C      PROGRAM PELEC(INPUT,OUTPUT,TAPE1,TAPE5=INPUT,TAPE6=OUTPUT)
COMMON PI,HALFPI,FOURPI,RAD,SQ2=Q,ZA,ZAZA,EFN,EGN,V,CG(30),GAM(30)PEL00010
COMMON/BESSEL/FL(15),PC(15),OF(15,15),M1,M2,B(15)                                PEL00020
COMMON/DFUNC/F(30),G(30),DF(30),DG(30),DFK(200),DFKP(200),CF(30),HPEL00030
COMMON /FAC/FACT(67),RTFAC(95),ROOT(50)                                         PEL00040
COMMON/FIDO/FI(30,15),U(30),JMP,NAME,SMELL,QV,EB,IZ                               PEL00050
COMMON /KUT/RK1(4),RK2(4),RK3(4),RK4(4),K4(4)                                     PEL00060
COMMON /LIMIT/JM,LM,KM,K2M,IEND,NEW,NKP,JKB,LMKB,NTAB                            PEL00070
COMMON/MAT/SF(30),SG(30),FK(200),FKP(200),SFK(200),SFKP(200),RCUT PEL00080
COMMON/QUANT/LK(30),LMK(30),JK(30),FKAP(30),SN(30),SI(30),CR(30) PEL00090
COMMON /ONWARD/HX,SCX,GBX,FBX                                              PEL00100
COMMON /TAPES/X(1500),SCF(1500),FB(1500),GB(1500),GAMB,SCREEN                  PEL00110
COMMON/TRANS/MF(30,15),HFM(30,15),JNG(30),JPS(30)                                PEL00120
COMMON/VECT/KF(200),KG(200),LBES(200),LBS(200),LKB                           PEL00130
DIMENSION XN(36),XL(36),XJ(36),ERG(36),XZ(36)                                 PEL00140
FL(1) = 1.0                                         PEL00150
PC(1) = 1.0                                         PEL00160
DO 5 L=2,15                                         PEL00170
FL(L) = 2*L-1                                      PEL00180
PC(L) = PC(L-1)/FL(L)                         PEL00190
DO 5 J=1,15                                         PEL00200
FLJ = J*(2*(L+J)-1)                         PEL00210
5 OF(L,J) = 1.0/FLJ                         PEL00220
R001(1) = 1.0                                         PEL00230
DO 10 I=2,50                                         PEL00240
FAT = I                                         PEL00250
10 R001(I) = SQRT(FAT)                         PEL00260
FACT(1) = 1.0                                         PEL00270
FACT(3) = 1.0                                         PEL00280
RTFAC(1) = 1.0                                         PEL00290
RTFAC(3) = 1.0                                         PEL00300
FAT = 1.0                                         PEL00310
DO 15 I=2,33                                         PEL00320
F1 = 1                                         PEL00330
FAT = FAT*F1                                         PEL00340
FACT(2*I+1) = FAT                         PEL00350
15 RTFAC(2*I+1) = SQRT(FAT)                   PEL00360
FAT = 1.0                                         PEL00370
DO 20 I=34,47                                         PEL00380
F1 = 1                                         PEL00390
FAT = FAT*F1                                         PEL00400
20 RTFAC(2*I+1) = SQRT(FAT)*RTFAC(67)          PEL00410
SQ2 = 1.0 / ROOT(2)                         PEL00420
RK1 (1) = 0.5                                         PEL00430
RK1 (2) = 1.0-SQ2                         PEL00440
RK1 (3) = 1.0+SQ2                         PEL00450
RK1 (4) = 1.0/6.0                         PEL00460
RK2 (1) = 2.0                                         PEL00470
RK2 (2) = 1.0                                         PEL00480
RK2 (3) = 1.0                                         PEL00490
RK2 (4) = 2.0                                         PEL00500
RK3 (1) = 0.5                                         PEL00510
RK3 (2) = 1.0-SQ2                         PEL00520
RK3 (3) = 1.0+SQ2                         PEL00530
RK3 (4) = 0.5                                         PEL00540
RK4 (1) = 0.5                                         PEL00550
RK4 (2) = 0.0                                         PEL00560
RK4 (3) = 0.5                                         PEL00570
RK4 (4) = 0.0                                         PEL00580
K4(1) = 1                                         PEL00590

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K4(2) = 0 PEL00600
K4(3) = 1 PEL00610
K4(4) = 0 PEL00620
CCM = 511.0062 PEL00630
ALFA = 1.0/157.0367 PEL00640
REL = 0.281777 PEL00650
PI = 3.14159265 PEL00660
FOURPI = 4.0*PI PEL00670
HALFPI = 0.5 * PI PEL00680
RAU = PI / 180.0 PEL00690
FIB = 0.250*PI*REL*REL/ALFA PEL00700
22 READ (5,25) JM,KMAX,LM,NTAPE,NEDGE,IA,IB,IZ,LOOP,QV,SAVE PEL00710
25 FORMAT (9I5,2E15.8) PEL00720
C ORIGINALLY, IA = 0, IB = 0, SAVE = 0. PEL00730
C IB .NE. 0 CUTS OFF CALCULATION AFTER IB SHELLS PEL00740
C IA .GT. 0 RESTARTS AFTER IA SHELLS PEL00750
C SAVE IS THEN CROSS SECTION OF FIRST IA SHELLS READ BACK IN PEL00760
C QV ENTERED IN X.E.V., SAVE ENTERED IN BARNS PEL00770
C LOOP = 0 ORIGINALLY, LOOP = 1 FOR LM REDUCTION PEL00780
C NEDGE NEGATIVE TERMINATES PROGRAM PEL00790
C IF (NEDGE.LT.0) CALL EXIT PEL00800
C WRITE (6,27) PEL00810
27 FORMAT (1H1//2X,4UHINPUT DATA FOR PHOTOELECTRIC CALCULATION //2X,PEL00820
116HINPUT CARD READS//2X,38HJM KMAX LM NTAPE NEDGE IA IB IZ,PEL00830
20H LOOP,/X,2H0V,1UX,4HSAVE //) PEL00840
WRITE (6,25) JM,KMAX,LM,NTAPE,NEDGE,IA,IB,IZ,LOOP,QV,SAVE PEL00850
C DATA CHECKING PEL00860
IF (MINU(JM,KMAX,LM,IA,IB).GE.0) GO TO 29 PEL00870
28 WRITE (6,102) PEL00880
102 FORMAT (5X,15HINCORRECT INPUT //) PEL00890
GO TO 22 PEL00900
29 IF ((IZ.LT.2).OR.(IZ.GT.102)) GO TO 36 PEL00910
IF (QV.LE.0.0) GO TO 28 PEL00920
IF ((LOOP.NE.0).AND.(LOOP.NE.1)) GO TO 28 PEL00930
IF (JM.LE.24) GO TO 111 PEL00940
JM=24 PEL00950
WRITE (6,109) JM PEL00960
109 FORMAT (/5X56HIN ORDER NOT TO EXCEED DIMENSION JM HAS BEEN REDUCEDPEL00970
1 TO 13/) PEL00980
111 IF (KMAX.LE.12) GO TO 112 PEL00990
KMAX=12 PEL01000
WRITE (6,113) KMAX PEL01010
113 FORMAT (/5X58HIN ORDER NOT TO EXCEED DIMENSION KMAX HAS BEEN REDUCPEL01020
1 ED TO 13/) PEL01030
112 IF (LM.LE.12) GO TO 116 PEL01040
LM=12 PEL01050
WRITE (6,114) LM PEL01060
114 FORMAT (/5X56HIN ORDER NOT TO EXCEED DIMENSION LM HAS BEEN REDUCEDPEL01070
1 TO 13/) PEL01080
116 Z = IZ PEL01090
ZA = Z*ALFA PEL01100
ZAZA = ZA*ZA PEL01110
WRITE (6,50) IZ,QV,KMAX,LM,JM PEL01120
50 FORMAT (1H1//5X40HINPUT DATA FOR PHOTOELECTRIC CALCULATION // PEL01130
114X, 14,17H = NUCLEAR CHARGE /9X,F9.3,16H = PHOTON ENERGY // PEL01140
215X13,25H = MAX KAPPA FOR ELECTRON /15X13,19H = MAX L FOR PHOTON /PEL01150
315X13,26H = MAX J (LEGENDRE COEFF.) //) PEL01160
REWIND NTAPE PEL01170
READ (NTAPE) NGRID,ISIXF,I,IONL,RSIXFI,RONE,(X(I),I=1,NGRID) PEL01180
55 READ (NTAPE) ZTRY,JX,NAME,SCREEN,(XN(I),XL(I),XJ(I),XZ(I),ERG(I), PEL01190
I1=1,JX) PEL01200
121 = ZTRY + 0.01 PEL01210

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IF ( IZ .EQ. IZT ) GO TO 40
READ (NTAPE) (SCF(I),I=1,NGRID)
C SKIPS LOGICAL RECORDS CONTAINING POTENTIAL
DO 99 ISKIP=1,JX
 99 READ (NTAPE) RCUT,KJI,( GB(I),I=1,KJI ), ( FB(I), I=1,KJI )
C SKIPS UNWANTED LOGICAL RECORDS TO NEXT ELEMENT
IF ( IZT .LE. 102 ) GO TO 35
36 WRITE (6,30) IZ
30 FORMAT (//3UX19HNUCLEAR CHARGE Z = I3,1X18HNOT FOUND ON TAPE.)
GO TO 22
40 WRITE (6,45)
45 FORMAT (////2UX,25HTAPE POSITIONED PROPERLY.////)
IF (NEDGE.GT.JX) GO TO 28
IF ((IA.GE.JX).OR.(IB.GT.JX)) GO TO 28
READ (NTAPE) (SCF(I),I=1,NGRID)
IF ( NEDGE .EQ. 0 ) GO TO 93
Q = ERG(NEDGE)
QV = Q * CLM
GO TO 94
93 Q = QV / CLM
94 WRITE (6,1/3) NAME,IZ,JX,SCREEN,IONE,RONE,ISIXFI,RSIXFI,NGRID,
 1X(NGRID)
1/3 FORMAT (//25XA6,1X4H= ELEMENT/28XI3,1X15H= ATOMIC NUMBER/
129XI2,1X27H= NUMBER OF ELECTRON SHELLS/
216XI5.8,1X46H= SCREENING FACTOR OF OUTERMOST BOUND ELECTRON/
528XI3,1X24H= RADIAL GRID UP TO X = F4.1/
427XI4,1X24H= RADIAL GRID UP TO X = F5.1/
527XI4,1X14H= TOTAL RADIAL GRID /16XE15.8,1X24H= OUTERMOST RADIAL VPEL01490
5ALUE //)
SECI = SAVE
IF ( IB .EQ. 0 ) IB = JX
DO 60 I = 1, IB
 60 READ (NTAPE) RCUT,KJI, (GB(L),L=1,KJI), (FB(L),L=1,KJI)
IF (I.LE.IA) GO TO 60
IF (Q.GE.ERG(I)) GO TO 90
WRITE (6,95) XN(I)
95 FORMAT (/5X,18HENERGY FALLS BELOW,1XA6,1X4HEDGE//)
GO TO 60
90 IF ( Q .EQ. ERG(I) ) NEDGE = I
 90 WRITE (6,80) XN(I),RCUT,KJI
98 FORMAT (1H1/25XA6,1X7H= SHELL/16XE15.8,1X21H= INTEGRATION CUT-OFF/
127XI4,1X3/H= NUMBER OF WAVE FUNCTION GRID POINTS /)
FST = FB*XL(1)/Q
LK8 = XL(1) + 0.01
JK8 = 2.0*XJ(1) + 0.01
LMK8 = JK8-LK8
FK8 = XJ(1)+0.5
GAM8 = SQRT(FK8**2-ZA*ZA)
KB = FK8 + 0.01
KM = MAXU ( KB+1, KMAX )
KM = MINU ( KM, KB+LM )
IF (KM.EQ.KMAX) GO TO 186
WRITE (6,18/) KM
18/ FORMAT (28XI3,27H = MAX KAPPA FOR THIS SHELL )
186 K2M = 2 * KM
JMP = MINU ( JM+1,K2M )
EFN=Q-ERG(I)
EB=ERG(I)*CLM
SHELL=XN(I)
CALL SINDEX
IF ((NK.LE.200).AND.(NKP.LE.200)) GO TO 83
WRITE (6,100) NK,NKP

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PEL01220
 PEL01230
 PEL01240
 PEL01250
 PEL01260
 PEL01270
 PEL01280
 PEL01290
 PEL01300
 PEL01310
 PEL01320
 PEL01330
 PEL01340
 PEL01350
 PEL01360
 PEL01370
 PEL01380
 PEL01390
 PEL01400
 PEL01410
 PEL01420
 PEL01430
 PEL01440
 PEL01450
 PEL01460
 PEL01470
 PEL01480
 PEL01490
 PEL01500
 PEL01510
 PEL01520
 PEL01530
 PEL01540
 PEL01550
 PEL01560
 PEL01570
 PEL01580
 PEL01590
 PEL01600
 PEL01610
 PEL01620
 PEL01630
 PEL01640
 PEL01650
 PEL01660
 PEL01670
 PEL01680
 PEL01690
 PEL01700
 PEL01710
 PEL01720
 PEL01730
 PEL01740
 PEL01750
 PEL01760
 PEL01770
 PEL01780
 PEL01790
 PEL01800
 PEL01810
 PEL01820
 PEL01830

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1UU FORMAT (5X34HMATRIX ELEMENT DIMENSIONS EXCEEDED,14X5HJK = I4,
16HNKP = I4//30X12HCASE DROPPED //)
   GO TO 22
85 NTOT=NK+NKP
   WRITE (6,1101) NTOT
1101 FORMAT (27X,I4*4H = NUMBER OF MATRIX ELEMENTS FOR THIS SHELL //) PEL01840
   CALL RADINT
85 CALL LEGENDU
   DO 86 J=1,JMP
86 U(J)=FST*U(J)
   WRITE (6,2) JM, KM, LM
2 FORMAT(1H1//15X,I3*26H = MAX J (LEGENDRE COEFF.)/ 15X,I3*25H = MAX KAPP
A FOR ELECTRON/15XI3,19H = MAX L FOR PHOTON/) PEL01850
   1      1 25H = MAX KAPPA FOR ELECTRON/15XI3,19H = MAX L FOR PHOTON/) PEL01860
   CALL ANGLE
   IF (ILOOP.LT.2)      GO TO 88
   WRITE (6,62) LM
62 FORMAT (1///50X23H LOOP REDUCTION TO LM = I2) PEL01870
87 IF (LM.EQ.1)      GO TO 63
   LM = LM-1
   IF (KM.LE.(KB+LM))      GO TO 61
   KM = KB+LM
   K2M = 2*KM
   JMP = MINU ( JMP, K2M )
   JM = JMP - 1
61 CALL HUM
   GO TO 85
88 IF (1.EQ.NEDGE)      SEDGE = FOURPI*D(1)
   SECT = SECT+FOURPI*D(1)
   IF (ILOOP.EQ.0)      GO TO 60
   LOOP = 2
   LMS = LM
   JMS = JM
   JPS = JMP
   GO TO 87
63 LOOP = 1
   LM = LMS
   JM = JMS
   JMP = JPS
60 CONTINUE
   WRITE(6,200) NAME, IC, QV, SECT
200 FORMAT(1H1///30X,7HELEMENT,27X,13HATOMIC NUMBER//32X,A6,31X,I3//) PEL02100
   1 30X,17HPHOTON ENERGY = ,F12.7*5H KEV //// 40X, PEL02105
   2 22HTOTAL CROSS SECTION = ,E15.8,7H BARNS //// ) PEL02110
   1F (NEDGE.EQ.0)      GO TO 22
C   1F AT EDGE, CROSS SECTION BELOW EDGE PEL02120
   SECT = SECT-SEdge
   WRITE (6,75) SECT PEL02130
75 FORMAT (/40X27HCROSS SECTION BELOW EDGE = E15.8,6H BARNS/) PEL02140
   GO TO 22
   END PEL02150

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SUBROUTINE ANGLE

Purpose: This routine computes the angular distribution from the Legendre coefficients of the cross section and a calculation of the Legendre polynomials, and outputs the differential cross-section at two degree intervals.

Method: Legendre polynomials are computed at two degree intervals, then multiplied by the Legendre coefficients of the cross section and finally summed.

Subroutine called: None

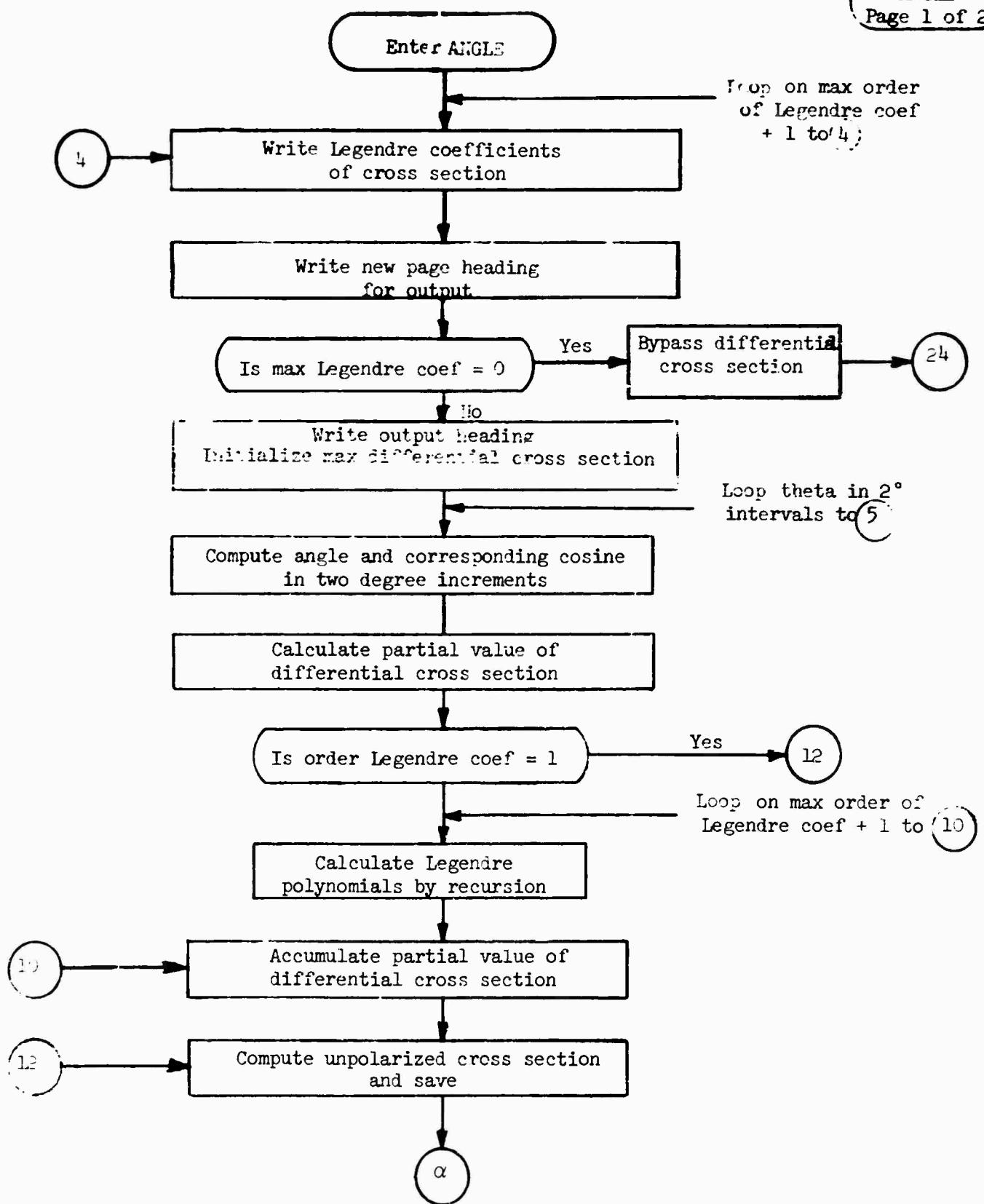
Subroutine called by: PELEC

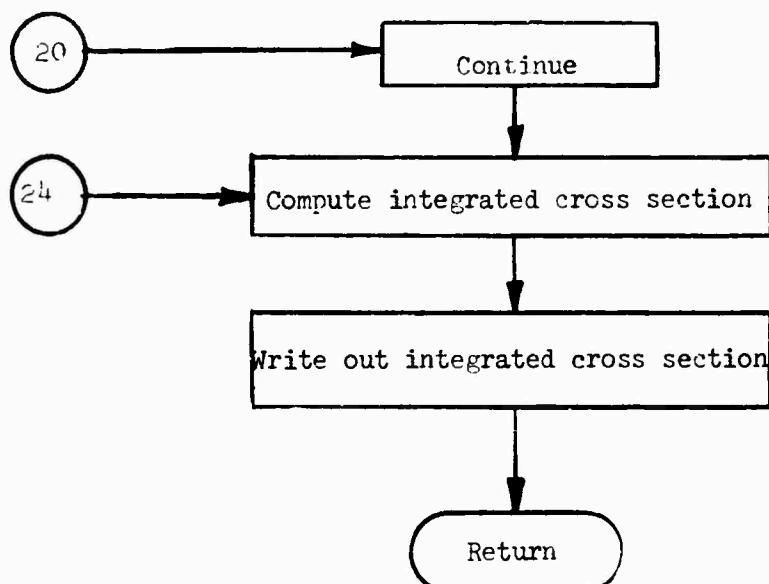
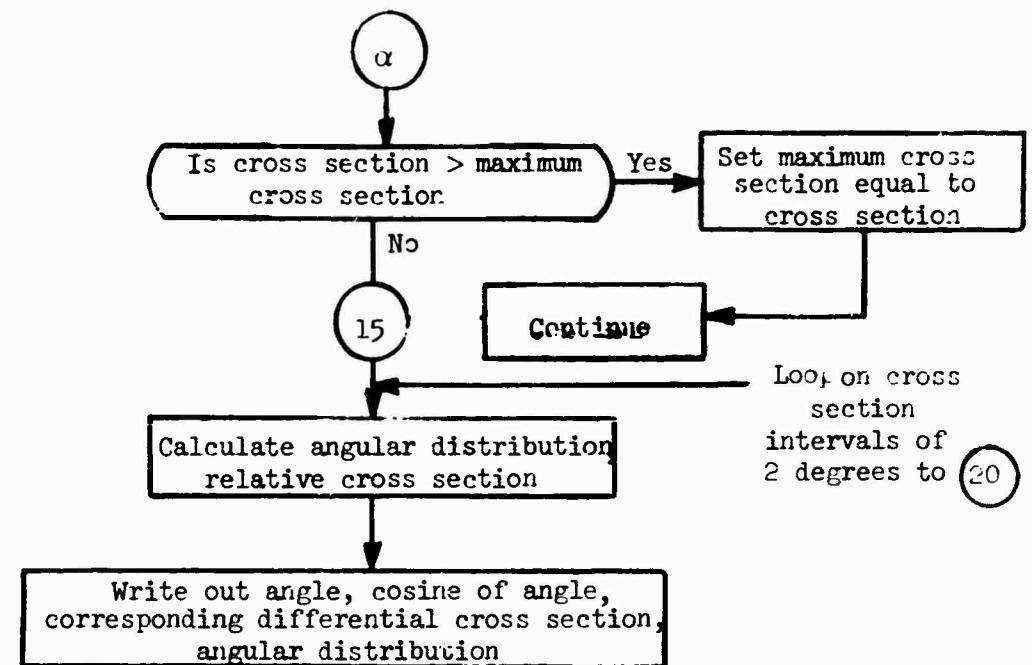
Variables in unlabelled Common: PI, HALFPI, FOURPI, RAD, SQ2, Q, ZA, ZAZA,
EFN, V, CG, GAM

Labelled Common: FID \emptyset

Local Variables:

Name	Dimension	Mode	Meaning
JL		I	Order of Legendre coefficient
EL		R	Electron kinetic energy in keV
SMAX		R	Maximum differential cross section
KMUQ		I	Indexing variable
ITHETA		I	Angle (in degrees) between photon and electron
IT	91	I	Stores angle values
FMUQ		R	Cosine of angle
SIP		R	Unpolarized cross section (in barns/steradian)
PPL		R	Legendre polynomial
SP	91	R	Stored values of unpolarized cross section
AD	91	R	Angular distribution
XFC		R	Integrated cross section (in barns)
QMU	91	R	Stored values of cosine of angle





S18F1C ANGL

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SUBROUTINE ANGLE                                         ANG00010
COMMON PI,HALFPI,FOURPI,RAD,SQ2,Q,ZA,ZAZA,EFN,EGN,V,CG(30),GAM(30) ANG00020
COMMON/FI00/F1(30,15),D(30),JMP,NAME,SHELL,QV,EB,I2          ANG00030
DIMENSION IT(91), QMU(91), SP(91), AD(91)                  ANG00040
      WRITE (6,2)
2 FORMAT(//10X,38HLEGENDRE COEFFICIENTS OF CROSS SECTION//    ANG00050
1      6X,1HJ,10X,4HD(J) // )                                ANG00060
DO 4 J = 1, JMP                                         ANG00070
  JL = J - 1                                           ANG00080
  WRITE (6,3) JL, D(J)                                 ANG00090
3 FORMAT( 17,5X, E15.8 )                                ANG00100
4 CONTINUE                                              ANG00120
  EL = QV - EB                                         ANG00130
  WRITE (6,5) NAME, IZ, SHELL, EB, QV, EL               ANG00140
5 FORMAT( 1H1///,33X,7HELEMENT,7X,13HATOMIC NUMBER, 13X,5HSHELL// ANG00150
1      35X,A6,11X,13,17X,A6///16X,14HBINDING ENERGY,17X,     ANG00160
2      15HPHOTON ENERGY,11X,23HELECTRON KINETIC ENERGY//      ANG00170
3      3(14X,F12.7,4H KEV) // )                          ANG00180
  IF ( JMP .EQ. 1 )           GO TO 24                 ANG00190
  WRITE (6,8)
8 FORMAT(25X,4SHUNPOLARIZED CROSS SECTION (BARNs/STERADIAn) // ANG00210
1      16X,5HTHETA,15X,9HCOS THETA,18X,13HCROSS SECTION, 16X, ANG00220
2      1UHANG. DIST. // )                                ANG00230
  SMAX = 0.0                                         ANG00240
  DO 15 KMUQ = 1, 91                                  ANG00250
    ITTHETA = 2 * ( KMUQ - 1 )                         ANG00260
    IT(KMUQ) = ITTHETA                               ANG00270
    THE=RAD*FLUAT (ITTHETA)                           ANG00280
    FMUG=COS (THE)                                 ANG00290
    QMU(KMUQ) = FMUG                                ANG00300
    PMI=1.0                                         ANG00310
    PN=FMUG                                         ANG00320
    SIP = D(1) + FMUG * D(2)                         ANG00330
    IF (JMP.EQ.2)           GO TO 12                 ANG00340
    DO 10 J=3,JMP                                     ANG00350
    FN=J-2                                         ANG00360
    PPL = ( PN*FMUG*(2.0*FN+1.0) - PMI*FN ) / ( FN+1.0 ) ANG00370
    PMI=PN                                         ANG00380
    PN=PPL                                         ANG00390
10   SIP = SIP + PPL * D(J)                         ANG00400
12   SF(KMUQ) = SIP                                ANG00410
    IF ( SF(KMUQ) .GT. SMAX )           SMAX = SP(KMUQ) ANG00420
15   CONTINUE                                         ANG00430
    DO 20 KMUQ = 1, 91                 ANG00440
    AD(KMUQ) = SP(KMUQ) / SMAX                      ANG00450
    WRITE ( 6,18) IT(KMUQ), QMU(KMUQ), SP(KMUQ), AD(KMUQ) ANG00460
18   FORMAT( 15X,15,15X,F10.7,17X ,E15.8 , 15X, F10.7 ) ANG00470
20   CONTINUE                                         ANG00480
24   XSEC = FOURPI * D(1)                           ANG00490
    WRITE (6,25) XSEC                                ANG00500
25   FORMAT( //1//3UX27HINTEGRATED CROSS SECTION = E15.8, 6H BARNs //) ANG00510
    RETURN                                         ANG00520
    END                                             ANG00530

```

SUBROUTINE CGEFS

Purpose: Computes Clebsch-Gordan coefficients.

Method: For computer computation economy, the requisite square roots of integers, factorials and square roots of factorials are stored in common. The routine uses explicit algebraic expressions for Clebsch-Gordan coefficients whose smallest angular momentum value is two or less (with appropriate permutation of indices). Otherwise the general formula is used, with a specialization for the parity Clebsch-Gordan coefficients. The input variables are double the angular momenta quantities, in order to use them in integer mode.

Subroutine called: None

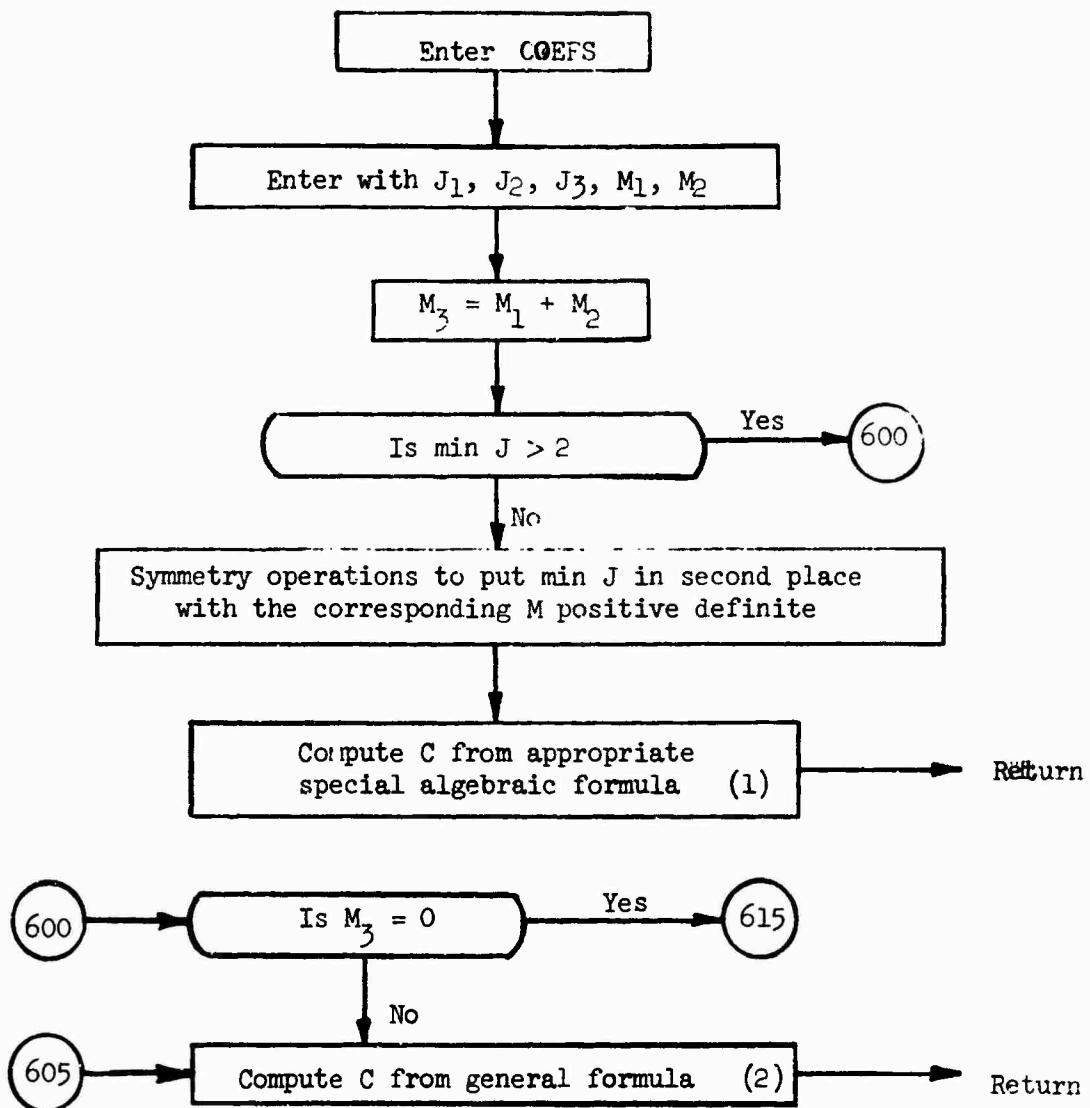
Subroutine called by: FILL, HUM, MUSS

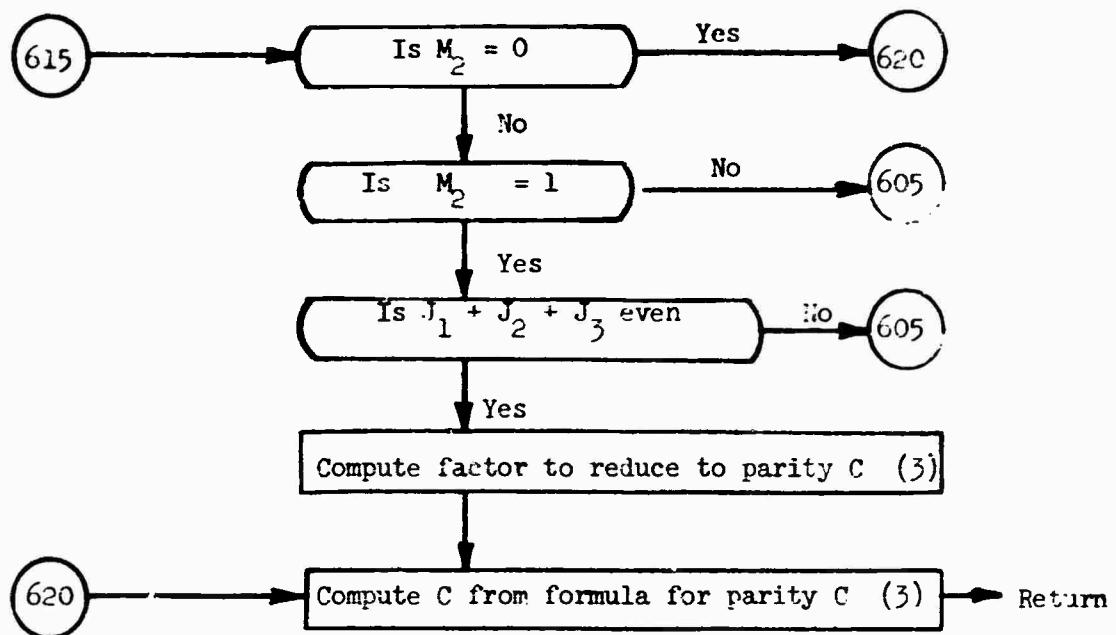
Labelled Common: FAC

Argument sequence: (J1, J2, J3, M1, M2, C)

Argument List:

Name	Dimension	Mode	Meaning
J1, J2, J3		I	Angular momenta
M1, M2		I	Magnetic quantum numbers
C		R	Clebsch-Gordan coefficient





References:

- (1) E. V. Condon and G. H. Shortley, Theory of Atomic Spectra, (Cambridge University Press, 1935).
- (2) G. Racah, Phys. Rev. 62, 438 (1942).
- (3) L. C. Biedenharn and M. E. Rose, Rev. Mod. Phys. 25, 729 (1953).

SUBROUTINE COEFS

```

SUBROUTINE COEFS ( J1,J2,J3,M1,M2,C )
COMMON /FAC/F(67),RT(45),R(50)
M3 = M1 + M2
C = 0.0
SIGM = 1.0
JMIN = MINU (J1,J2,J3)
IF ( JMIN .GT. 4 )      GO TO 600
IF ( JMIN .EQ. J2 )      GO TO 220
IF ( JMIN .EQ. J3 )      GO TO 230
210 L1 = J2
L2 = J1
L3 = J3
LM1 = -M2
LM2 = -M1
LM3 = -M3
GO TO 240
220 L1 = J1
L2 = J2
L3 = J3
LM1 = M1
LM2 = M2
LM3 = M3
GO TO 240
230 L1 = J1
L2 = J3
L3 = J2
LM1 = M1
LM2 = -M3
LM3 = -M2
SIGM = R(L2+1)/R(L3+1)
IF ( MOD ( J1 - M1 , 4 ) .NE. 0 )      SIGM = - SIGM
240 IF ( LM2 ) 245, 250, 250
245 LM1 = - LM1
LM2 = - LM2
LM3 = - LM3
IF ( MOD ( L1 + L2 - L3 , 4 ) .NE. 0 )      SIGM = - SIGM
250 JMIN = JMIN+1
K = L1+LM3
L = L1-LM3
GO TO (255,260,300,700,400), JMIN
255 IF (L1-L3) 800,256,800
256 IF (LM1-LM3) 800,257,800
257 C = SIGM
GO TO 800
260 IF (L3-L1-LM2) 265,280,270
265 SIGM = -SIGM
270 K = L
280 KP1 = K + 1
C = R(KP1)/R(2*L1+2)
290 C = SIGM*C
GO TO 800
300 IF (L3-L1) 305,310,315
305 IF (LM2) 800,325,330
310 IF (LM2) 800,340,345
315 IF (LM2) 800,355,360
320 C = -R(L)*R(K)/(R(2*L1)*R(L1+1))
GO TO 380
330 C = R(L)*R(L+2)/(2.0*R(L1)*R(L1+1))
GO TO 380
340 C = FLOAT(LM3)/(R(L1)*R(L1+2))
GO TO 380

```

COF00010
COF00920
COF00030
COF00040
COF00050
COF00060
COF00070
COF00080
COF00090
COF00100
COF00110
COF00120
COF00130
COF00140
COF00150
COF00160
COF00170
COF00180
COF00190
COF00200
COF00210
COF00220
COF00230
COF00240
COF00250
COF00260
COF00270
COF00280
COF00290
COF00300
COF00310
COF00320
COF00330
COF00340
COF00350
COF00360
COF00370
COF00380
COF00390
COF00400
COF00410
COF00420
COF00430
COF00440
COF00450
COF00460
COF00470
COF00480
COF00490
COF00500
COF00510
COF00520
COF00530
COF00540
COF00550
COF00560
COF00570
COF00580
COF00590
COF00600
COF00610

345 LOX = L+2 COF00620
 C = -R(K)*R(LOX)/(R(2*L1)*R(L1+2)) COF00630
 GO TO 380 COF00640
 355 LOX = L+2 COF00650
 LAX = K+2 COF00660
 C = R(LOX)*R(LAX)/(R(2*L1+2)*R(L1+2)) COF00670
 GO TO 380 COF00680
 360 C = R(K)*R(K+2)/(2.0*R(L1+1)*R(L1+2)) COF00690
 380 C = SIGM*C COF00700
 GO TO 800 COF00710
 400 M = LM2/2+1 COF00720
 J = (L3-L1)/2 +3 COF00730
 GO TO (480,510,540), M COF00740
 480 GO TO (485,490,495,500,505), J COF00750
 485 C = R(3)*R(L)*R(L-2)*R(K)*R(K-2)/(R(8)*R(L1-2)*R(L1-1)*R(L1) COF00760
 *R(L1+1)) COF00770
 GO TO 575 COF00780
 490 C = -0.5*FLOAT(LM3)*R(6)*R(L)*R(K)/(R(L1)*R(L1-2)*R(L1+1)*R(L1+2)) COF00790
 GO TO 575 COF00800
 495 C = 0.5*FLOAT(3*LM3*LM3-L1*(L1+2)) COF00810
 1 / (R(L1)*R(L1-1)*R(L1+2)*R(L1+3)) COF00820
 GO TO 575 COF00830
 500 LOX = L+2 COF00840
 LAX = K+2 COF00850
 C = 0.5*FLOAT(LM3) COF00860
 1 *R(6)*R(LOX)*R(LAX)/(R(L1)*R(L1+1)*R(L1+2)*R(L1+4)) COF00870
 GO TO 575 COF00880
 505 LOX = L+4 COF00890
 LAX = L+2 COF00900
 LLX = K+4 COF00910
 LXX = K+2 COF00920
 C = R(3)*R(LOX)*R(LAX)*R(LLX)*R(LXX)/(R(8)*R(L1+1)*R(L1+2)*R(L1+3)) COF00930
 1*R(L1+4)) COF00940
 GO TO 575 COF00950
 510 GO TO (515,520,525,530,535), J COF00960
 515 C = -R(L+2)*R(L)*R(L-2)*R(K-2)/(2.0*R(L1-2)*R(L1-1)*R(L1)*R(L1+1)) COF00970
 GO TO 575 COF00980
 520 C = 0.5*FLOAT(L1+2*LM3-2) COF00990
 1 *R(L+2)*R(L)/(R(L1)*R(L1-2)*R(L1+1)*R(L1+2)) COF01000
 GO TO 575 COF01010
 525 LOX = L+2 COF01020
 C = (1.0-FLOAT(LM3))*R(3)*R(LOX)*R(K)/(R(2*L1)*R(L1-1)*R(L1+2)) COF01030
 1*R(L1+3)) COF01040
 GO TO 575 COF01050
 530 C = 0.5*FLOAT(2*LM3-L1-4) COF01060
 1 *R(K+2)*R(K)/(R(L1)*R(L1+1)*R(L1+2)*R(L1+4)) COF01070
 GO TO 575 COF01080
 535 LOX = L+4 COF01090
 C=R(LOX)*R(K+4)*R(K+2)*R(K)/(2.0*R(L1+1)*R(L1+2)*R(L1+3)*R(L1+4)) COF01100
 GO TO 575 COF01110
 540 GO TO (545,550,555,560,565), J COF01120
 545 C = R(L-2)*R(L)*R(L+2)*R(L+4)/(4.0*R(L1)*R(L1-2)*R(L1-1)*R(L1+1)) COF01130
 GO TO 575 COF01140
 550 C = -R(K-2)*R(L)*R(L+2)*R(L+4)/(2.0*R(L1)*R(L1-2)*R(L1+2)*R(L1+1)) COF01150
 GO TO 575 COF01160
 555 LOX = L+2 COF01170
 LAX = L+4 COF01180
 C = R(3)*R(K-2)*R(K)*R(LOX)*R(LAX)/(R(8)*R(L1)*R(L1-1)*R(L1+2)) COF01190
 1*R(L1+3)) COF01200
 GO TO 575 COF01210
 560 LOX = L+4 COF01220
 C = -R(K-2)*R(K)*R(K+2)*R(LOX)/(2.0*R(L1)*R(L1+2)*R(L1+4)*R(L1+1)) COF01230

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      GO TO 575                                COF01240
565 C=R(K-2)*R(K)*R(K+2)*R(K+4)/(4.0*R(L1+1)*R(L1+2)*R(L1+3)*R(L1+4)) COF01250
575 C = SIGM*C                                COF01260
      GO TO 800                                COF01270
700 M = (LM2+1)/2                            COF01280
      J = (LJ-L1+5)/2                            COF01290
      GO TO ( 710, 740 ), M                      COF01300
710 GO TO ( 720, 725, 730, 735 ), J          CGF01310
720 C = R(3)*R(K-1)*R(L-1)*R(L+1)/(R(8)*R(L1)*R(L1-1)*R(L1+1)) COF01320
      GO TO 780                                COF01330
725 C = -FLOAT((L1+3+LM3-1)/2)*R(L+1)/(R(2)*R(L1-1)*R(L1+1)*R(L1+2)) COF01340
      GO TO 780                                COF01350
730 KP1 = K + 1                             COF01360
      C = -FLOAT((3-3*LM3+L1)/2)*R(KP1)/(R(2)*R(L1)*R(L1+1)*R(L1+3)) COF01370
      GO TO 780                                COF01380
735 LOX = L+3                             COF01390
      KP1 = K + 1                             COF01400
      KP3 = K + 3                             COF01410
      C = R(3)*R(KP1)*R(KP3)*R(LOX)/(R(8)*R(L1+1)*R(L1+2)*R(L1+3)) COF01420
      GO TO 780                                COF01430
740 GO TO ( 750, 755, 760, 765 ), J          COF01440
750 C = -R(L-1)*R(L+1)*R(L+3)/(R(8)*R(L1)*R(L1-1)*R(L1+1)) COF01450
      GO TO 780                                COF01460
755 LOX = L+3                             COF01470
      LAX = L+1                             COF01480
      C = R(3)*R(K-1)*R(LAX)*R(LOX)/(R(8)*R(L1-1)*R(L1+1)*R(L1+2)) COF01490
      GO TO 780                                COF01500
760 LOX = L+3                             COF01510
      C = -R(3)*R(K-1)*R(K+1)*R(LOX)/(R(8)*R(L1)*R(L1+1)*R(L1+3)) COF01520
      GO TO 780                                COF01530
765 C = R(K-1)*R(K+1)*R(K+3)/(R(8)*R(L1+1)*R(L1+2)*R(L1+3)) COF01540
780 C = C*SIGM                                COF01550
      GO TO 800                                COF01560
C   THIS IS THE BEGINNING OF COMPUTATION OF C-COEFFICIENT COF01570
C   USING THE GENERAL EXPRESSION. COF01580
600 L1 = J1+J2-J3+1                         COF01590
      L2 = J1-J2+J3+1                         COF01600
      L3 = -J1+J2+J3+1                         COF01610
      L10 = J1+J2+J3+3                         COF01620
      IF ( M3 .EQ. 0 )                         GO TO 615 COF01630
605 L4 = J1+M1+1                           COF01640
      L5 = J1-M1+1                           COF01650
      L6 = J2+M2+1                           COF01660
      L7 = J2-M2+1                           COF01670
      L8 = J3+M3+1                           COF01680
      L9 = J3-M3+1                           COF01690
      ST = RT(L10) / ( RT(L1)*RT(L4)*RT(L5) ) COF01700
      ST = ST / ( RT(L6) * RT(L7) )           COF01710
      ST = ST / ( R(J3+1)*RT(L2)*RT(L3) )     COF01720
      ST = ST / ( RT(L8) * RT(L9) )           COF01730
      N7 = L1-L7                            COF01740
      N4 = L1-L4                            COF01750
      MIN = MAXU (0,N4,N7)                   COF01760
      MAX = MINU (L1,L5,L6)                   COF01770
      IF (MOD(MIN,4).NE.0)      SIGM=-1.0 COF01780
      MIN = MIN+1                           COF01790
      N1 = L1+1                            COF01800
      N5 = L5+1                            COF01810
      N6 = L6+1                            COF01820
      SUM = 0.0                            COF01830
    DO 610 LZ=MIN,MAX+2                   COF01840
      N1L = N1-LZ                           COF01850

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NSL = N5-L6	COF01860	
N6L = N6-L6	COF01870	
N4L = -N4+L6	COF01880	
N7L = -N7+L6	COF01890	
TERM = ST * F(LZ) * F(N1L) * F(NSL) * F(N6L) * F(N4L) * F(N7L)	COF01900	
C = C + SIGM / TERM	COF01910	
610 SIGM = -SIGM	COF01920	
GO TO 800	COF01930	
615 IF (M2 .EQ. 0)	GO TO 620	COF01940
IF (IABS(M2) .NE. 2)	GO TO 605	COF01950
JMOU = MOU ((L10 + 1), 4)	COF01960	
IF (JMOU .NE. 0)	GO TO 605	COF01970
ST = J3 * (J3 + 2) - J1 * (J1 + 2) - J2 * (J2 + 2)	COF01980	
SIGM = 0.5 * SIGM * ST / (R(J1)*R(J1 + 2)*R(J2)*R(J2 + 2))	COF01990	
620 JMOU = MOU ((L1 - 1), 8)	COF02000	
IF (JMOU .NE. 0)	SIGM = - SIGM	COF02010
L4 = (L1 + 1) / 2	COF02020	
L5 = (L2 + 1) / 2	COF02030	
L6 = (L3 + 1) / 2	COF02040	
L7 = (L10 - 1) / 2	COF02050	
C = SIGM * R(J3 + 1) * F(L7) / (F(L4)*F(L5)*F(L6))	COF02060	
C = C * RT(L1) * RT(L2) * RT(L3) / RT(L10)	COF02070	
800 RETURN	COF02080	
END	COF02090	

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SUBROUTINE DERIV

Purpose: Computes for the Runge-Kut a integration the derivatives of the bound state wavefunctions and the integrands of the matrix elements up to one-half Bohr radius.

Method: Calculates the derivative of the radial components from the coupled Dirac radial equations. In evaluating the integrand of the matrix elements the r^Y factor is restored if $r < 1$.

Subroutine called: SPHBES

Subroutine called by: RKUT, RADINT

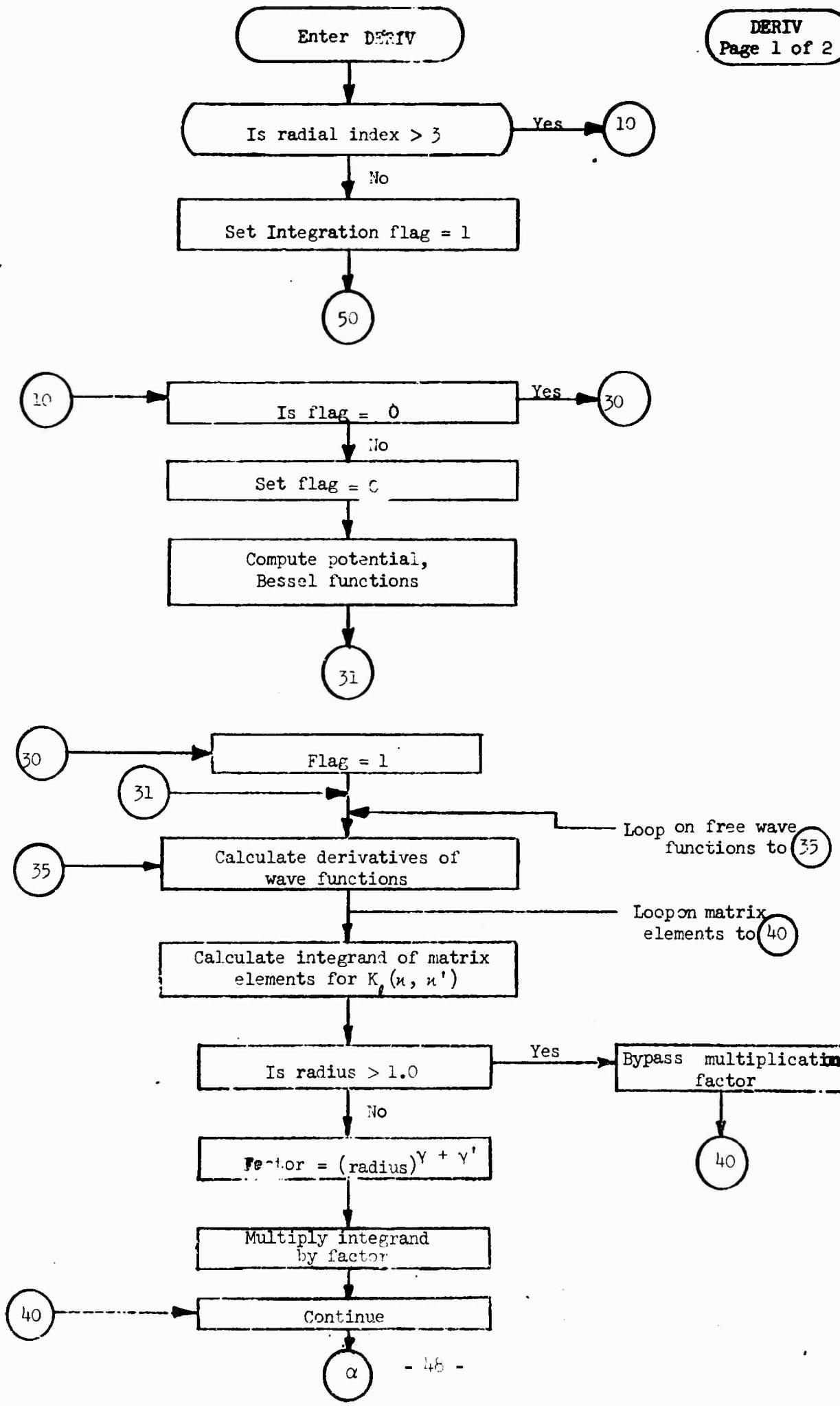
Variables in unlabelled Common: PI, HALFPI, F0URFI, RAD, SQZ, Q, ZA, ZAZA, EFN, EGN, V, CG, GAM

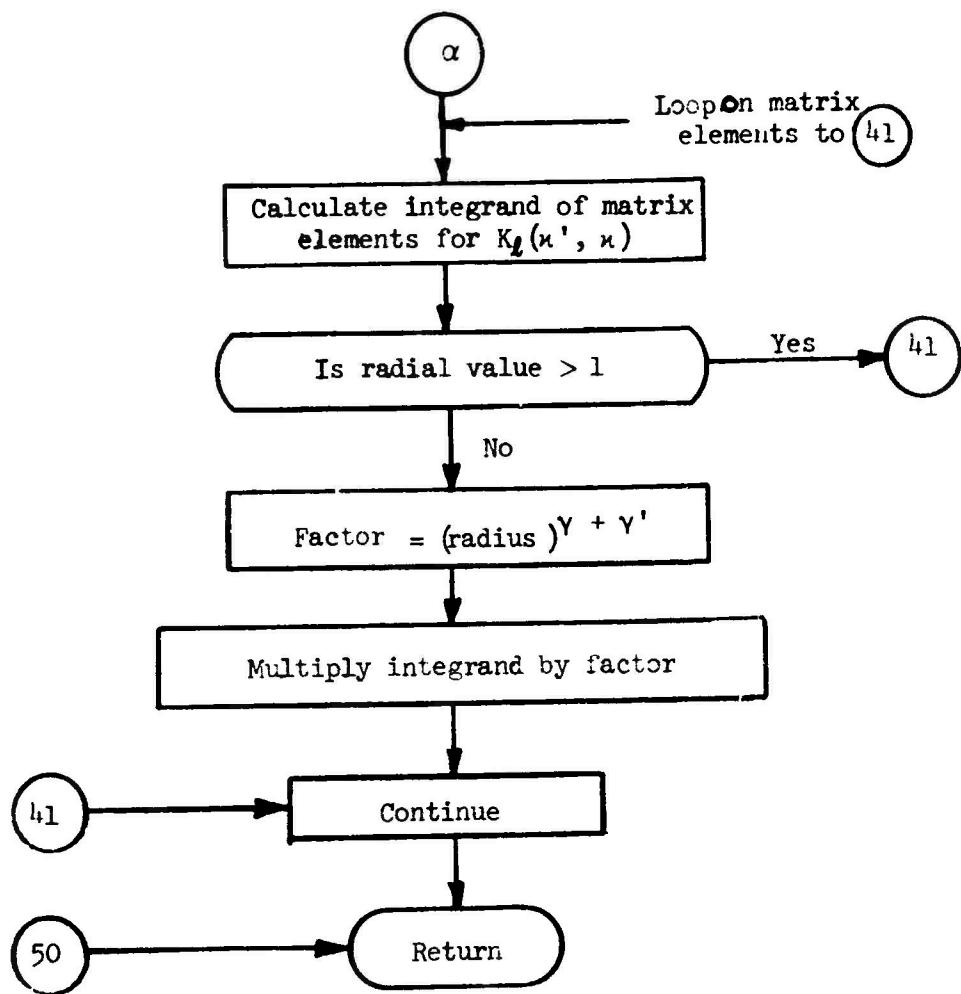
Labelled Common: BESSEL, DEFUNC, LIMIT, TAPES, VECT

Local Variables:

Name	Dimension	Mode	Meaning
Z		R	Photon momentum * radius
N		I	Indexing variable
A		R	Sum of gammas of bound and free state electron

Enter DERIV

DERIV
Page 1 of 2



SUBR DER1
 SUBROUTINE DER1
 COMPUTES DERIVATIVES
 COMMON PI,HALFPI,FOURPI,RAD,SQ2,Q,ZA,ZAZA,EFN,EGN,V,CG(30),GAM(30) DER00010
 COMMON/BESSEL/FL(15),PC(15),OF(15,15),M1,M2,B(15) DER00020
 COMMON/DFUNC/F(30),G(30),DF(30),DG(30),DFK(200),DFKP(200),CF(30),HDER00030
 COMMON /LIMIT/JM,LM,KM,K2M,IEND,NEW,NK,NKP,JKB,LMKB,NTAB DER00040
 COMMON /TAPES/X(1500),SCF(1500),FB(1500),GB(1500),GAMB,SCREEN DER00050
 COMMON/VECT/KF(200),KG(200),LBES(200),LBS(200),LKB DER00060
 IF (NTAB.GE.3) GO TO 10
 NEW = 1 DER00070
 GO TO 50
 10 IF (NEW.EQ.0) GO TO 30 DER00080
 NEW = 0 DER00090
 V=-SCF(NTAB)/X(NTAB)
 Z = Q*X(NTAB) DER00100
 CALL SPHMES (Z)
 GO TO 31 DER00110
 30 NEW = 1 DER00120
 31 DO 35 N=1,K2M DER00130
 DF(N) = CF(N)*F(N)/X(NTAB)-(EFN-V)*G(N) DER00140
 35 DG(N) = CG(N)*G(N)/X(NTAB)+(EGN-V)*F(N) DER00150
 DO 40 N=1,NK DER00160
 I = KG(N)
 L = LBES(N) DER00170
 DFK(N)=B(L)*G(I)*FB(NTAB) DER00180
 IF (X(NTAB).GT.1.0) GO TO 40 DER00190
 A = GAM(I)+GAMB DER00200
 DFK(N) = DFK(N)*(X(NTAB))**A DER00210
 40 CONTINUE DER00220
 DO 41 N=1,NKP DER00230
 I = KF(N)
 L = LBS(N) DER00240
 DFKP(N)=B(L)*F(I)*GB(NTAB) DER00250
 IF (X(NTAB).GT.1.0) GO TO 41 DER00260
 A = GAM(I)+GAMB DER00270
 DFKP(N) = DFKP(N)*(X(NTAB))**A DER00280
 41 CONTINUE DER00290
 50 RETURN DER00300
 END DER00310
 DER00320
 DER00330
 DER00340
 DER00350
 DER00360
 DER00370
 DER00380
 DER00390

SUBROUTINE FILL

Purpose: Computes $\phi(\kappa, \lambda)$

Method: $\phi(\kappa, \lambda)$ is computed in two passes, one for $K_{\ell}(\kappa \kappa')$ contributions the other for $K_{\ell}(\kappa' \kappa)$ and then the two pieces are added in subroutine HUM to yield ϕ . The selection rules are examined for each matrix element contribution to determine what values of $(\lambda - \ell)$ are allowed. If $\lambda = \ell \pm 1$, f can assure only the one value $f = \lambda \mp 1/2$; if $\lambda = \ell$ both the preceding values of f are possible. In the final run-through the remaining selection rules required for R are checked, R is computed from explicit algebraic expressions for the Racah coefficient with $J_5 = 1/2$, the corresponding Clebsch-Gordan coefficient called and $\phi(\kappa, \lambda)$ formed with appropriate ℓ summation. The indices used for ϕ are λ and K (K is a positive integer uniquely related to κ).

Subroutine called: C ϕ EFS

Subroutine called by: HUM

Labelled Common: FAC, LIMIT, QUANT

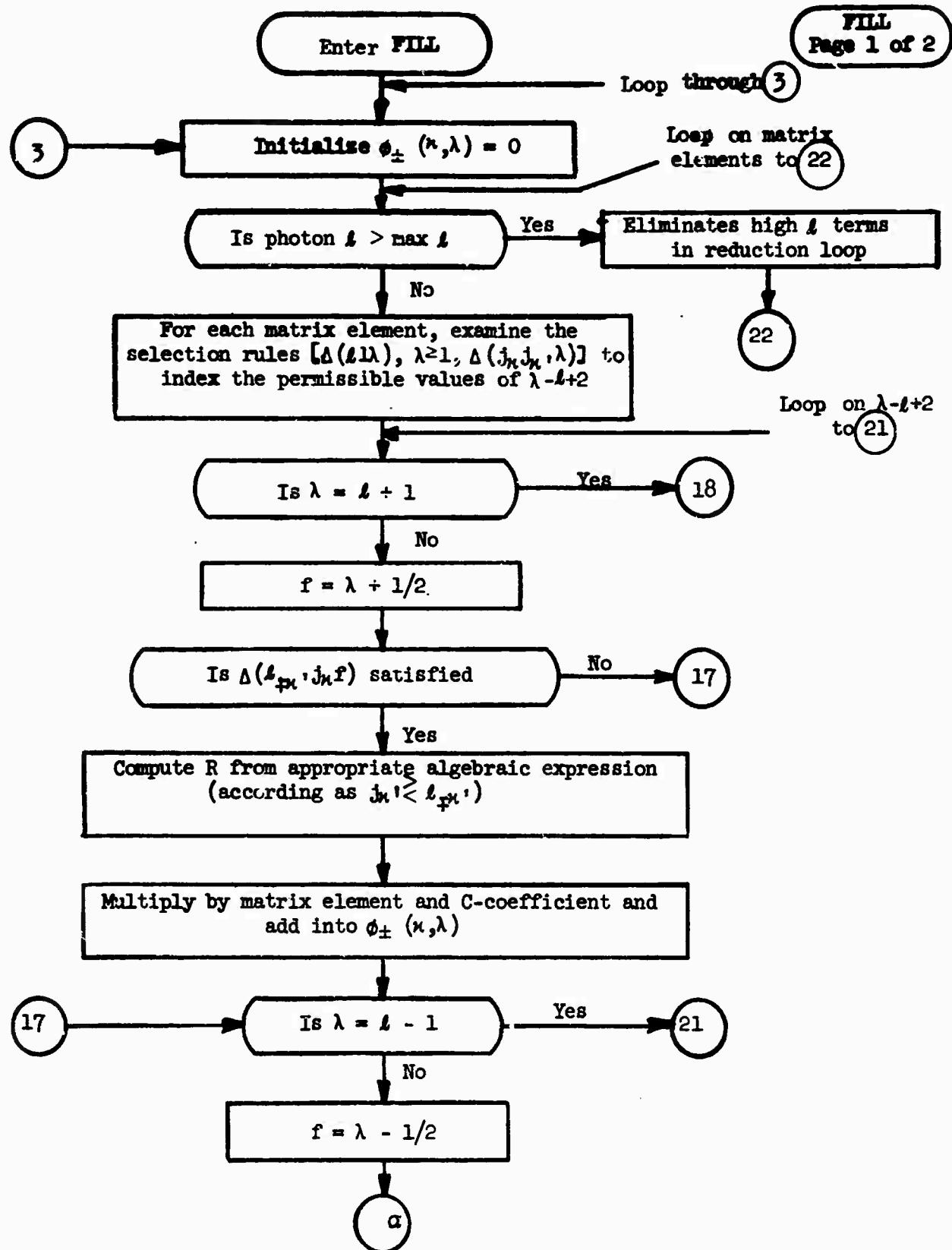
Argument sequence: (TK, KW, LB, NT, LP, FI)

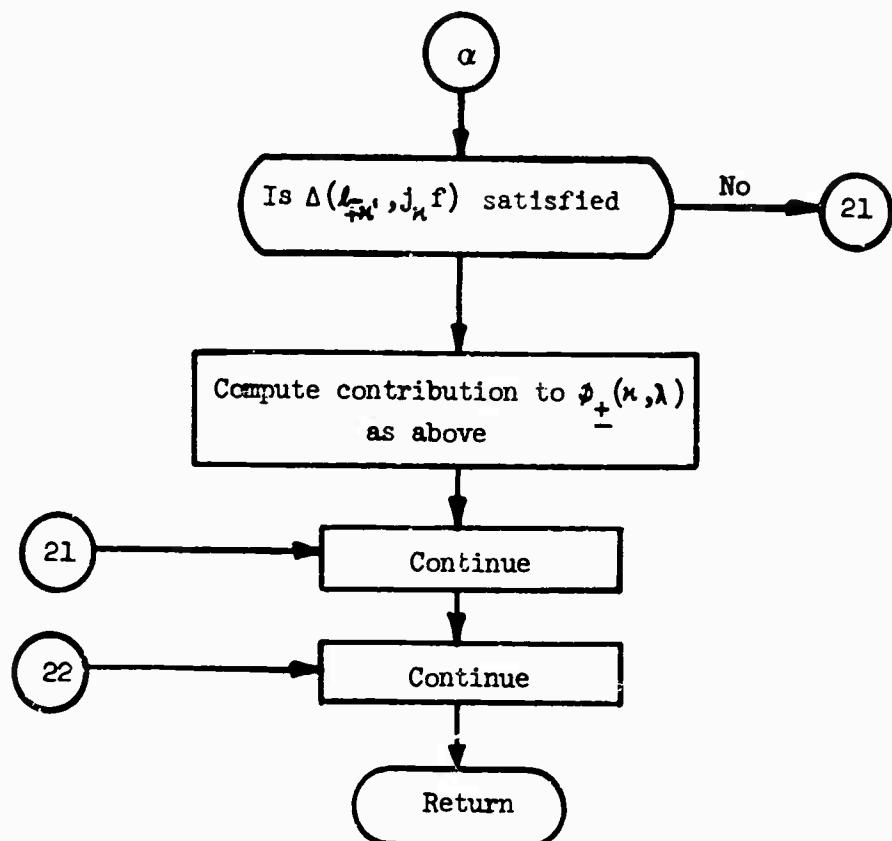
Argument List:

Name	Dimension	Mode	Meaning
TK	200	R	Matrix elements
KW	200	I	Index for κ values in matrix elements
LB	200	I	Photon angular momentum + 1 for matrix elements
NT		I	Number of matrix elements $K_{\ell}(\kappa \kappa')$ or $K_{\ell}(\kappa' \kappa)$
LP		I	$\ell_{-\kappa}$, or ℓ_{κ} ,
FI	30 x 15	R	$\phi_+(\kappa, \lambda)$ or $\phi_-(\kappa, \lambda)$

Local Variables:

Name	Dimension	Mode	Meaning
IMP		I	Max photon angular momentum + 1
LA		I	λ
K		I	Index of free electron state
LD		I	Twice bound electron j_{μ}
N		I	Index of matrix element
L		I	Photon angular momentum
JC		I	Twice free electron j_{μ}
NA, NB		I	Loop index for the range of $(\lambda - \ell)$
LAM		I	$2 * \lambda$
LEF		I	$2 * (\lambda \pm 1/2)$
NL		I	$(\lambda - \ell) + 2$
IR, IS		I	Terms in R
R		R	$R(j_{\mu}, \ell_{\mu}, \lambda f j_{\mu})$
C		R	Clebsch-Gordan coefficient
JPL		I	$2 x j_{\mu} + 2 x j_{\mu} - 2 x$ photon angular momentum
JML		I	$ 2 x j_{\mu}, - 2 x j_{\mu} - 2 x$ photon angular momentum





S1R4C FILE

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SUBROUTINE FILL (TK,KW,LB,NT,LP,FI)          FIL00010
COMMON /FAC/FACT(67),RTFAC(95),ROOT(50)      FIL00020
COMMON /LIMIT/JM,LM,KM,K2M,IEND,NEW,NK,NKP,JKB,LMKB,NTAB   FIL00030
COMMON/QUANT/LK(30),LMK(30),JK(30),FKAP(30),SN(30),SI(30),CR(30) FIL00040
DIMENSION IK(200),KW(200),LB(200),FI(30,15)    FIL00050
LMP=LM+1                                     FIL00060
DO 3 LA=1,LMP                                FIL00070
DO 3 K=1,K2M                                  FIL00080
3 FI(K,LA)=0.0                                 FIL00090
LD=2*LP                                     FIL00100
DO 22 N = 1, NT                               FIL00110
L=LB(N)-1                                    FIL00120
IF (L.GT.LM)        GO TO 22                FIL00130
K=KW(N)                                      FIL00140
JC=JK(K)                                     FIL00150
IF (L.EQ.0)        GO TO 8                 FIL00160
L2=2*L                                     FIL00170
JPL=JKB+JC-L2                                FIL00180
JML=IABS (JKB-JC)-L2                         FIL00190
IF (JPL.LT.2)        GO TO 9                 FIL00200
4 IF (L.EQ.1)        GO TO 6                 FIL00210
IF (JML.GT.(-2))    GO TO 6                 FIL00220
NA=1                                         FIL00230
NB=3                                         FIL00240
GO TO 14                                     FIL00250
6 IF (JML.GT.0)        GO TO 8                 FIL00260
NA=2                                         FIL00270
NB=3                                         FIL00280
GO TO 14                                     FIL00290
8 NA=3                                         FIL00300
NB=3                                         FIL00310
GO TO 14                                     FIL00320
9 IF (L.EQ.1)        GO TO 13                FIL00330
IF (JPL.GE.0)        GO TO 11                FIL00340
NA=1                                         FIL00350
NB=1                                         FIL00360
GO TO 14                                     FIL00370
11 IF (JML.GT.(-2))    GO TO 13               FIL00380
NA=1                                         FIL00390
NB=2                                         FIL00400
GO TO 14                                     FIL00410
13 NA=2                                         FIL00420
NB=2                                         FIL00430
14 DO 21 NL=NA,NB                            FIL00440
LA=L-2+NL                                     FIL00450
LAM=2*LA                                     FIL00460
IF (NL.EQ.3)        GO TO 18                FIL00470
LEF=LAM+1                                    FIL00480
IF ((LD+JC).LT.LEF)    GO TO 17               FIL00490
IF (IABS(LD-JC).GT.LEF)  GO TO 17             FIL00500
IF (JKB.GT.LD)        GO TO 15                FIL00510
IK=JKB+JC+LAM+4                            FIL00520
IS=JKB-JC+LAM+2                            FIL00530
R=-ROOT(IK)*ROOT(IS)*ROOT(LA)              FIL00540
GO TO 16                                     FIL00550
15 IS=JC+JKB-LAM                            FIL00560
IF (IS.EQ.0)        GO TO 17                FIL00570
IR=JC-JKB+LAM+2                            FIL00580
R=ROOT(IR)*ROOT(IS)*ROOT(LA)              FIL00590
16 CALL  LOEFS (LEF,LD,JC,1,0,C)            FIL00600
FI(K,LA)=FI(K,LA)+TK(N)*R*C              FIL00610

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17 IF (NL.EQ.1)	GO TO 21	
18 LEF=LAM-1		FIL00620
IF ((LD+JC).LT.LEF)	GO TO 21	FIL00630
IF (1ABS(LU-JC).GT.LEF)	GO TO 21	FIL00640
IF (JKB.GT.LD)	GO TO 19	FIL00650
IS=JC-JKB+LAM		FIL00660
IF (IS.EQ.0)	GO TO 21	FIL00670
IR=JC+JKB+LAM+2		FIL00680
GO TO 20		FIL00690
19 IS=JKB-JC+LAM		FIL00700
IF (IS.EQ.0)	GO TO 21	FIL00710
IR=JKB+JC+LAM+2		FIL00720
20 R=ROUT(IR)*ROUT(IS)*ROUT(LA+1)		FIL00730
CALL COEFS (LEF,LU,JC,1,U,C)		FIL00740
FI(K,LA)=FI(K,LA)+TK(N)*R*C		FIL00750
21 CONTINUE		FIL00760
22 CONTINUE		FIL00770
RETURN		FIL00780
END		FIL00790
		FIL00800

SUBROUTINE HUM

Purpose: Computes $H(\kappa, \mu')$

Method: For every $\kappa > 0$, the selection rules on the Clebsch-Gordan coefficient are examined to determine the allowed range of λ values. The maximum (positive) value of μ' and its minimum (largest negative) value are computed and indexed for subsequent use. Since j_κ depends only on the absolute value of κ , the Clebsch-Gordan coefficient is the same for $(-\kappa)$ as for κ . Over the allowed range of positive μ' , the Clebsch-Gordan coefficients are computed for given λ and κ , multiplied in turn by $\phi(\kappa, \lambda)$ and $\phi(-\kappa, \lambda)$ to obtain corresponding contributions to $H(\kappa, \mu')$ and $H(-\kappa, \mu')$, and the products are summed over λ . The results are denoted by $HF(K, M)$ where K is a positive integer indexing κ , and $M = \mu' + 1/2$. The procedure is then repeated for μ' negative, leading to $HFM(K, M)$, where K is as above and $M = -\mu' + 1/2$. The explicit separation of positive and negative μ' terms is useful later on.

Subroutines called: C₀EFS, FILL

Subroutine called by: RADINT

Labelled Common: FID ϕ , LIMIT, MAT, QUANT, TRANS, VECT

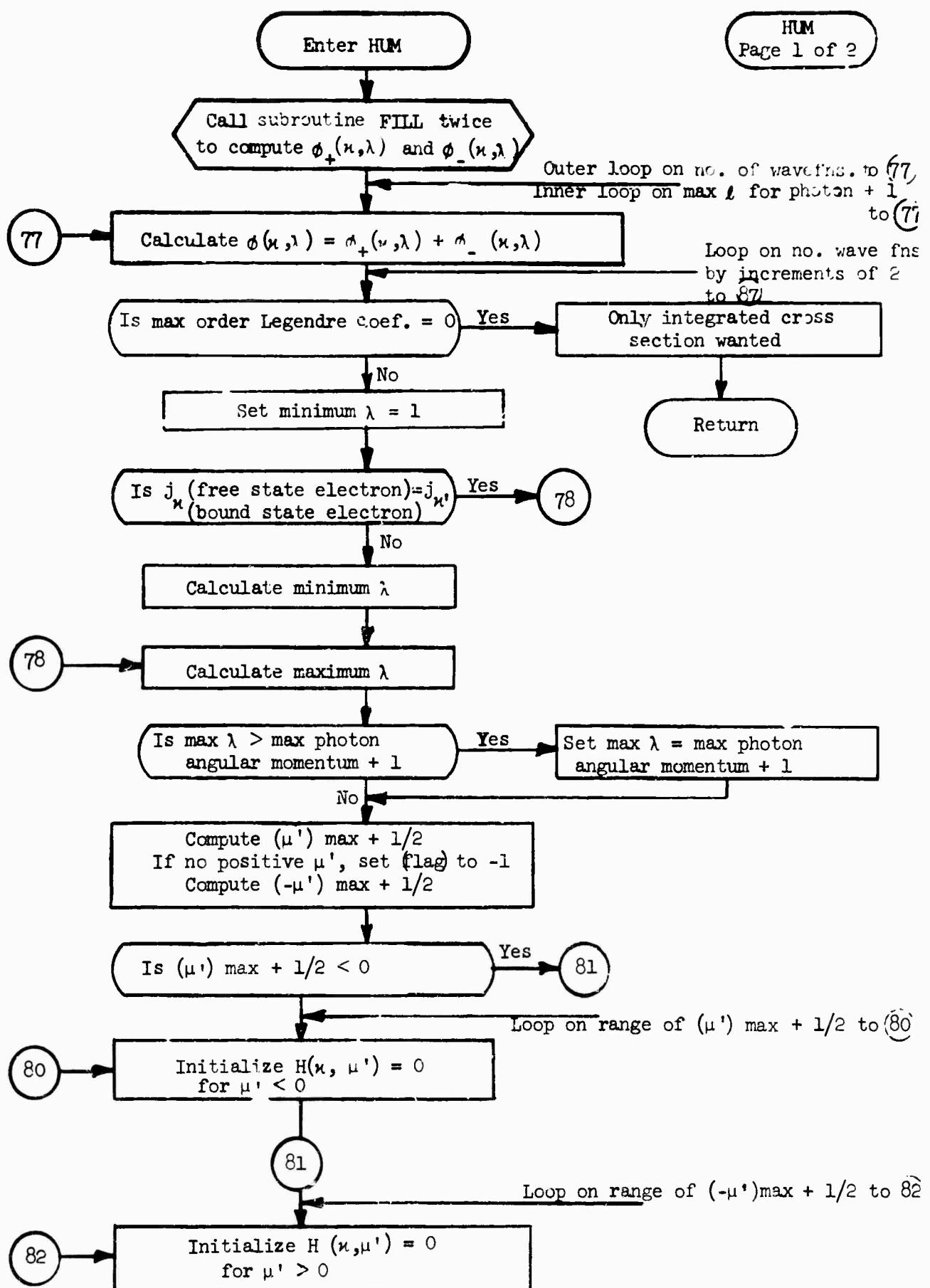
Local Variables:

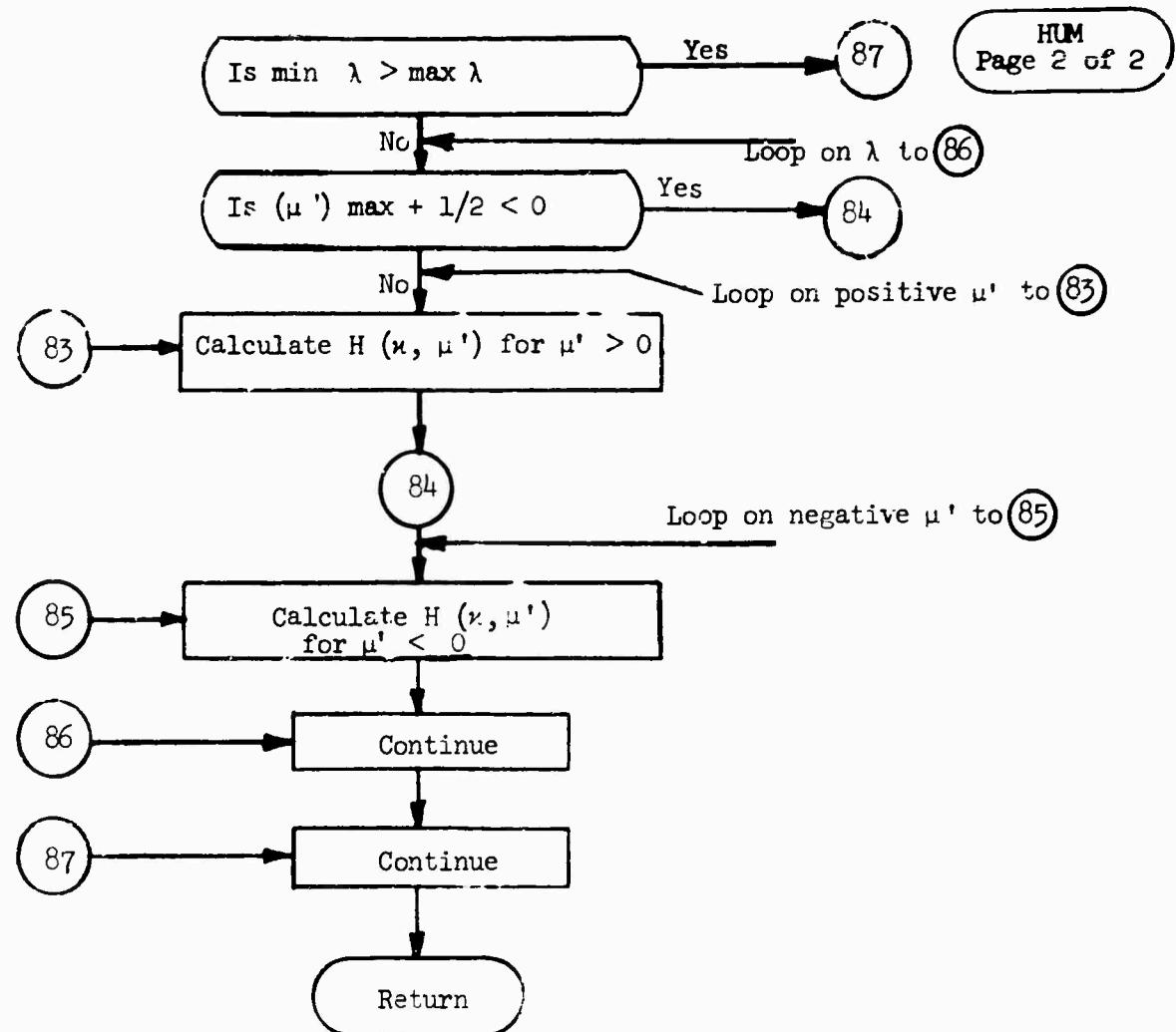
Name	Dimension	Mode	Meaning
LMP		I	Maximum photon angular momentum + 1
K		I	Loop index for bound electron state
LA			λ
JC		I	Twice j_κ (free electron state)
LAD		I	Minimum λ from selection rules

Name	Dimension	Mode	Meaning
LAP		I	Maximum λ from selection rules
JPOS		I	$(\mu')_{\max} + 1/2$ provided $\mu' > 0$ permitted, -1 otherwise
JNEG		I	$(-\mu')_{\max} + 1/2$
M		I	Loop index for μ'
LAM		I	Twice λ
MU		I	Twice μ'

Enter HUM

HUM
Page 1 of 2





S1B+IC HUMM

SUBROUTINE HUM

```

COMMON/F100/FI(30,15),D(30),JMP,NAME,SHELL,QV,E9,IZ          HUM00010
COMMON /LIMIT/JM,LM,KM,K2M,IEND,NEW,NK,NKP,JKB,LMKB,NTAB      HUM00020
COMMON/MAT/SF(30),SG(30),FK(200),FKP(200),SFK(200),SFKP(200),RCUT HUM00030
COMMON/QUANT/LK(30),LMK(30),JK(30),FKAP(30),SN(30),SI(30),CR(30) HUM00040
COMMON/TRANS/HF(30,15),HFM(30,15),JNG(30),JPS(30)           HUM00050
COMMON/VECT/KF(200),KG(200),LBES(200),LBS(200),LKB             HUM00060
DIMENSION F1(30,15),FTP(30,15)                                HUM00070
LMP=LM+1                                                       HUM00080
CALL FILL (FK,KG,LBES,NK,LMKB,FT)                            HUM00090
CALL FILL (FKP,KF,LBS,NKP,LKB,FTP)                           HUM00100
DO 77 K=1,K2M                                                 HUM00110
DO 77 LA=1,LMP                                              HUM00120
// FI(K,LA)=FT(K,LA)+FTP(K,LA)                               HUM00130
IF ( JM .EQ. 0 )          RETURN                               HUM00140
DO 87 K=1,K2M+2                                             HUM00150
KP = K + 1                                                   HUM00160
JC=JK(K)                                                    HUM00170
LAU=1                                                       HUM00180
IF ( JC.EQ.JKB)      GO TO 78                               HUM00190
LAU=IAHS (JC-JKB)/2                                         HUM00200
78 LAP = (JC+JKB)/2                                         HUM00210
IF ( LAP .GT. LMP )          LAP = LMP                      HUM00220
JP05=JC-2                                                   HUM00230
IF ( JC.LT.4)      GO TO 79                               HUM00240
JP05=MIND (JKB,JP05)                                         HUM00250
JP05=(JP05+1)/2                                            HUM00260
79 JNEG=MINU (JKB,(JC+2))                                 HUM00270
JNEG=(JNEG+1)/2                                            HUM00280
JNG(K)=JNEG                                               HUM00290
JPS(K)=JP05                                              HUM00300
JNG(KP)=JNEG                                              HUM00310
JPS(KP)=JP05                                              HUM00320
IF ( JP05.LT.0)      GO TO 81                           HUM00330
DO 80 M=1,JP05                                           HUM00340
HF(K,M) = 0.0                                              HUM00350
80 HF(KP,M) = 0.0                                         HUM00360
81 DO 82 M=1,JNEG                                         HUM00370
HFM(K,M) = 0.0                                              HUM00380
82 HFM(KP,M) = 0.0                                         HUM00390
IF ( LAU.GT.LAP)      GO TO 87                           HUM00400
DO 86 LA=LAU,LAP                                         HUM00410
LAM=2*LA                                                 HUM00420
IF ( JP05.LT.0)      GO TO 84                           HUM00430
DO 83 M=1,JP05                                           HUM00440
MU=2*M-1                                                 HUM00450
CALL COEFS (LAM,JKB,JC,2,MU,C)                           HUM00460
HF(K,M) = HF(K,M) + FI(K,LA) * C                         HUM00470
83 HF(KP,M) = HF(KP,M) + FI(KP,LA) * C                  HUM00480
84 DO 85 M=1,JNEG                                         HUM00490
MU=1-2*M                                                 HUM00500
CALL COEFS (LAM,JKB,JC,2,MU,C)                           HUM00510
HFM(K,M) = HFM(K,M) + FI(K,LA) * C                         HUM00520
85 HFM(KP,M) = HFM(KP,M) + FI(KP,LA) * C                  HUM00530
86 CONTINUE                                              HUM00540
87 CONTINUE                                              HUM00550
RETURN                                                 HUM00560
END                                                 HUM00570

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SUBROUTINE INTERP

Purpose: Interpolates on the bound-state tabulations for radii greater than one-half Bohr unit where the integration grid is much finer than the table, to obtain intermediate values of the bound-state wavefunctions and corresponding potential.

Method: Linear interpolation between successive entries in table.

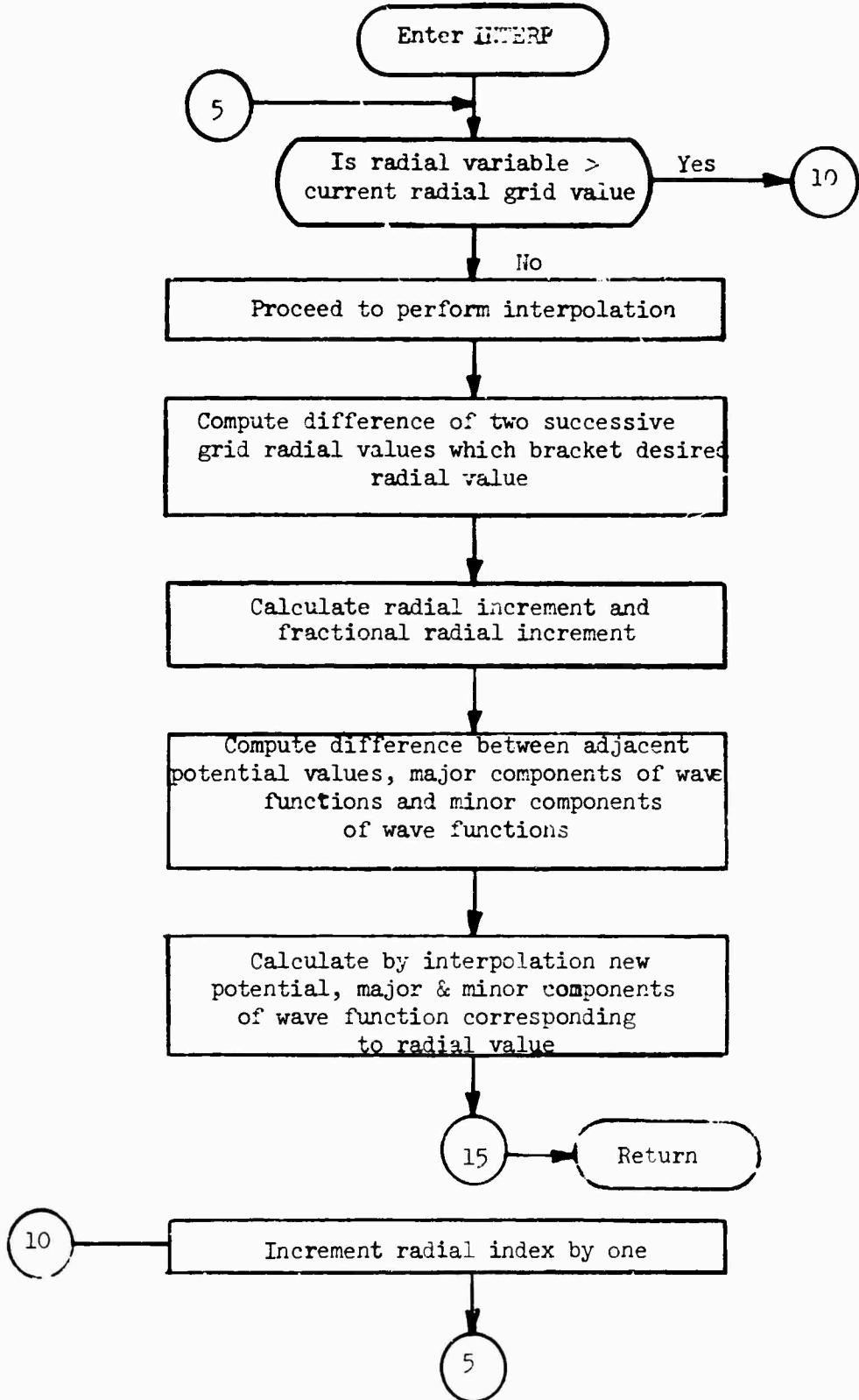
Subroutine called: None

Subroutine called by: XDERIV

Labelled Common: LIMIT, ϕ NWARD, TAPES

Local Variables:

Name	Dimension	Mode	Meaning
DX		R	Difference between two successive tabulated radial values
DL		R	Radial increment; difference between integrating radius and lower grid point
QU ϕ T		R	Fractional radial increment
DV		R	Difference between two successive tabulated potential values
DGB		R	Difference between two successive tabulated values of "large" component of wavefunction.
DFB		R	Difference between two successive tabulated values of "small" component of wavefunction.



SIMPLC INTP

SUBROUTINE INTPR
COMMON/LIMIT/JM,LM,KM,K2M,IEND,NEW,NK,NKP,JKB,LMKB,NTAB
COMMON /ONWARD/RX,SCX,GBX,FBX
COMMON/TAPES/X(1500),SCF(1500),FB(1500),GB(1500),GAMB,SCREEN

5 IF (RX.GT.X(NTAB+1)) GO TO 10
UX = X(NTAB+1)-X(NTAB)
UL = RX-X(NTAB)
QUOT = UL/UX
UV = SCF(NTAB+1)-SCF(NTAB)
UGB = GB(NTAB+1)-GB(NTAB)
DFB = FB(NTAB+1)-FB(NTAB)
SCX = SCF(NTAB)+QUOT*UV
GBX = GB(NTAB)+QUOT*UGB
FBX = FB(NTAB)+QUOT*DFB
GO TO 15
10 NTAB = NTAB+1
GO TO 5
15 RETURN
END

INT00010
INT00020
INT00030
INT00040
INT00050
INT00060
INT00070
INT00080
INT00090
INT00100
INT00110
INT00120
INT00130
INT00140
INT00150
INT00160
INT00170
INT00180
INT00190

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SUBROUTINE LEGEND

Purpose: Computes the Legendre coefficients of the cross section.

Method: For $j = 0$, this consists of carrying out the sum

$$D_0 = \frac{\pi^2 e^2 w}{2\epsilon} \sum_{\lambda} \frac{1}{2\lambda + 1} \sum_{\kappa} \phi^2(\kappa, \lambda) \text{ over all } \kappa \text{ and } \lambda$$

(The ϕ 's have been initialized.) For $j > 0$, subroutine MUSS is called where the $T_j(\kappa, \kappa')$ of the sum

$$D_j = \frac{\pi^2 e^2 w}{2\epsilon} (-1)^j \sum_{\kappa \kappa'} \cos(\delta_{\kappa} - \delta_{\kappa'}) T_j(\kappa, \kappa') \text{ is performed.}$$

The summation $(-1)^j \sum_{\kappa \kappa'} \cos(\delta_{\kappa} - \delta_{\kappa'}) T_j(\kappa, \kappa')$ is subject to the selection rules $\Delta(j_{\kappa}, j_{\kappa'}, j)$, $\Delta(l_{\kappa}, l_{\kappa'}, j)$ and $l_{\kappa} + l_{\kappa'} + j = \text{even integer}$. The diagonal terms in the double sum are done first (with the cosine equal to unity), carried over $j_{\kappa} > 1/2$ and contributing to even j terms only. Since the off-diagonal terms are symmetric in κ and κ' , twice the sum with $K' < K$ is taken. For given κ and κ' , the smallest j for which there can be a contribution is $|l_{\kappa} - l_{\kappa'}|$ provided $|j_{\kappa} - j_{\kappa'}|$ is not larger; otherwise $j = |j_{\kappa} - j_{\kappa'}|$ has the wrong parity and the minimum j value is $|j_{\kappa} - j_{\kappa'}| + 1 = |l_{\kappa} - l_{\kappa'}| + 2$. There may also be contributions for larger j (going up in steps of two to preserve parity) up to the lesser of $(l_{\kappa} + l_{\kappa'})$ and $(j_{\kappa} + j_{\kappa'})$, or up to an assigned maximum j if smaller.

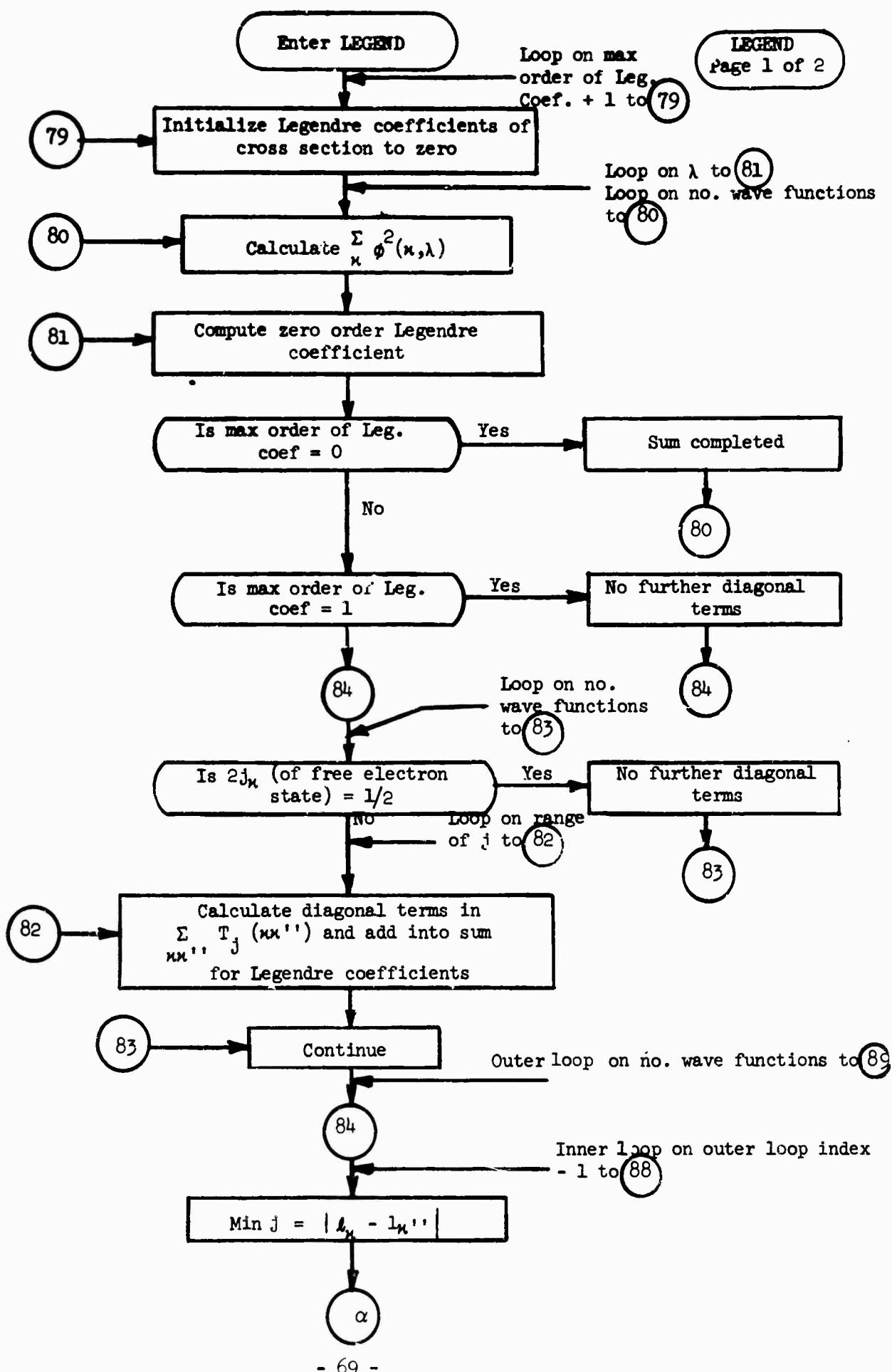
Subroutine called: MUSS

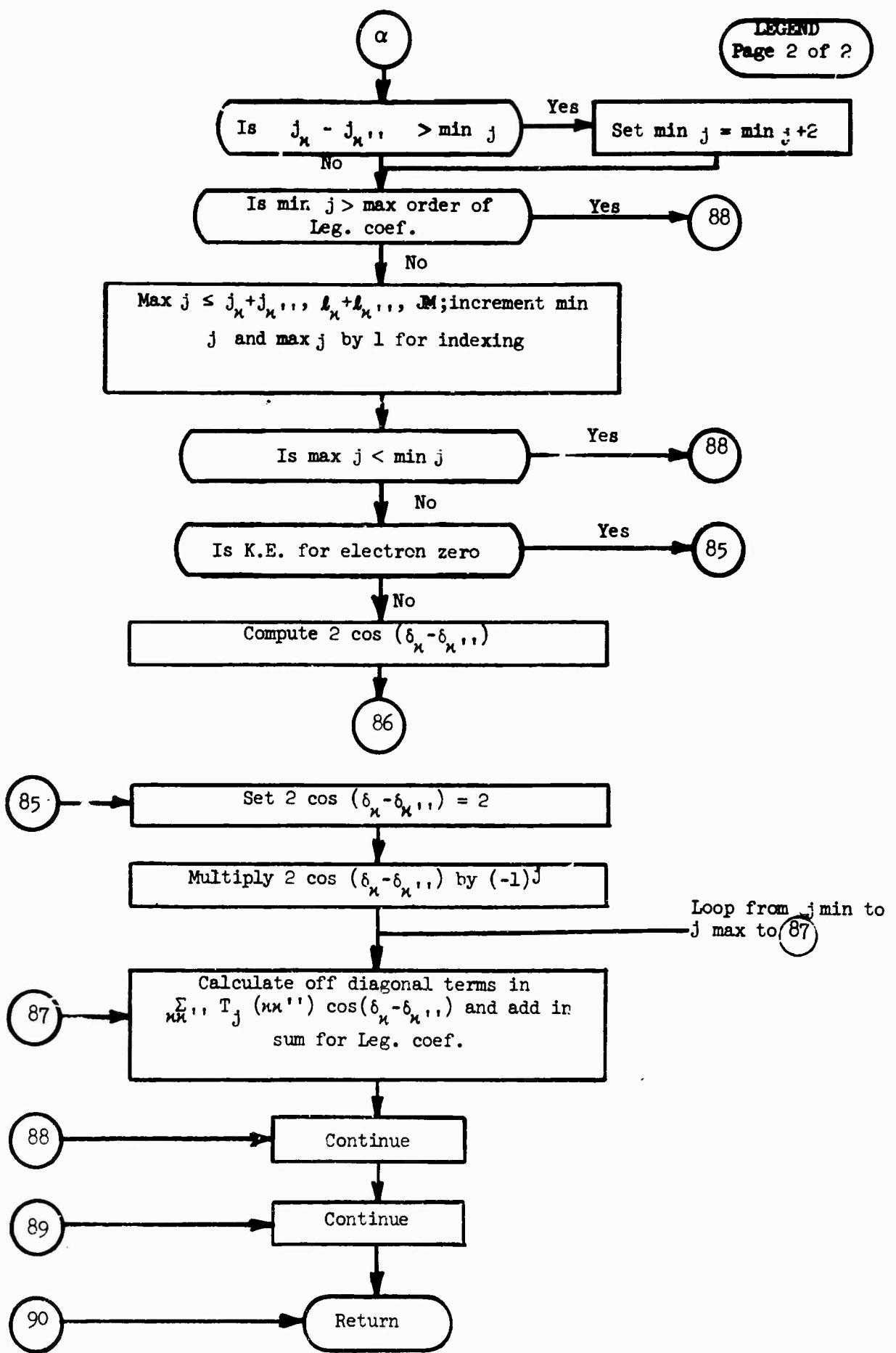
Subroutine called by: PELEC

Labelled Common: FINDΦ, LIMIT, QUANT

Local Variables:

Name	Dimension	Mode	Meaning
LMP		I	Max photon angular momentum + 1
J		I	Order of Legendre coefficient
LA		I	λ
STAT		R	$2\lambda + 1$
SKP		R	$\sum_{\kappa} \phi^2(\kappa, \lambda)$
JMAX		I	Max j contribution for given κ and κ''
JMIN		I	Min j contribution for given κ and κ''
K		I	Loop index for bound electron state
TJ		R	$T_j(\kappa, \kappa'')$
JDIF		I	$ \epsilon_{\kappa} - \epsilon_{\kappa''} $
COD		R	$2 \cos(\delta_{\kappa} - \delta_{\kappa''})$
MINI		I	$(-1)^{j-1}$





SUBROUTINE LEGEND

SUBROUTINE LEGEND

COMMON/F1UU/F1(30,15),D(30),JMP,NAME,SHELL,QV,EB,IZ	LEG00010
COMMON/LIMIT/JM,LM,KM,K2M,IEND,NEW,NK,NKP,JKB,LMKB,NTAB	LEG00020
COMMON/QUANT/LK(30),LMK(30),JK(30),FKAP(30),SN(30),SI(30),CR(30)	LEG00030
LMW=LM+1	LEG00040
DO 74 J=1, JMP	LEG00050
74 U(J)=U.0	LEG00060
DO 81 LA=1, LMW	LEG00070
STAT=2*LA+1	LEG00080
SKP=U.0	LEG00090
DO 80 K=1, K2M	LEG00100
80 SKP = SKP+F1(K,LA)*F1(K,LA)	LEG00110
81 U(1)=U(1)+SKP/STAT	LEG00120
IF (JM.EQ.0) GO TO 90	LEG00130
IF (JM.EQ.1) GO TO 84	LEG00140
DO 83 K=1, K2M	LEG00150
IF (JK(K) .EQ. 1) GO TO 83	LEG00160
JMAX=MINU(JK(K),2*LK(K),JM)+1	LEG00170
DO 82 J=3, JMAX,2	LEG00180
CALL MUSS(K,K,J,TJ)	LEG00190
82 U(J)=U(J)+TJ	LEG00200
83 CONTINUE	LEG00210
84 DO 89 K=2, K2M	LEG00220
KLS=K-1	LEG00230
DO 88 KK=1, KLS	LEG00240
JMIN=IABS(LK(K)-LK(KK))	LEG00250
JDIF=IABS(JK(K)-JK(KK))	LEG00260
IF (JDIF.GT.(2*JMIN)) JMIN=JMIN+2	LEG00270
:IF (JMIN.GT.JM) GO TO 38	LEG00280
JMIN=JMIN+1	LEG00290
JMAX=MINU(((JK(K)+JK(KK))/2),(LK(K)+LK(KK)),JM)+1	LEG00300
IF (JMAX .LT. JMIN) GO TO 88	LEG00310
IF (IEND .EQ. 1) GO TO 85	LEG00320
COD = 2.0 * (CR(K)*CR(KK) + SI(K)*SI(KK))	LEG00330
GO TO 86	LEG00340
85 COD = 2.0	LEG00350
86 MINI= MOD(JMIN,2)	LEG00360
IF (MINI.EQ.0) COD=-COD	LEG00370
DO 87 J=JMIN,JMAX,2	LEG00380
CALL MUSS (K,KK,J,TJ)	LEG00390
87 U(J)=U(J)+TJ*COD	LEG00400
88 CONTINUE	LEG00410
89 CONTINUE	LEG00420
90 RETURN	LEG00430
END	LEG00440
	LEG00450

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SUBROUTINE LOGGAM

Purpose: Computes the natural logarithm of the gamma function for complex arguments, i.e. $\ln \Gamma(x + iy)$ and $\operatorname{Im} \ln \Gamma(x + iy)$

Method: a) Set $\Gamma(z) = -z + (z - 1/2) \ln z + \ln \sqrt{2\pi} + J(z)$ where $J(z)$ is given as a continuous fraction. See Wall, "Analytic Theory of Continued Functions," p. 364, formula 93.9.

b) For $x > 2$, $\ln \Gamma(z)$ is computed from the recursion relation:

$$\ln \Gamma(z) = \ln \Gamma(1 + z) - \ln z$$

c) For negative x , the $\operatorname{Im} \ln \Gamma(z)$ can be thought of as being equal to $V + 2\pi k$ where k is an integer and V is given by this routine.

Restrictions: a) x and y may not both be equal to zero.

b) if $y = 0$, x may not be equal to a negative integer.

This routine is taken from M. S. Shapiro and M. Goldstein, "A Collection of Mathematical Computer Routines," NYO-1480-14 (1965).

Subroutine called: None

Subroutine called by: RADINT

Argument sequence: (X, Y, U, V)

Argument List:

Name	Dimension	Mode	Meaning
X		R	Real part of argument
Y		R	Imaginary part of argument
U		R	Real part of result
V		R	Imaginary part of result

```

S18FIC LGAM
  SUBROUTINE LOGGAM(X,Y,U,V)                               LGM00010
C THIS SUBROUTINE COMPUTES THE NATURAL LOG OF THE GAMMA FUNCTION FOR   LGM00020
C COMPLEX ARGUMENTS. THE ROUTINE IS ENTERED BY THE STATEMENT           LGM00030
C   CALL LGGM(X,Y,U,V)                                                 LGM00040
C WHERE X IS THE REAL PART OF THE ARGUMENT                      LGM00050
C       Y IS THE IMAGINARY PART OF THE ARGUMENT                  LGM00060
C       U IS THE REAL PART OF THE RESULT                         LGM00070
C       V IS THE IMAGINARY PART OF THE RESULT                  LGM00080
  DIMENSION H(7)                                              LGM00090
  H(1)=2.269488974                                         LGM00100
  H(2)=1.517473649                                         LGM00110
  H(3)=1.011523068                                         LGM00120
  H(4)=.5256064690                                         LGM00130
  H(5)=.2523809524                                         LGM00140
  H(6)=0.053333333333                                     LGM00150
  H(7)=0.083333333333                                     LGM00160
  E2=1.57079632679                                         LGM00170
  E8=3.14159265359                                         LGM00180
  B1=0.0                                           LGM00190
  B2=0.0                                           LGM00200
  J=2                                           LGM00210
  X2=X                                           LGM00220
  4 IF(X)1,2,3                                         LGM00230
  3 B6=ATAN(Y/X)                                         LGM00240
  1=X*X                                         LGM00250
  5 B7=Y*Y+T                                         LGM00260
C REAL PART OF LGM                                         LGM00270
  T1=0.5*ALOG(B7)                                         LGM00280
  IF(X>2.0)7,7,6                                         LGM00290
  / B1=B1+B6                                         LGM00300
  B2=B2+T1                                         LGM00310
  X=X+1.0                                         LGM00320
  J=1                                           LGM00330
  GO TO 4                                         LGM00340
  6 T3=-Y*B6+(T1*(X-.5)-X+.9189365332 )          LGM00350
  T2=B6*(X-.5)+Y*T1-Y                                LGM00360
  T4=X                                           LGM00370
  T5=-Y                                           LGM00380
  T1=B7                                           LGM00390
  DO 8 I=1,7                                         LGM00400
  T=H(I)/T1                                         LGM00410
  T4=I*T4+X                                         LGM00420
  T5=-(I*T5+Y)                                         LGM00430
  8 T1=I*T4+T5*T5                                         LGM00440
  T3=T4-X+T5                                         LGM00450
  T2=-T5-Y+T2                                         LGM00460
  GO TO 10 (9,10),J                                    LGM00470
  9 T3=T3-B2                                         LGM00480
  T2=T2-B1                                         LGM00490
  10 IF(X2)11,12,12                                    LGM00500
  12 U=T3                                         LGM00510
  V=T2                                         LGM00520
  X=X2                                         LGM00530
  RETURN                                         LGM00540
  11 U=T3-E4                                         LGM00550
  V=T2-E5                                         LGM00560
  X=X2                                         LGM00570
  RETURN                                         LGM00580
C X IS ZERO                                         LGM00590
  2 T=0.0                                         LGM00600
  IF(Y)13,14,15                                    LGM00610

```

13 B6=-E2 LGM00620
GO TO 5 LGM00630
15 B6=E2 LGM00640
GO TO 5 LGM00650
C X IS NEGATIVE LGM00660
1 E4=0.0 LGM00670
E5=0.0 LGM00680
IE6=0 LGM00690
16 E4=E4+.5*(ALOG(X*X +Y*Y)) LGM00700
E5=E5+ATAN (Y/X) LGM00710
IE6=IE6+1 LGM00720
X=X+1.0 LGM00730
IF(X)16,17,17 LGM00740
17 IF(MOD (IE6,2))18,4,18 LGM00750
18 E5=E5+E8 LGM00760
GO TO 4 LGM00770
14 WRITE(6,19) X2,Y LGM00780
19 FORMAT(2YM ATTEMPTED TO TAKE LOGGAM OF 2HX=F6.0,1X2HY=F6.0)
CALL EXIT LGM00790
RETURN LGM00800
END LGM00810
LGM00820

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SUBROUTINE MUSS

Purpose: Performs the μ' sum and computes the term $T_j(\kappa, \kappa'') = C(j_\kappa, j_\kappa j; 1/2, -1/2) \sum_{\mu'} (-1)^{\mu' + 1/2} H(\kappa, \mu') H(\kappa'', \mu')$ $C(j_\kappa, j_\kappa j; \mu' + 1, -\mu' - 1)$ which is used in computation of D_j (Legendre coefficient).

Method: The sum is carried out first for $(\mu' + 1/2) \geq 0$, computing the C-coefficients and recording them as an indexed variable, the upper limit on μ' being the lesser of the upper limits for κ and κ'' computed in subroutine HUM. The sum for the negative $(\mu' + 1/2)$ is similarly carried up to the lesser of the maximum $|\mu'|$ values for negative μ' , but the C-coefficient is obtained from the previously obtained ones by a symmetry operation (introducing at most a sign change). The C-coefficient in front of the sum is the one computed for $\mu' = -1/2$.

Subroutine called: C0EFS

Subroutine called by: LEGEND

Labelled Common: QUANT, TRANS

Argument sequence: (K, KK, J, TJ)

Argument List:

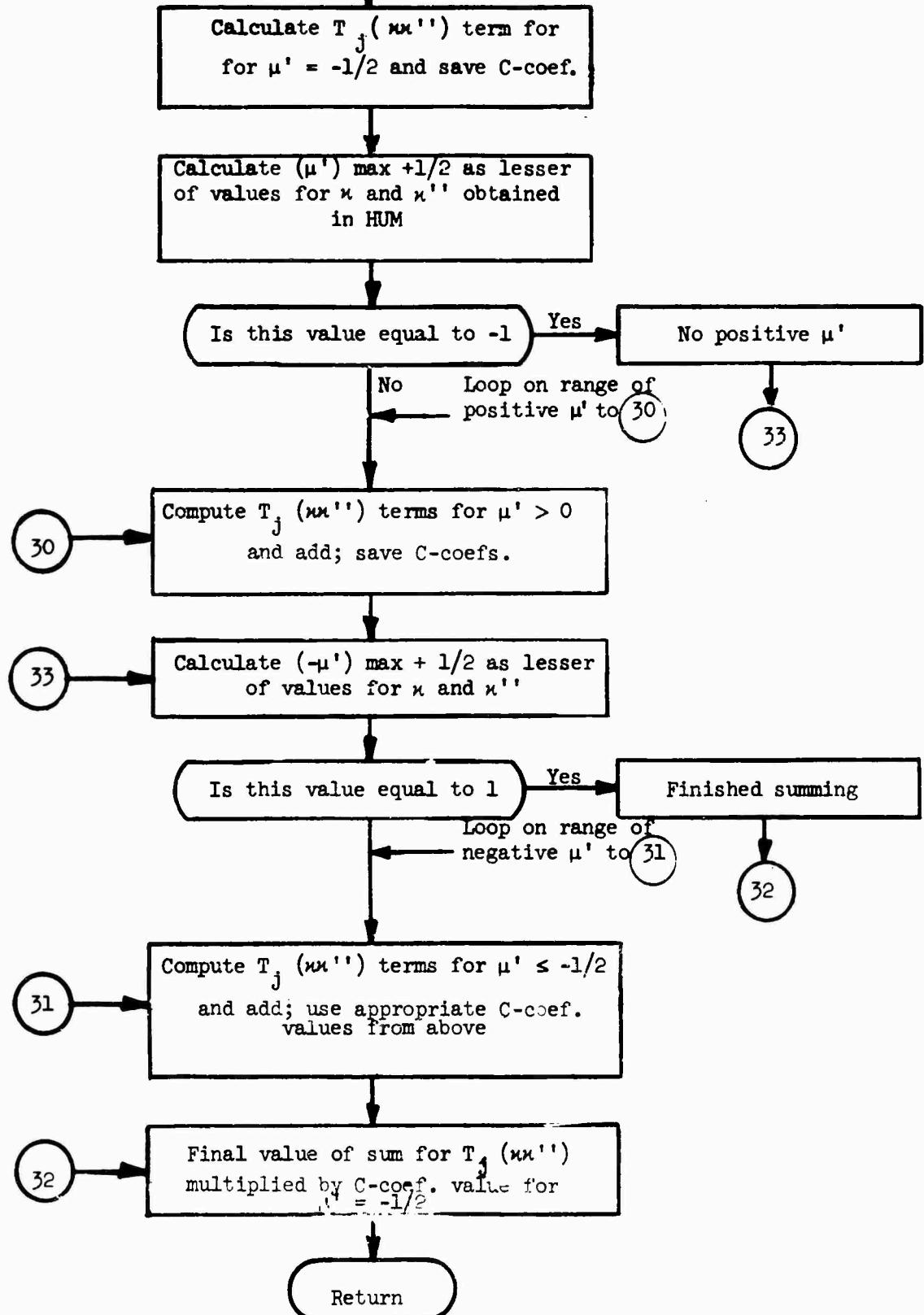
Name	Dimension	Mode	Meaning
K		I	Index for κ
KK		I	Index for κ''
J		I	Order of Legendre coefficient + 1
TJ		R	$T_j(\kappa, \kappa'')$

Local Variables:

Name	Dimension	Mode	Meaning
JD		I	Twice order of Legendre coefficient
C		R	Clebsch-Gordan coefficient
CL	30	R	Clebsch-Gordan coefficient saved
JP <small>OS</small>		I	Range of positive μ' (-1 means none)
M		I	Loop index for μ'
PM		R	$(-1)^{\mu' + 1/2}$ (times $i^{j_\kappa + j_{\kappa'}, + j}$ if μ' negative)
MP		I	$2 \mid \mu' + 1 \mid$
JNEG		I	Range of negative μ'
JMD		I	$i^{j_\kappa + j_{\kappa'}, + j}$

Enter MUSS

MUSS
Page 1 of 1



SIBFIC MUSE

```
SUBROUTINE MUSS (K, KK, J, TJ)          MUS00010
COMMON/QUANT/LK(30),LMK(30),JK(30),FKAP(30),SN(30),SI(30),CR(30) MUS00020
COMMON/TRANS/HF(30,15),HFM(30,15),JNG(30),JPS(30)      MUS00030
DIMENSION CL(30)                      MUS00040
JD=2*(J-1)                          MUS00050
CALL COEFS(JK(K),JK(KK),JD,1,-1,C)    MUS00060
TJ = HFM(K,1) * HFM(KK,1) * C          MUS00070
CL(1)=C                            MUS00080
JPOS=MIN0(JPS(K),JPS(KK))           MUS00090
IF (JPOS.EQ.1)      GO TO 33        MUS00100
PM=1.0                            MUS00110
DO 30 M=1,JPOS                   MUS00120
PM=-PM                           MUS00130
MP=2*M+1                         MUS00140
CALL COEFS(JK(K),JK(KK),JD,MP,-MP,C) MUS00150
CL(MP)=C                         MUS00160
30 TJ = TJ + HF(K,M) * HF(KK,M) * C * PM      MUS00170
35 JNEG=MIN0(JNG(K),JNG(KK))       MUS00180
IF (JNEG.EQ.1)      GO TO 32        MUS00190
JMOD=MOD((JK(K)+JK(KK)+JD),4)      MUS00200
PM=-1.0                           MUS00210
IF (JMOD.EQ.0)      PM=1.0        MUS00220
DO 31 M=2,JNEG                  MUS00230
PM=-PM                           MUS00240
MP=2*M-3                         MUS00250
31 TJ = TJ + HFM(K,M) * HFM(KK,M) * CL(MP) * PM      MUS00260
32 TJ=TJ*CL(1)                    MUS00270
RETURN                           MUS00280
END                                MUS00290
```

SUBROUTINE RADINT

Purpose: This is the control subroutine for the integrations.

Method: The requisite coefficients and the initial values of the free-electron wavefunctions and their derivatives are computed. The radial integrals are performed by calling the Runge-Kutta integration subroutines in D ϕ loops. Normalization factors are obtained from WNORM and applied to the matrix elements. The phase shifts are obtained by wave-matching. Finally, subroutine HUM is called to start the angular momentum sums.

Subroutines called: LGGAM, RKUT, DERIV, XDERIV, XRKUT, WNORM, SPHBES, HUM

Subroutine called by: PELEC

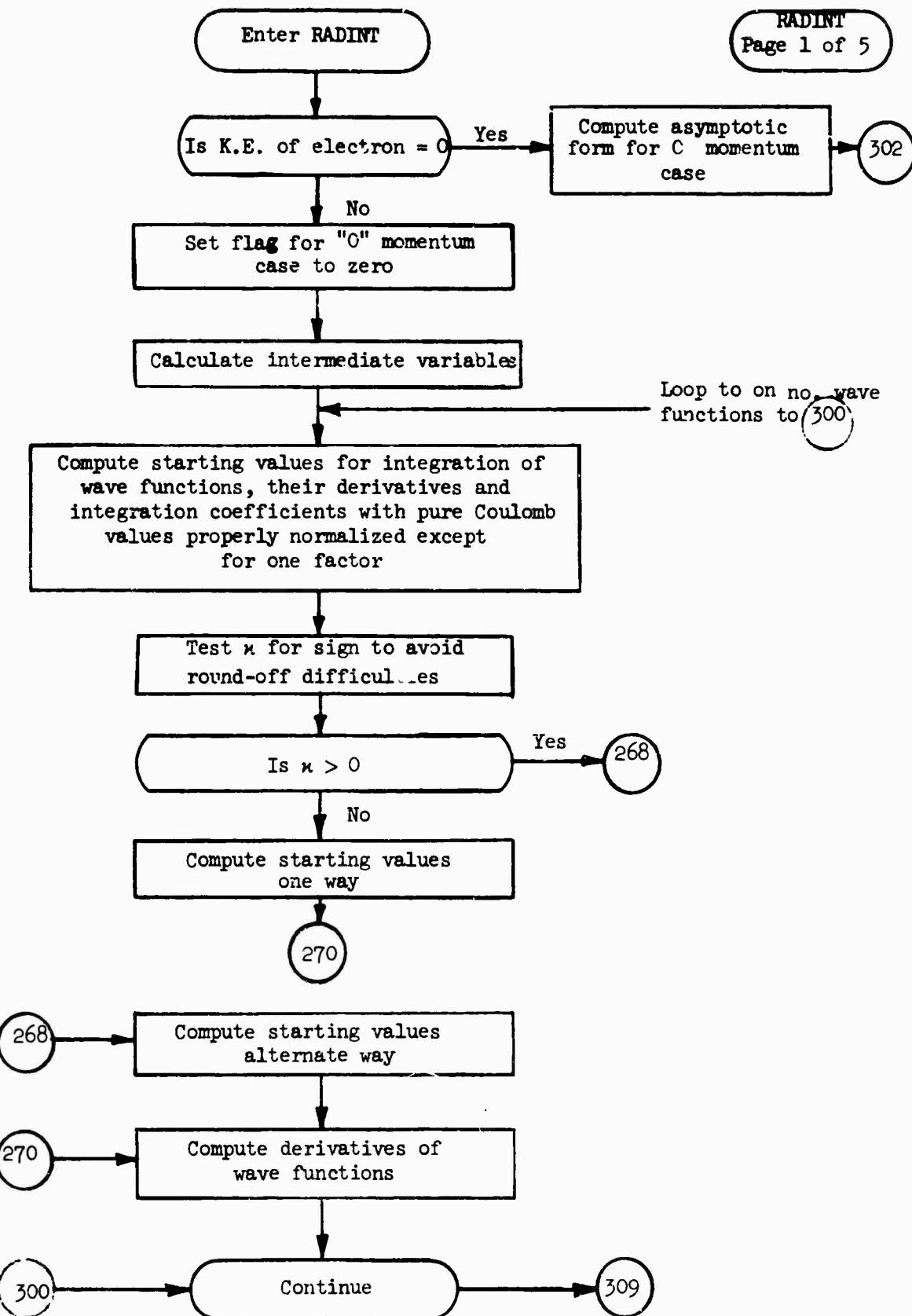
Variables in unlabelled Common: PI, HALFPI, FURPI, RAD, SQ2, Q, ZA, ZAZA,
EFN, EGN, V, CG, GAM

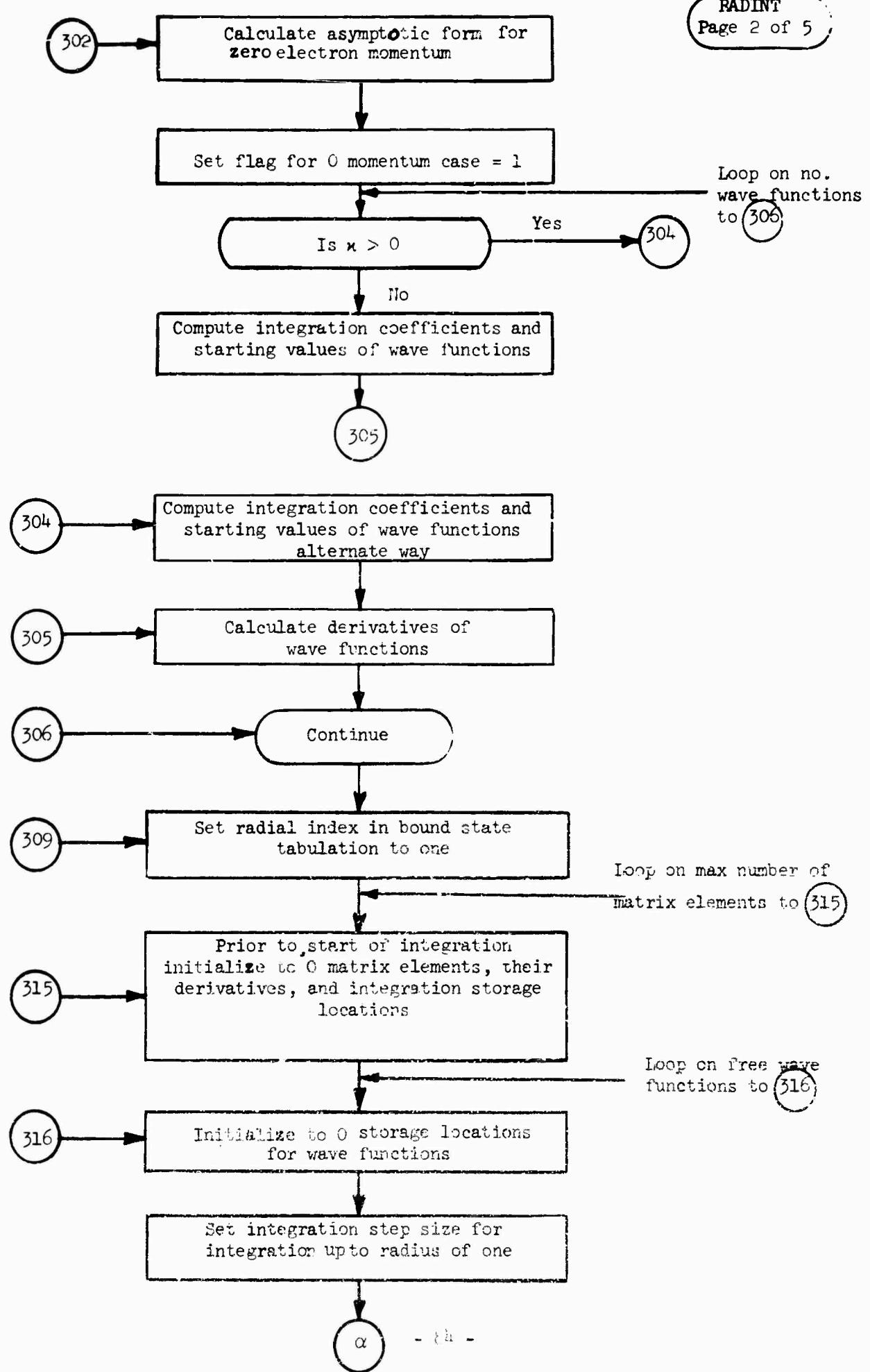
Labelled Common: BESSEL, DFUNC, LIMIT, MAT, QUANT, VECT, ONWARD

Local Variables:

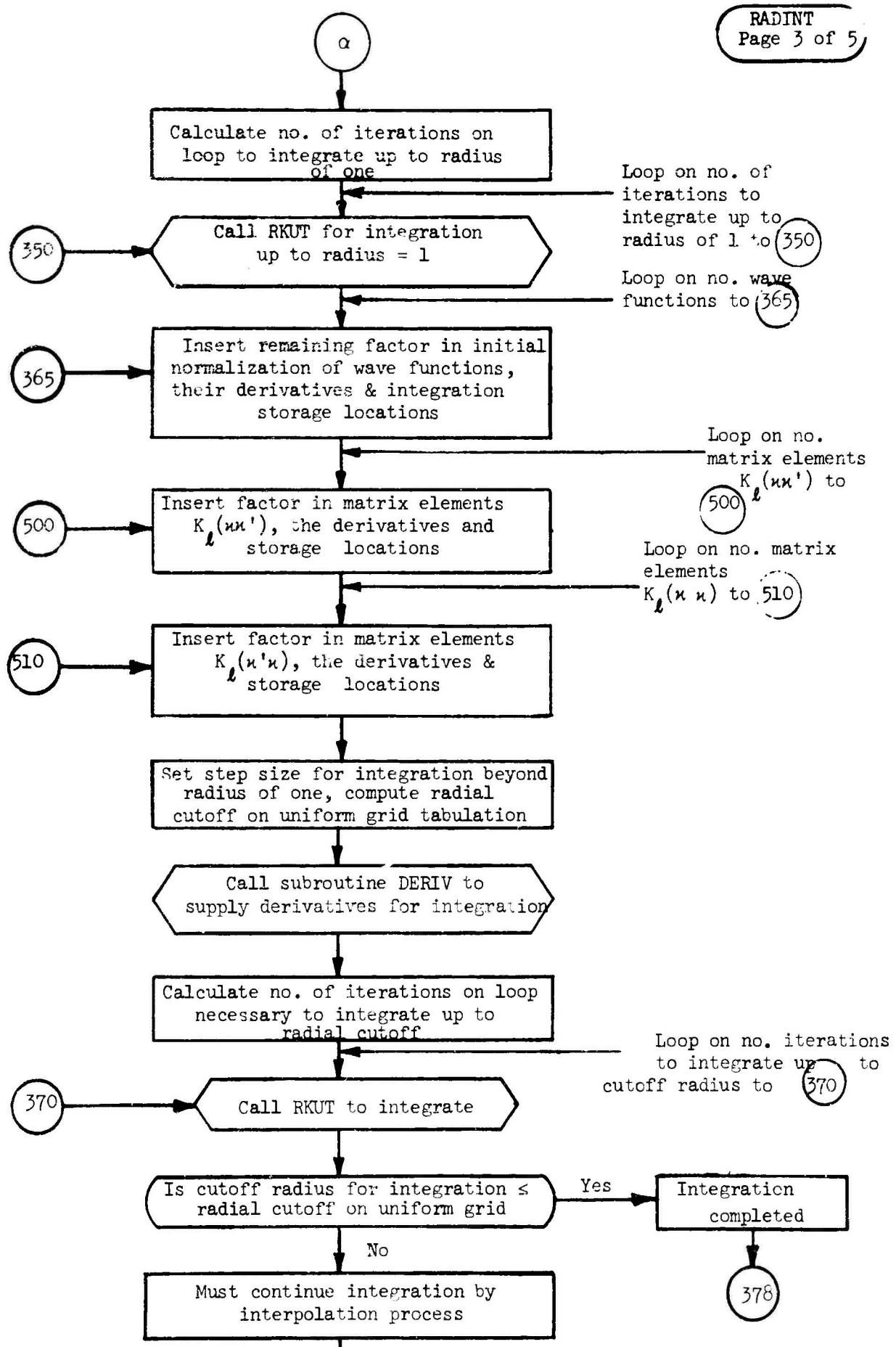
Name	Dimension	Mode	Meaning
E		R	Free electron energy (in mc^2 units)
RK		R	$\sqrt{E^2 - 1}$, free electron momentum
I		I	Loop index of free electron state
TUGAM	30	R	$2\sqrt{\mu^2 - (\frac{Z}{137.0367})^2} + 1$
IUP		I	Max number of matrix elements
N ϕ		I	Loop index to initialize to zero components of free electron wavefunction, their derivatives, integrand for matrix elements and their integration storage variables.
N		I	Range on number of iterations for radial integration up to radius of one.
XCUT		R	Radial cutoff on uniform grid in tabulation.
WAVE		R	Max of wave numbers of free electron and photon.

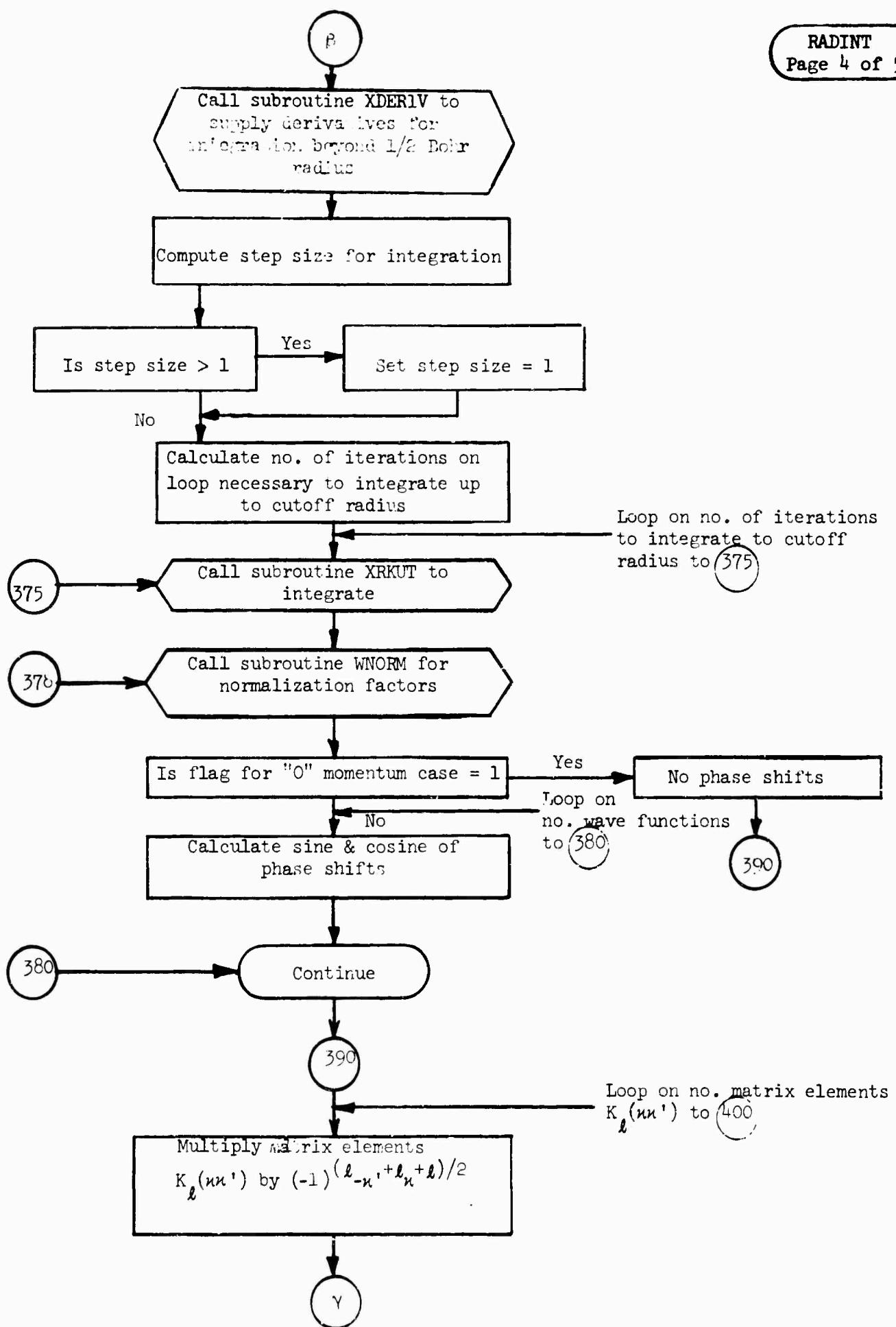
Name	Dimension	Mode	Meaning
LUB		I	Range on number of iterations beyond one-half Bohr radius for radial integration
RX		R	Current radial variable beyond one-half Bohr radius
LTOT		I	$\ell_{-n}, + \ell_n + \ell$

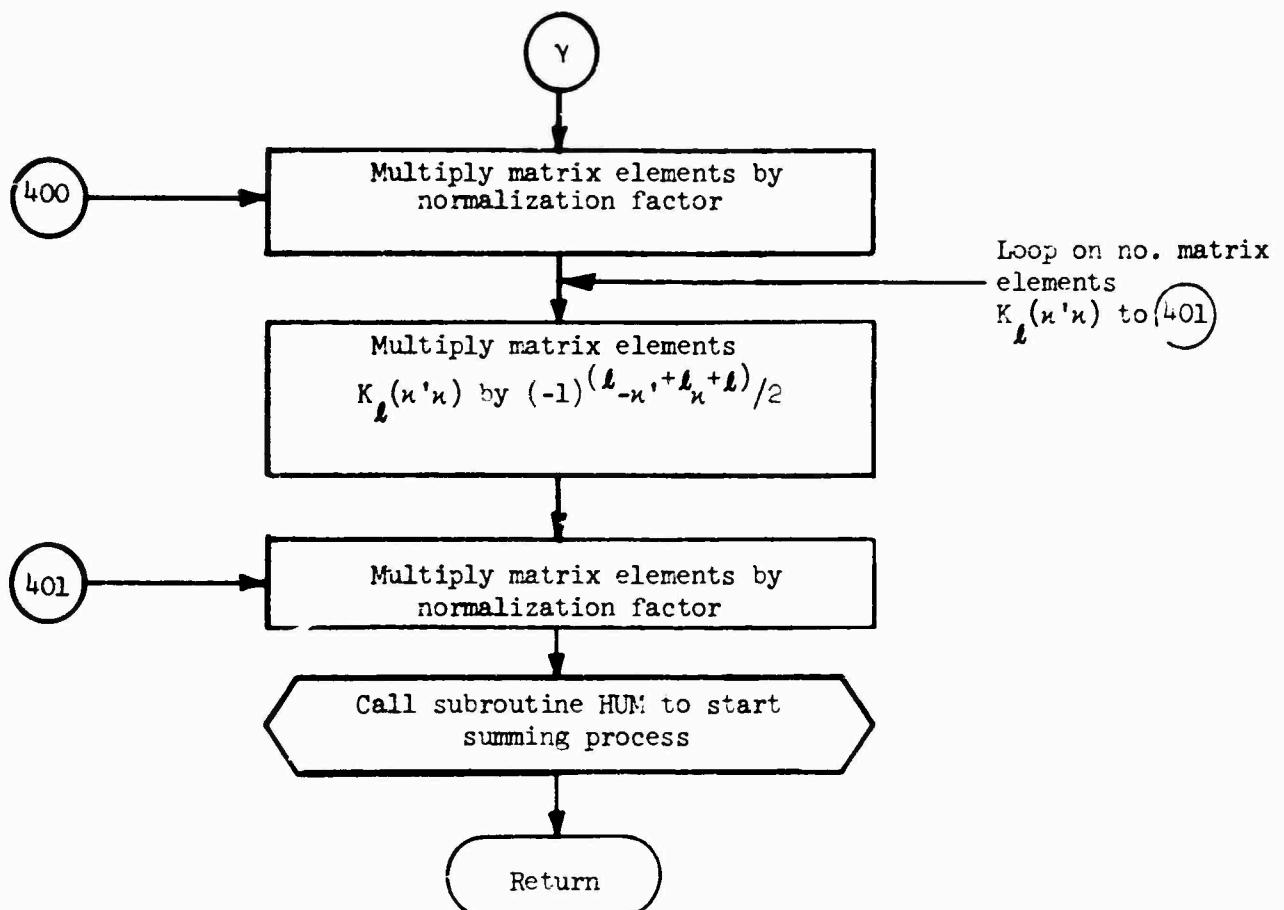




- 14 -







S18F1C RADN

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SUBROUTINE RADINT                               RAD00010
COMMON PI,HALFPI,FOURPI,RAD,SQ2,Q,ZA,ZAZA,EFN,EGN,V,CG(30),GAM(30)RAD00020
COMMON/BESSEL/FL(15),PC(15),OF(15,15),M1,M2,B(15)      RAD00030
COMMON/DFUNC/F(30),G(30),DF(30),DG(30),DFK(200),DFKP(200),CF(30),HRAD00040
COMMON/LIMIT/JM,LM,KM,K2M,IEND,NEW,NK,NKP,JKB,LMB,NTAB    RAD00050
COMMON/MAT/SF(30),SG(30),FK(200),FKP(200),SFK(200),SFKP(200),RCUT RAD00060
COMMON /ONWARD/RX,SCX,GBX,FBX                  RAD00100
COMMON/QUANT/LK(30),LMK(30),JK(30),FKAP(30),SN(30),SI(30),CR(30) RAD00070
COMMON/VECT/KF(200),KG(200),LBES(200),LBS(200),LKB        RAD00080
DIMENSION KNORM(30), TUGAM(30)                 RAD00090

100 FORMAT(5X,5ULENGTH UNITS ARE HBAR MC ( 1 BOHR RADIUS = 137 )//)RAD00110
101 FORMAT (5X,24HINTEGRATION STEP SIZE IS,F11.7, 5X,5HUP TO,F9.3//) RAD00120
E = EFN+1.0                                     RAD00130
EGN = E+1.0                                     RAD00140
IF ( EFN .EQ. 0.)      GO TO 302               RAD00150
RK = SQRT(EFN*EGN)                            RAD00160
IEND = 0                                         RAD00170
SQEG = SQRT (EGN)                            RAD00180
SQE = RK/SQEG                                RAD00190
RKE = RK / EGN                                RAD00200
GNU = ZA*E/RK                                 RAD00210
TRK = 2.0*RK                                 RAD00220
TWORK = EXP ( GNU * HALFPI ) / SQRT ( TRK * PI ) RAD00230
DO 300 I=1,K2M                                RAD00240
GAM(I) = SQRT (FKAP(I)**2-ZAZA)                RAD00250
TUGAM(I) = 2.0*GAM(I)+1.0                      RAD00260
CALL LOGGAM (GAM(I),GNU,XRE,XIM)              RAD00270
ZK = TWORK*(TRK**GAM(I))*EXP(XRE)            RAD00280
IF (FKAP(I).GT.0.0)      GO TO 268             RAD00290
CF(I) = FKAP(I)-GAM(I)                        RAD00300
CG(I) = -ZAZA/CF(I)                           RAD00310
HM = ZAZA * EFN / ( CF(I) * ( E* FKAP(I) - GAM(I) ) ) RAD00320
HP = 2.0 - HM                                 RAD00330
HM = SQRT ( HM )                             RAD00340
HP = SQRT ( HP )                           RAD00350
G(I) = ZK * SQEG * ( GAM(I) * HP + GNU * HM ) RAD00360
F(I) = ZA*G(I)/CF(I)                         RAD00370
GO TO 270                                     RAD00380
268 CG(I) = -FKAP(I)-GAM(I)                   RAD00390
CF(I) = -ZAZA/CG(I)                           RAD00400
HP = -ZAZA * EGN * ( E*FKAP(I)+GAM(I) ) / CG(I) RAD00410
HP = HP / ( EFN * EGN * FKAP(I) + ZAZA )       RAD00420
HM = 2.0 - HP                                RAD00430
HM = SQRT ( HM )                             RAD00440
HP = SQRT ( HP )                           RAD00450
F(I) = ZK * SQE * ( GAM(I) * HM + GNU * HP ) RAD00460
G(I) = -ZA*F(I)/CG(I)                         RAD00470
270 DG(I) = F(I)*((1.0-CF(I))*EGN-CF(I)*EFN)/TUGAM(I) RAD00480
UF(I) = -G(I)*((1.0-(CG(I)))*EFN-CG(I)*EGN)/TUGAM(I) RAD00490
300 CONTINUE                                    RAD00500
GO TO 304                                     RAD00510
302 HAZ=SQRT (ZA)                            RAD00520
TUAZ = 2.0*ZA                                RAD00530
IEND = 1                                      RAD00540
DO 306 I=1,K2M                                RAD00550
GAM(I) = SQRT (FKAP(I)**2-ZAZA)                RAD00560
TUGAM(I) = 2.0 * GAM(I) + 1.0                  RAD00570
F(I) = HAZ*(TUAZ**GAM(I))                     RAD00580
IF (FKAP(I).GT.0.0)      GO TO 304             RAD00590
F(I) = -F(I)                                  RAD00600
CF(I) = FKAP(I)-GAM(I)                        RAD00610

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CG(I) = -ZAZA/CF(I) RAD00620
AZKAP = CF(I)/ZA RAD00630
GO TO 305 RAD00640
304 CG(I) = -FKAP(I)-GAM(I) RAD00650
CF(I) = -ZAZA/CG(I) RAD00660
AZKAP = -ZA/CG(I) RAD00670
305 G(I) = AZKAP*F(I) RAD00680
UF(I) = -F(I)*TUAZ/TUGAM(I) RAD00690
DG(I) = 2.0*F(I)*(1.0-CF(I))/TUGAM(I) RAD00700
306 CONTINUE RAD00710
307 NTAB = 1 RAD00720
M1 = LM+1 RAD00730
M2 = LM+2 RAD00740
IUP = MAXU (NK,NKP) RAD00750
DO 315 NO=1,IUP RAD00760
FK(NO) = 0.0 RAD00770
FKP(NO) = 0.0 RAD00780
DFK(NO) = 0.0 RAD00790
DFKP(NO) = 0.0 RAD00800
SFK(NO) = 0.0 RAD00810
315 SFKP(NO) = 0.0 RAD00820
DO 316 NO=1,K2M RAD00830
SF(NU) = 0.0 RAD00840
316 SG(NO) = 0.0 RAD00850
H=U.00/8125 RAD00860
N = 1.0/H + .1 RAD00870
RONE=1.0 RAD00880
DO 350 I=1·N RAD00890
350 CALL RKUT RAD00900
DO 365 I=1·K2M RAD00910
CALL LOGGAM (TUGAM(I),U,DUM1,DUM2)
RNORM(I) = EXP (-DUM1) RAD00920
F(I) = F(I)*RNORM(I) RAD00930
G(I) = G(I)*RNORM(I) RAD00940
DF(I) = DF(I)*RNORM(I) RAD00950
DG(I) = DG(I)*RNORM(I) RAD00960
SF(I) = SF(I)*RNORM(I) RAD00970
SG(I) = SG(I)*RNORM(I) RAD00980
CG(I) = FKAP(I) RAD00990
365 CG(I) = -FKAP(I) RAD01000
DO 500 N=1·NK RAD01010
I = KG(N) RAD01020
FK(N) = FK(N)*RNORM(I) RAD01030
DFK(N) = DFK(N)*RNORM(I) RAD01040
500 SFK(N) = SFK(N)*RNORM(I) RAD01050
DO 510 N=1·NKP RAD01060
I = KF(N) RAD01070
FKP(N) = FKP(N)*RNORM(I) RAD01080
DFKP(N) = DFKP(N)*RNORM(I) RAD01090
510 SFKP(N) = SFKP(N)*RNORM(I) RAD01100
WRITE ( 6, 100 ) RAD01110
WRITE ( 6,101 ) H·RONE RAD01120
H = U.125 RAD01130
XCUT = AMIN1 (KCUT,65.0) RAD01140
WRITE ( 6, 101 ) H, XCUT RAD01150
NEW = 1 RAD01160
CALL DERIV RAD01170
NDUN = (XCUT-1.0)/H+U.1 RAD01180
DO 370 NDU=1,NDUN RAD01190
370 CALL RKUT RAD01200
RX = XCUT RAD01210
IF (KCUT.LE.XCUT) GO TO 378 RAD01220

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NEW=1                               RAD01240
CALL XDERIV                         RAD01250
WAVE = AMAX1 (RK,Q)                 RAD01260
IH=PI/WAVE                          RAD01270
H=FLOAT (IH)/8.0                    RAD01280
IF (H.GT.1.0)      H=1.0            RAD01290
WRITE ( 6, 101 ) H, RCUT           RAD01300
LUB = (RCUT-RX)/H+0.1              RAD01310
DO 375 I=1,LUB                     RAD01320
375 CALL XHKUT                      RAD01330
378 CALL WNORM (RKNORM,NX)         RAD01340
  IF (IEND .EQ. 1)      GO TO 390   RAD01350
  M1 = KM + 2                     RAD01360
  M2 = KM + 3                     RAD01370
  Y = RK * RCUT                  RAD01380
  CALL SPHBES(Y)                 RAD01390
  DO 380 I=1,K2M                 RAD01400
    J1 = LMK(I) + 1               RAD01410
    J2 = LK(I) + 1               RAD01420
    SI(I) = RKE * SN(I) * G(I) * B(J1) - F(I) * B(J2)  RAD01430
    CR(I) = RKE * G(I) * B(J2) + SN(I) * F(I) * B(J1)  RAD01440
    RNM = SQRT ( SI(I) * SI(I) + CR(I) * CR(I) )        RAD01450
    SI(I) = SI(I) / RNM          RAD01460
    CR(I) = CR(I) / RNM          RAD01470
380U CONTINUE                      RAD01480
390U DO 400 K=1,NK                 RAD01490
  I = KG(K)                      RAD01500
  LTOT = LMKB+LK(I)+LBES(K)-1     RAD01510
  IF (MOD(LTOT,4).NE.0)      FK(K)=-FK(K)  RAD01520
400U FK(K) = FK(K)*RKNORM(1)       RAD01530
  DO 401 K=1,NKP                RAD01540
  I = KF(K)                      RAD01570
  LTOT = LMKB+LK(I)+LBES(K)-1     RAD01550
  IF (MOD(LTOT,4).NE.0)      FKP(K)=-FKP(K)  RAD01560
401 FKP(K) = FKP(K)*RNORM(I)      RAD01580
420U CALL HUM                      RAD01590
  RETURN                         RAD01600
  END                           RAD01610

```

SUBROUTINE RKUT

Purpose: Performs the Runge-Kutta integration. The routine uses indexed tabulated values of the bound-state wavefunction and the potential obtained previously by interpolation from the Waber output. Radial integration is performed up to a maximum of one-half Bohr radius.

Method: Runge-Kutta Integration (Gill Form). A fourth order integration scheme in which the error in each step is of the order h^5 , where h is the interval size.

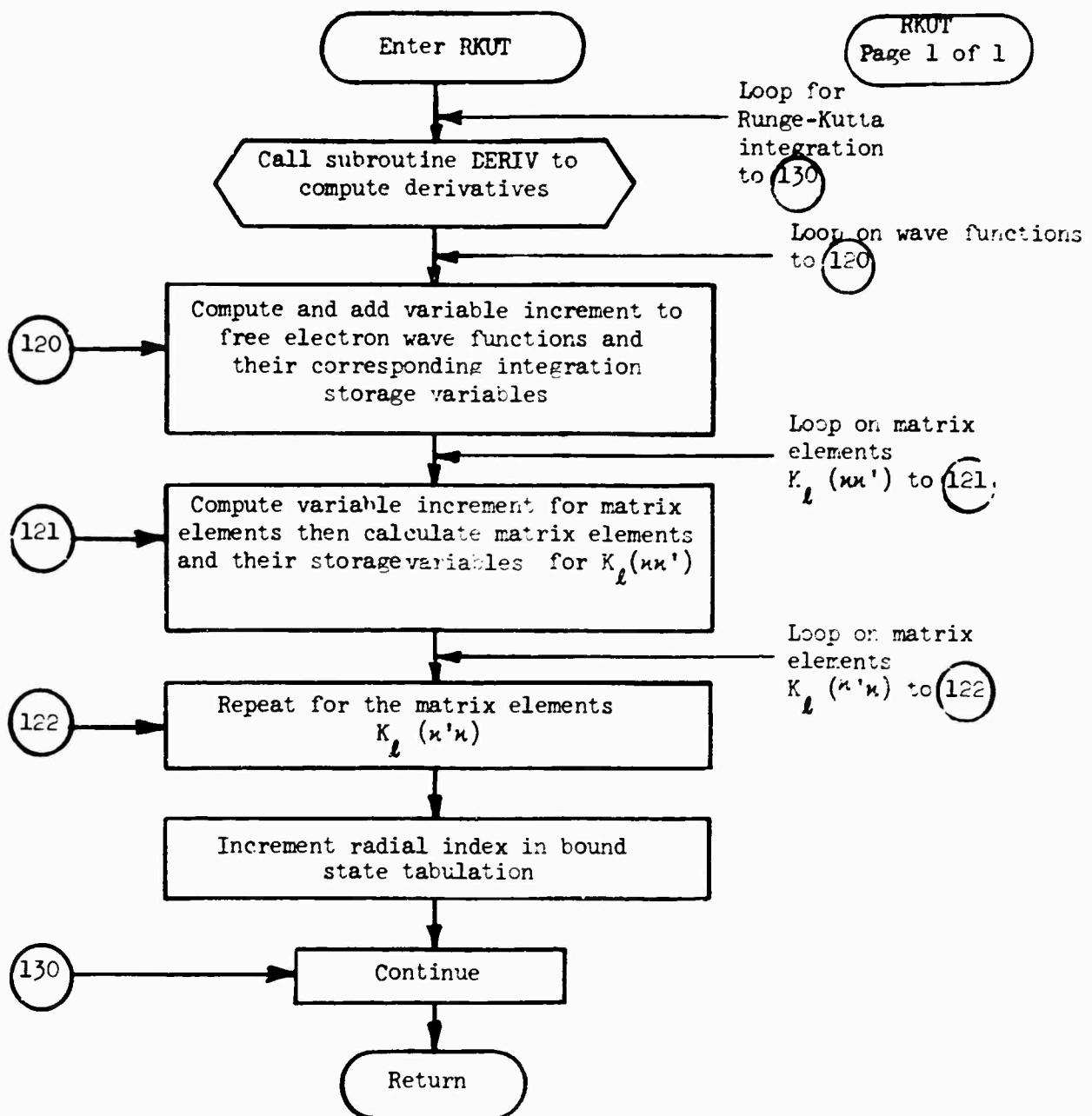
Subroutine called: DERIV

Subroutine called by: RADINT

Labelled Common: DFUNC, KUT, LIMIT, MAT, TAPES

Local Variables:

Name	Dimension	Mode	Meaning
J		I	Loop index on Runge-Kutta integration
I		I	Loop index on; number of free wavefunctions, number of matrix elements $K_{\mu\mu'}$ and $K_{\mu'\mu}$
Z		R	Incremental variable for "small" component of free electron wavefunction
ZP		R	Incremental variable for "large" component of free electron wavefunction



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S1BFC RKUG          RKU00010
      SUBROUTINE RKUT          RKU00020
C           RUNGE-KUTTA INTEGRATION          RKU00030
COMMON/DFUNC/F(30),G(30),DF(30),DG(30),DFK(200),DFKP(200),CF(30),HRKU00040
COMMON /KUT/RK1(4),RK2(4),RK3(4),RK4(4),K4(4)          RKU00050
COMMON/LIMIT/JM,LM,KM,K2M,IENU,NEW,NK,NKP,JKB,LMKB,NTAB          RKU00060
COMMON/MAT/SF(30),SG(30),FK(200),FKP(200),SFK(200),SFKP(200),RCUT          RKU00070
COMMON /TAPF/,X(1:1000),SCF(1500),FB(1500),GB(1500),GAMB,SCREEN          RKU00080
DO 130 J=1,+          RKU00090
CALL DERIV          RKU00100
DO 120 I=1,NK          RKU00110
Z = RK1(J)*(DF(I)-RK2(J)*SF(I))          RKU00120
ZP = RK1(J)*(DG(I)-RK2(J)*SG(I))          RKU00130
F(I) = F(I)+H*Z          RKU00140
G(I) = G(I)+H*ZP          RKU00150
SF(I) = SF(I)+3.0*Z-RK3(J)*DF(I)          RKU00160
120 SG(I) = SG(I)+3.0*ZP-RK3(J)*DG(I)          RKU00170
DO 121 I=1,NK          RKU00180
Z = RK1(J)*(DFK(I)-RK2(J)*SFK(I))          RKU00190
FK(I) = FK(I)+H*Z          RKU00200
121 SFK(I) = SFK(I)+3.0*Z-RK3(J)*DFK(I)          RKU00210
DO 122 I=1,NKP          RKU00220
Z = RK1(J)*(DFKP(I)-RK2(J)*SFKP(I))          RKU00230
FKP(I) = FKP(I)+H*Z          RKU00240
122 SFKP(I) = SFKP(I)+3.0*Z-RK3(J)*DFKP(I)          RKU00250
NTAB=NTAB+K4(J)          RKU00260
130 CONTINUE          RKU00270
RETURN          RKU00280
END

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SUBROUTINE SINDEX

Purpose: To catalogue and index matrix elements consistent with selection rules.

Method: Routine examines the angular momentum values to find and index all the matrix elements compatible with the selection rules and with the input cutoff values of the quantum numbers and records the free electron κ and the photon ℓ values for each matrix element in reference vectors (separately for the two kinds of matrix elements).

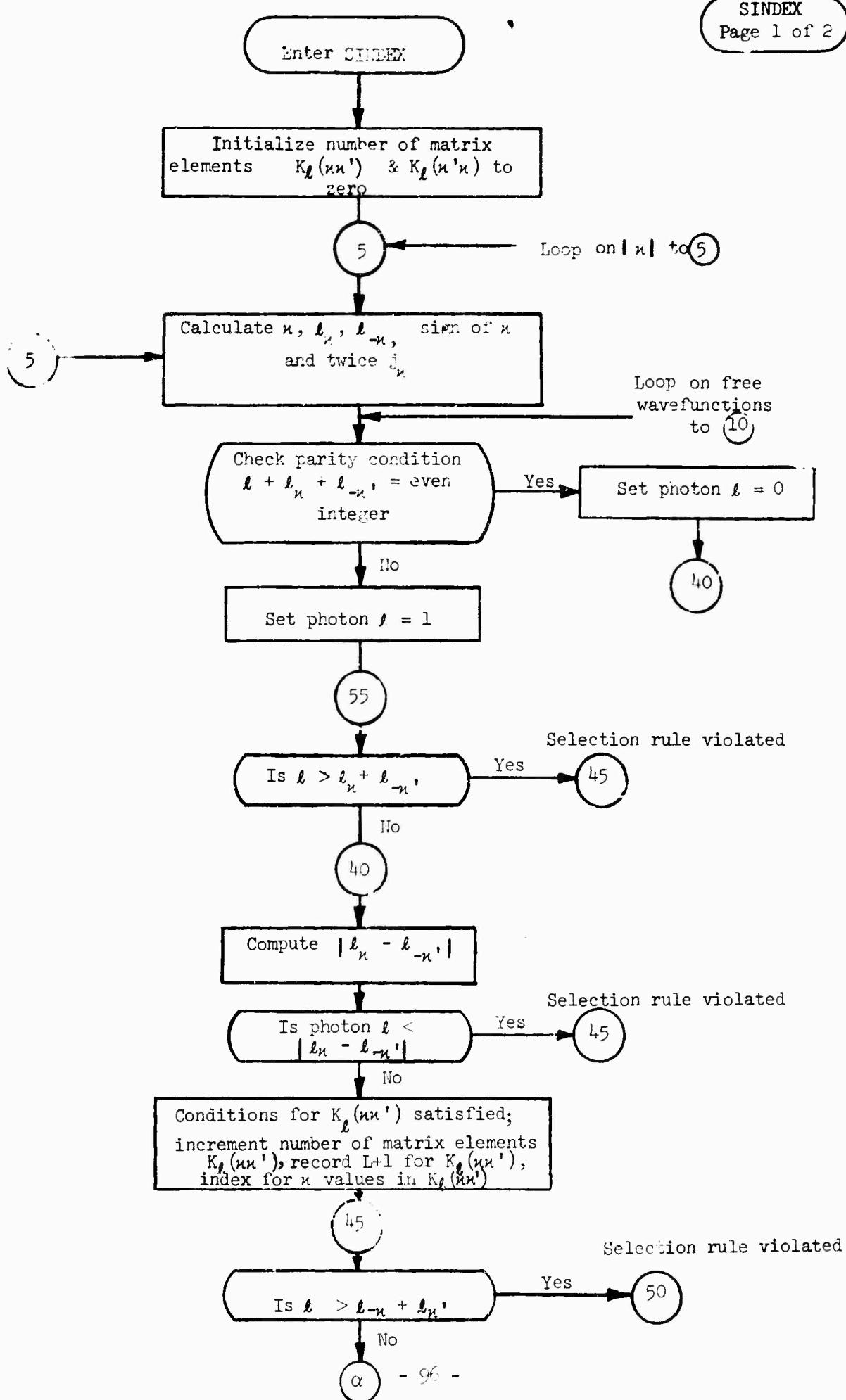
Subroutine called: None

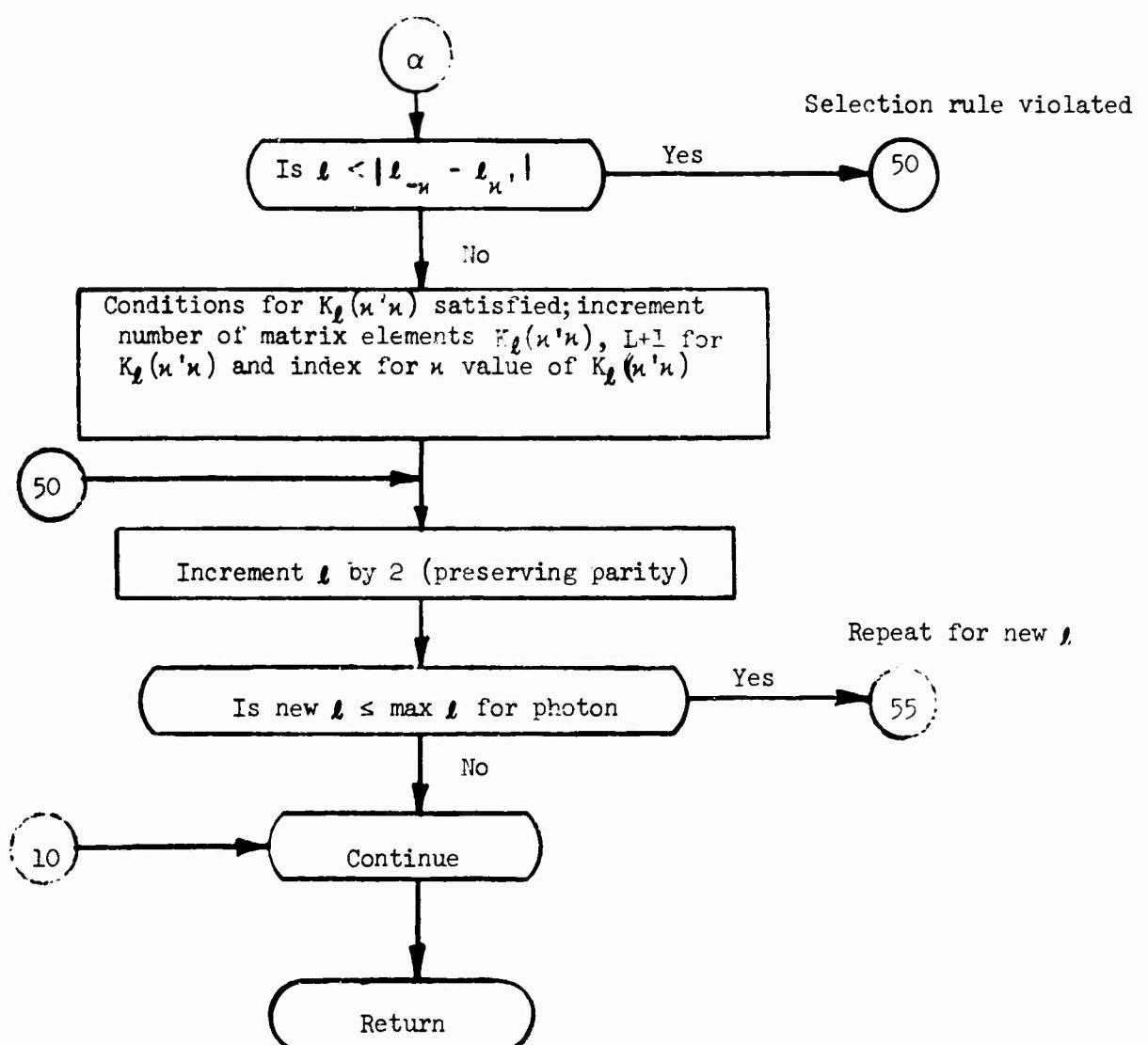
Subroutine called by: PELEC

Labelled \rightarrow : QUANT, VECT, LIMIT

Local Variables:

Name	Dimension	Mode	Meaning
I		I	Loop index on max κ for electron
K		I	Loop index on number of free electron states
LCUM		I	$\ell_\kappa + \ell_{-\kappa}$
LDIFF		I	$ \ell_\kappa - \ell_{-\kappa} $
L		I	Photon angular momentum





SIBFIC SIND

SUBROUTINE SINDEX	SND000010
COMMON/QUANT/LK(30),LMK(30),JK(30),FKAP(30),SN(30),SI(30),CR(30)	SND000020
COMMON/VECT/KF(200),KG(200),LBES(200),LBS(200),LKB	SND000030
COMMON /LIMIT/JM,LN,KM,K2M,IEND,NEW,NK,NKP,JKB,LMKB,NTAB	SND000040
NK=0	SND000050
NKP=0	SND000060
DO 5 I=1,KM	SND000070
K=2*I-1	SND000080
J=K+1	SND000090
FKAP(K)=-I	SND00100
FKAP(J)=I	SND00110
LK(K)=I-1	SND00120
LK(J)=I	SND00130
LMK(K)=I	SND00140
LMK(J)=I-1	SND00150
SN(K)=-1.0	SND00160
SN(J)=1.0	SND00170
JK(K)=LK(K)+LMK(K)	SND00180
5 JK(J)=JK(K)	SND00190
DO 10 K=1,K2M	SND00200
LSUM = LK(K)+LMKB	SND00210
IF (MOD(LSUM,2)) 35,30,35	SND00220
30 L=0	SND00230
GO TO 40	SND00240
55 L=1	SND00250
55 IF (L.GT.LSUM) GO TO 45	SND00260
40 LDIFF = IAHS (LK(K)-LMKB)	SND00270
IF (L.LT.LDIFF) GO TO 45	SND00280
NK=NK+1	SND00290
LBES(NK)=L+1	SND00300
KG(NK)=K	SND00310
45 LT=LMK(K)+LKB	SND00320
IF (L.GT.LT) GO TO 50	SND00330
LU=IAHS (LMK(K)-LKB)	SND00340
IF (L.LT.LU) GO TO 50	SND00350
NKP=NKP+1	SND00360
LBS(NKP)=L+1	SND00370
KF(NKP)=K	SND00380
50 L=L+2	SND00390
IF (L.LE.LM) GO TO 55	SND00400
10 CONTINUE	SND00410
RETURN	SND00420
END	SND00430

SUBROUTINE SPHBES

Purpose: Computes the values of the spherical Bessel function.

Method: The zero order function is obtained as $\sin R/R$. For small argument the higher order functions are calculated from the power series expansion. For large argument, the first order function is computed from its explicit sinusoidal representation and the remaining ones obtained by recursion relations. For intermediate arguments, the lower order functions are obtained by recursion, the higher order by power series.

Subroutines called: None

Subroutine called by: DERIV, XDERIV, RADINT

Labelled Common: BESEL

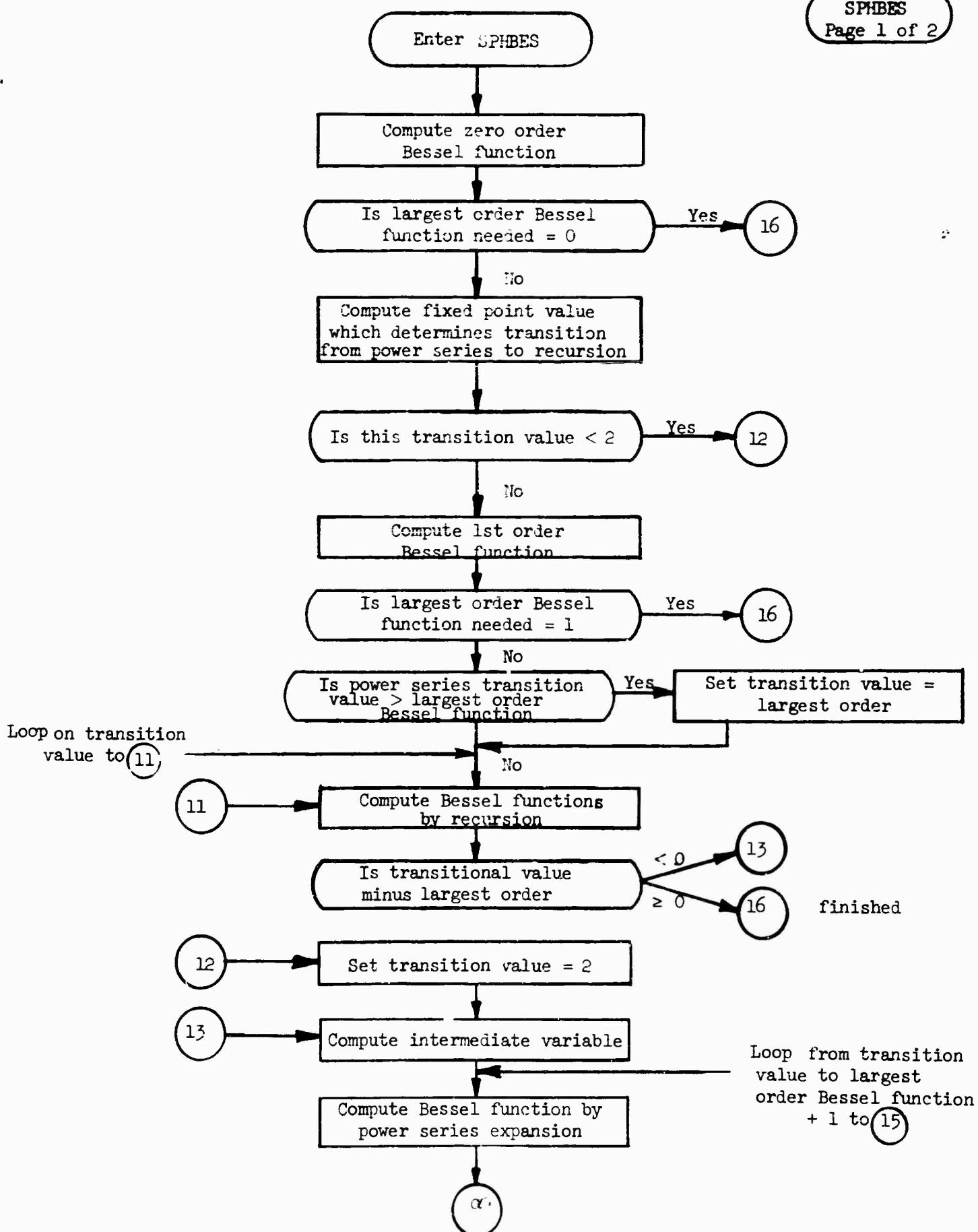
Argument sequence: (R)

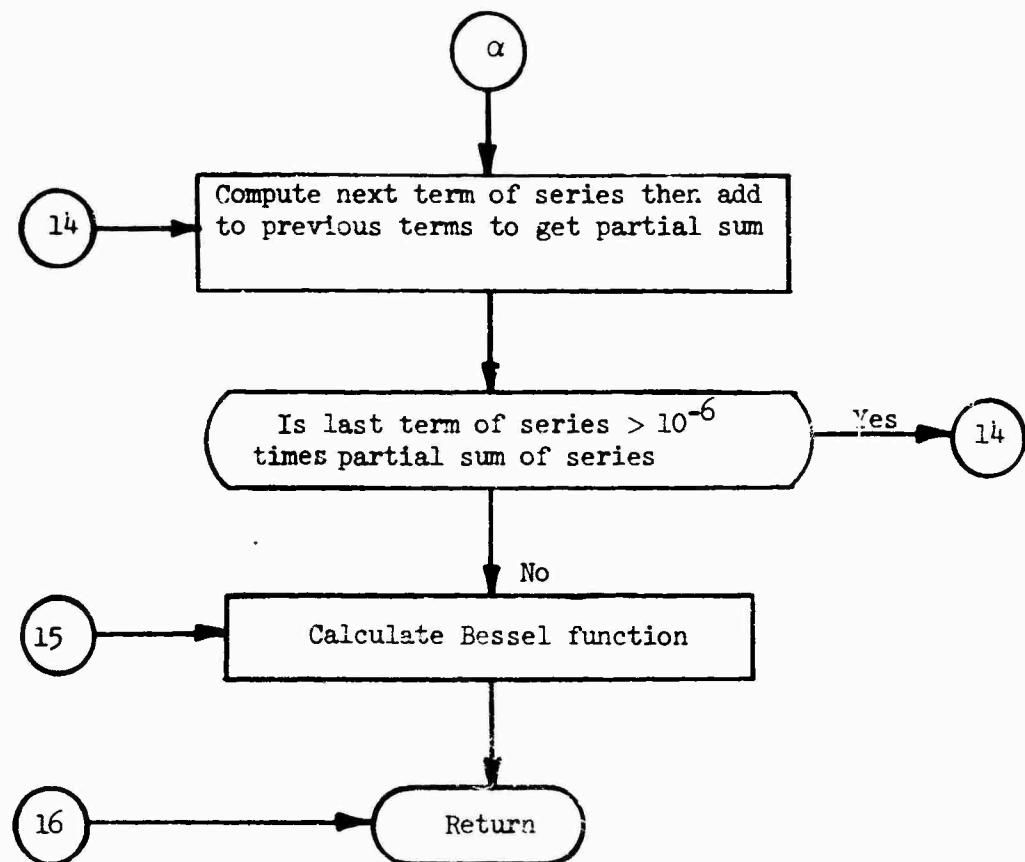
Argument List:

Name	Dimension	Mode	Meaning
R		R	Bessel function argument; photon momentum * radius from DERIV, XDERIV; free electron momentum x radius from RADINT.

Local Variables:

Name	Dimension	Mode	Meaning
NR		I	Defines transition from power series to recursion.
L		I	Loop index on calculating Bessel function.
SER		R	Partial sum of power series expansion.
TER		R	Last term of series expansion.





SUBRATIC SPHBS
 C SUBROUTINE SPHBS (R) SPH00010
 SPHERICAL BESSSEL FUNCTION SPH00020
 COMMON/BESSEL/FL(15),PC(15),OF(15,15),M1,M2,B(15) SPH00030
 OR = 1.0 / R SPH00040
 B(1) = SIN(R) * OR SPH00050
 IF (M1 .EQ. 1) GO TO 16 SPH00060
 NR = R + 2.0 SPH00070
 IF (NR .LT. 2) GO TO 12 SPH00080
 B(2) = (B(1) - COS(R)) * OR SPH00090
 IF (M1 .EQ. 2) GO TO 16 SPH00100
 IF (NR .GT. M1) NR=M1 SPH00110
 DO 11 L = 2, NR SPH00120
 11 B(L+1) = FL(L) * B(L) * OR - B(L-1) SPH00130
 IF (NR = M1) 13,16,16 SPH00140
 12 NR = 2 SPH00150
 13 HAS = 0.5 * R * R SPH00160
 DO 15 L = NR, M2 SPH00170
 J = U SPH00180
 SER = 1.0 SPH00190
 TER = 1.0 SPH00200
 14 J = J + 1 SPH0C210
 TER = - TER * HAS * OF(L,J) SPH00220
 SER = SER + TER SPH00230
 IF (ABS(TER) .GT. (0.000001 * ABS(SER))) GO TO 14 SPH00240
 15 B(L) = SER * PC(L) * (R**L) SPH00250
 16 RETURN SPH0G260
 END SPH00270

SUBROUTINE WNORM

Purpose: Computes the normalization factors for the free-electron wavefunction after termination of the numerical integration.

Method: The normalization factors are determined by a matching to the W.K.B. solution. Derivatives of the potential in the W.K.B. expression are obtained from a numerical fit of an exponential to the screening function (ratio of screened to unscreened potential) at the cutoff radius. When the W.K.B. conditions fail (vanishing kinetic energy and high angular momentum), the normalization factor of the previous wavefunctions is used.

Subroutine called: None

Subroutine called by: RADINT

Variables in unlabelled Common: PI, HALFPI, F0URPI, RAD, SQ2, Q, ZA, ZAZA,
EFN, EGN, V, CG, GAM

Labelled Common: DFUNC, LIMIT, TAPES

Argument sequence: (RN RM, RX)

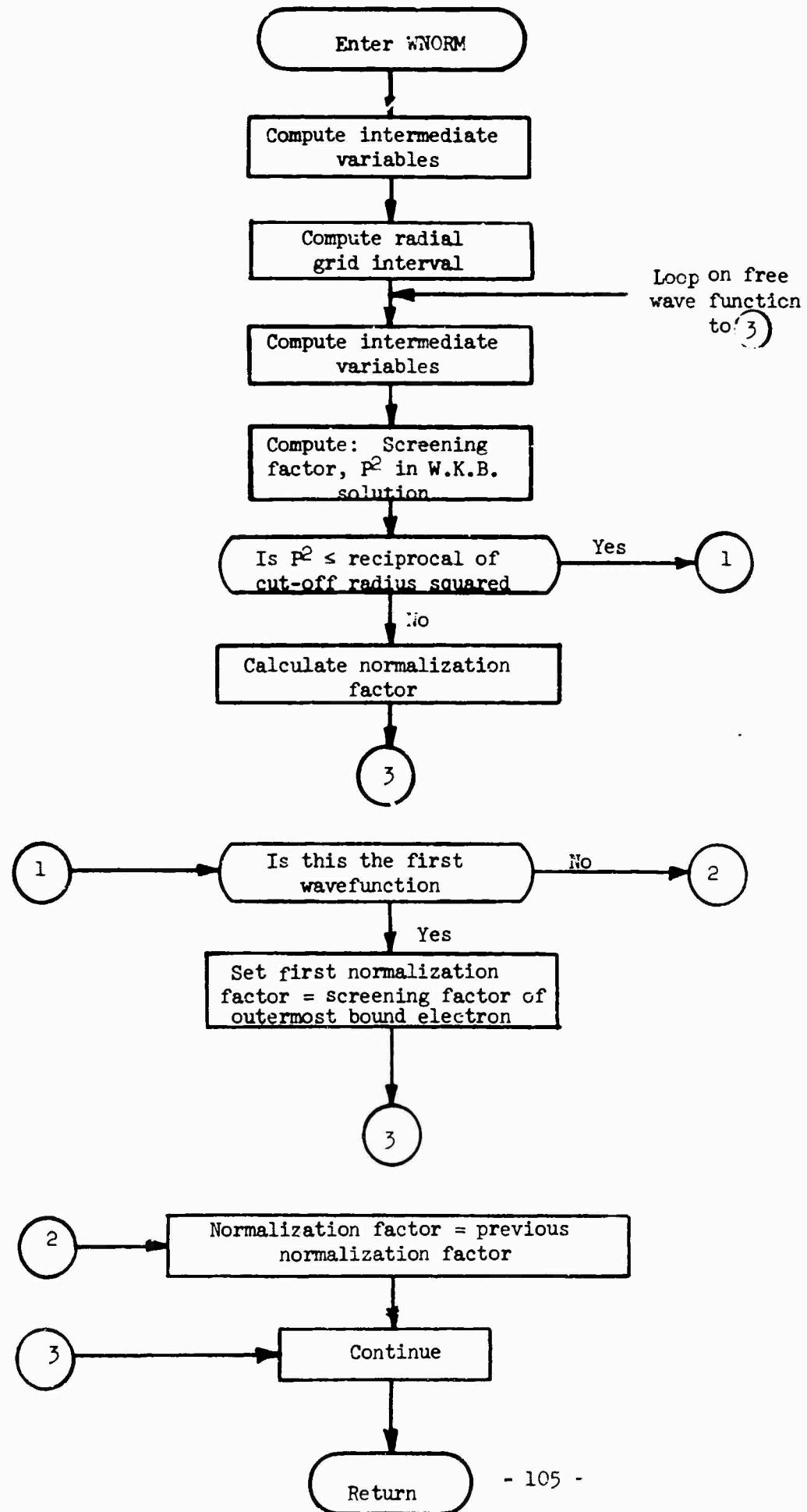
Argument List:

Name	Dimension	Mode	Meaning
WNORM	30	R	Normalization factors
RX		R	Terminal radius on numerical integration

Local Variables:

Name	Dimension	Mode	Meaning
ΦVERR		R	Reciprocal of terminal radius
EMVP1		R	Free electron energy - potential energy + 1
EMV		R	Free electron energy - potential energy
ΦRIGH		R	Radial grid interval
I		I	Loop index on number of free electron states

Name	Dimension	Mode	Meaning
RA, RB		R	Tabulated values of screening factor at grid points bracketing terminal radius
EP		R	Screening attenuation coefficient
P'Q		R	P^2 in W.K.B. solution
PSQP		R	Derivative of P^2



S1BFTC WNR

```

SUBROUTINE WNR (RNORM,RX) WNR00010
COMMON PI,HALFPI,FOURPI,RAD,SQ2,Q,ZA,ZAZA,EFN,EGN,V,CG(30),GAM(30) WNR00020
COMMON/UFUNC/F(30),G(30),DF(30),DG(30),DFK(200),DFKP(200),CF(30),HWR00030
COMMON/LIMIT/JM,LM,KM,K2M,IEND,NEW,NK,NKP,JKB,LMKB,NTAB WNR00040
COMMON/TAPES/X(1500),SCF(1500),FB(1500),GB(1500),GAMB,SCREEN WNR00050
DIMENSION RNORM(30) WNR00060
OVERR = 1.0 / RX WNR00070
OVRHSQ = OVERR*OVERR WNR00080
EMVP1 = EGN-V WNR00090
EMV = EMVP1-1.0 WNR00100
Y = -V/EMVP1 WNR00110
ORIGH = X(NTAB+1) - X(NTAB) WNR00120
DO 3 I=1,K2M WNR00130
PK = CF(I) WNR00140
FKSQ = PK*(PK+1.0) WNR00150
FKR = PK * OVERR WNR00160
FOR = FKSQ * OVRHSQ WNR00170
RA = SCF(NTAB) WNR00180
RB = SCF(NTAB+1) WNR00190
EP = ALOG(RA/RB)/ORIGH WNR00200
V1 = EP + OVERR WNR00210
V2 = V1 * V1 + OVRHSQ WNR00220
V3 = V1 * V2 + 2.0 * OVRHSQ * (V1 + OVERR) WNR00230
V1X = V1*Y WNR00240
V2X = V2*Y WNR00250
VXSQ = V1X * V1X WNR00260
FKVR = V1X*FKR WNR00270
PSQ = EMV * EMV - 1.0 + FKVR - 0.75 * VXSQ + 0.5 * V2X - FOR WNR00280
IF (PSQ.LE.OVRHSQ) GO TO 1 WNR00290
PSQP = 2.0 * EMV * V * V1 + (FKR - 1.5*V1X) * VXSQ + 2.0* V1X* V2X WNR00300
1   - 0.5 * V3 * Y - OVERR * (FKVR + PK*V2X - 2.0*FOR) WNR00310
TERM3 = G(1)*(0.5*V1X-FKR+0.25*(PSQP/PSQ))+F(1)*EMVP1 WNR00320
A = (PI/(SQRT(PSQ)*EMVP1))*(PSQ*G(I) +G(I) +TERM3*TERM3) WNR00330
RNORM(I) = 1.0/SQRT(A) WNR00340
GO TO 3 WNR00350
1 IF (I.GT.1) GO TO 2 WNR00360
RNORM(1)=SCREEN WNR00370
GO TO 3 WNR00380
2 RNORM(I)=RNORM(I-1) WNR00390
3 CONTINUE WNR00400
RETURN WNR00410
END WNR00420

```

SUBROUTINE XDERIV

Purpose: Supplies the derivatives for the Runge-Kutta integration of the bound-state wavefunctions and the integrands of the matrix elements for numerical integration beyond one-half Bohr radius.

Method: Calculates the derivatives of the radial components from the coupled Dirac radial equations and the integrand of the matrix elements using values obtained by linear interpolation on the Waber grid of bound state wavefunctions.

Subroutines called: SPHBES, INTERP

Subroutines called by: XRKUT, RADINT

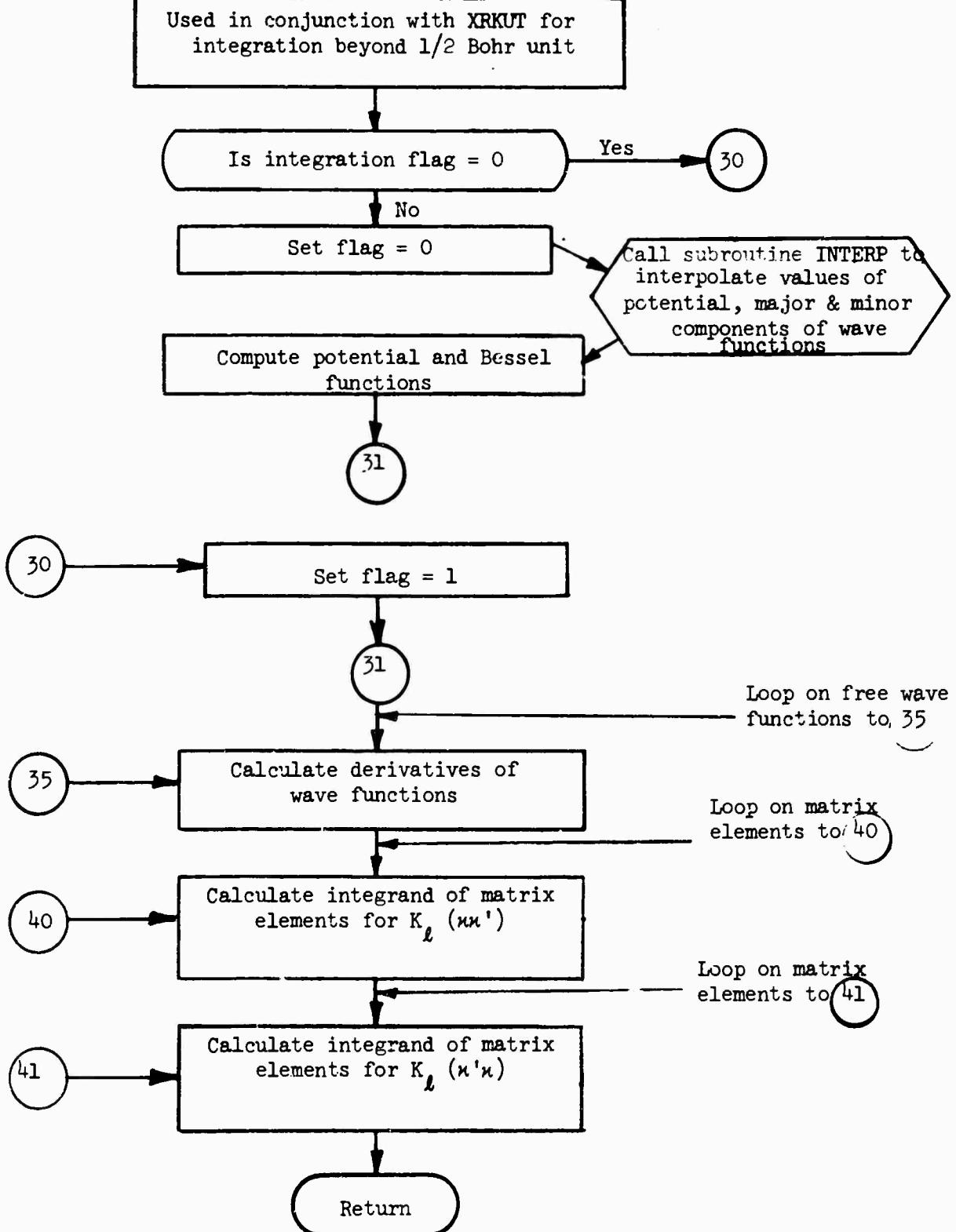
Labelled Common: BESSEL, DFUNCT, LIMIT, φNWARD, VECT

Local Variables:

Name	Dimension	Mode	Meaning
Z		R	Photon momentum * radius
N		I	Indexing variable

Enter XDERIV

XDERIV
Page 1 of 1



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S1BFC XDER
SUBROUTINE XDERIV          XDR00010
    COMPUTES DERIVATIVES      XDR00020
COMMON PI,HALFPI,FOURPI,RAU,SQ2,Q,ZA,ZAZA,EFN,EGN,V,CG(30),GAM(30) XDR00030
COMMON/BESSEL/FL(15),PC(15),OF(15,15),M1,M2,B(15)                  XDR00040
COMMON/DFUNC/F(30),G(30),DF(30),DG(30),DFK(200),DFKP(200),CF(30),HXDR00050
COMMON/LIMIT/JM,LM,KM,K2M,IENU,NEW,NK,NKP,JKB,LMB,NTAB             XDR00060
COMMON /ONWARD/RX,SCX,GBX,FBX                                     XDR00070
COMMON/VECT/KF(200),KG(200),LBES(200),LBS(200),LKB                XDR00080
IF (NEW.EQ.0)      GO TO 30                                      XDR00090
NEW = 0                                         XDR00100
CALL INTERP                                     XDR00110
V = - SCX / RX                                XDR00120
Z=0*RX                                         XDR00130
CALL SPHBS (2)                                 XDR00140
GO TO 31                                         XDR00150
30 NEW = 1                                       XDR00160
31 DO 35 N=1,K2M                                XDR00170
    UF(N) = CF(N)*F(N)/RX-(EFN-V)*G(N)           XDR00180
35 DG(N) = CG(N)*G(N)/RX+(EGN-V)*F(N)           XDR00190
DO 40 N=1,NK                                     XDR00200
    I = KG(N)                                     XDR00210
    L = LBES(N)                                  XDR00220
40 UFK(N) = B(L)*G(I)*FBX                      XDR00230
DO 41 N=1,NKP                                    XDR00240
    I = KF(N)                                     XDR00250
    L = LBS(N)                                   XDR00260
41 UFKP(N) = B(L)*F(I)*GBX                     XDR00270
RETURN                                         XDR00280
END                                           XDR00290

```

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SUBROUTINE XRKUT

Purpose: Performs the Runge-Kutta integration for radial values beyond one-half Bohr radius. The routine uses linearly interpolated values of the bound-state wavefunctions and the potential.

Method: Runge-Kutta Integration (Gill Form)

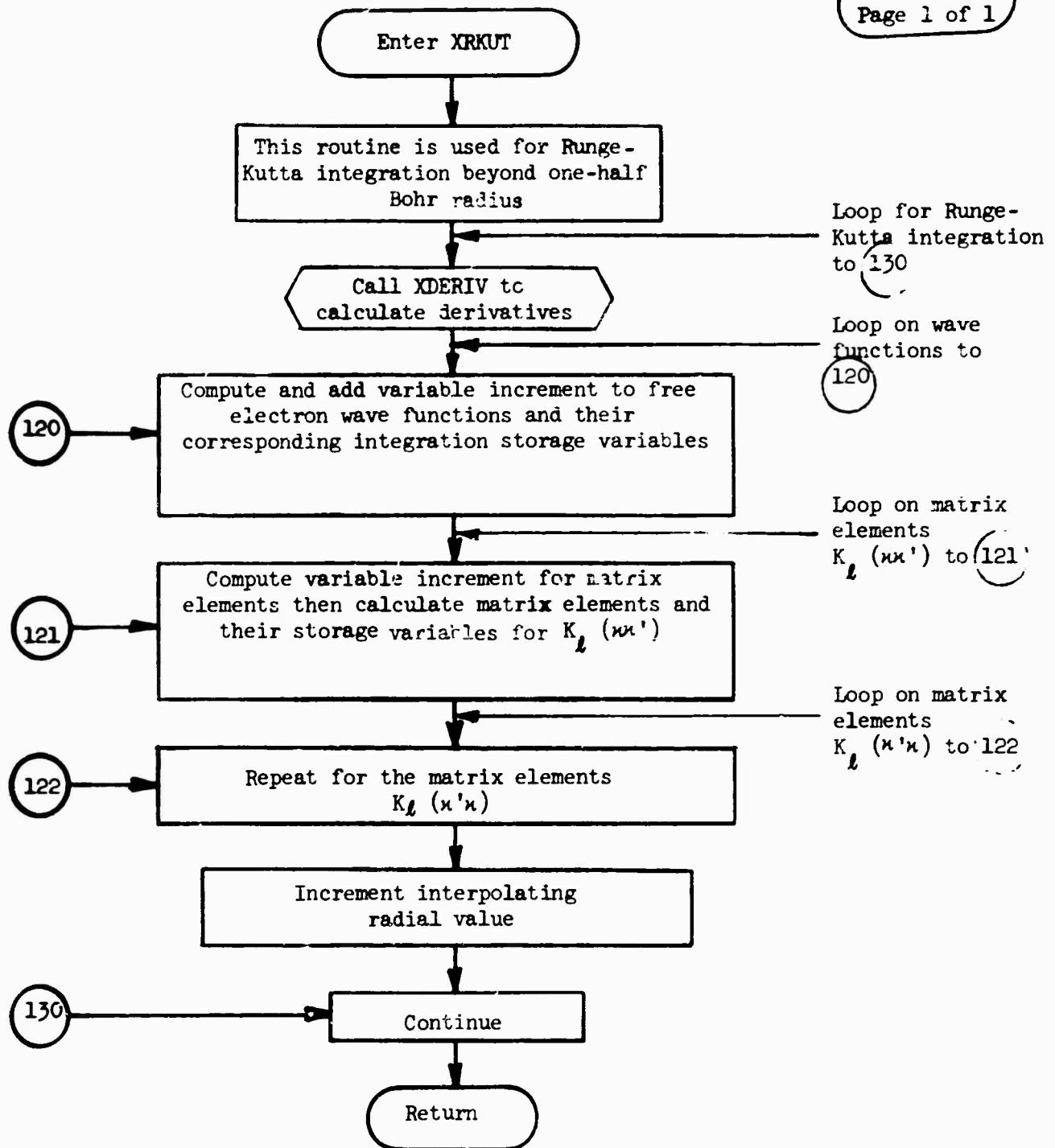
Subroutine called: XDERIV

Subroutine called by: RADINT

Labelled Common: DFUNC, KUT, LIMIT, MAT, ONWARD

Local Variables:

Name	Dimension	Mode	Meaning
J		I	Loop index on Runge-Kutta integration
I		I	Loop index on; number of free wavefunctions, number of matrix elements $K_{\ell}(nn')$ and $K_{\ell}(n'n)$
Z		R	Incremental variable for "small" component of free electron wavefunction
ZP		R	Incremental variable for "large" component of free electron wavefunction



```

S18F1C XRKU
    SUBROUTINE XRKUT                               XRK00010
C          RUNGE-KUTTA INTEGRATION                 XRK00020
COMMON/DFUNC/F(30),G(30),DF(30),DG(30),DFK(200),DFKP(200),CF(30),HXRK00030
COMMON /KUT/ RK1(4),RK2(4),RK3(4),RK4(4),K4(4)   XRK00040
COMMON/LIM1/I/JM,LM,KM,K2M,IENU,NEW,NK,NKP,JKB,LMKB,NTAB   XRK00050
COMMON/MAT/SF(30),SG(30),FK(200),FKP(200),SFK(200),SFKP(200),RCUT   XRK00060
COMMON /ONWARD/RX,SCX,GRX,FBX
DO 150 J=1,4
CALL XUEKIV
DO 120 I=1,K2M
Z = RK1(J)*(DF(I)-RK2(J)*SF(I))
ZP = RK1(J)*(UG(I)-RK2(J)*SG(I))
F(I) = F(I)+H*Z
G(I) = G(I)+H*ZP
SF(I) = SF(I)+3.0*Z-RK3(J)*DF(I)
120 SG(I) = SG(I)+3.0*ZP-RK3(J)*DG(I)
DO 121 I=1,NK
Z = RK1(J)*(DFK(I)-RK2(J)*SFK(I))
FK(I) = FK(I)+H*Z
121 SFK(I) = SFK(I)+3.0*Z-RK3(J)*DFK(I)
DO 122 I=1,NKP
Z = RK1(J)*(DFKP(I)-RK2(J)*SFKP(I))
FKP(I) = FKP(I)+H*Z
122 SFKP(I) = SFKP(I)+3.0*Z-RK3(J)*DFKP(I)
RX = RX+RK4(J)*H
150 CONTINUE
RETURN
END

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